

# Design of Parallel and High-Performance Computing

Fall 2015

*Lecture:* Locks and Lock-Free continued

*Motivational video:* <https://www.youtube.com/watch?v=-7Bpo1Quxyw>

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# Administrivia

## ■ Final presentations: Monday 12/14 (three weeks!)

- Should have (pretty much) final results
- Show us how great your project is
- Some more ideas what to talk about:

*Which architecture(s) did you test on?*

*How did you verify correctness of the parallelization?*

*Use bounds models for comparisons!*

*(Somewhat) realistic use-cases and input sets?*

*Emphasize on the key concepts (may relate to theory of lecture)!*

*What are remaining issues/limitations?*

## ■ Report will be due in January!

- Still, starting to write early is very helpful --- write – rewrite – rewrite (no joke!)
- Last 30 minutes today: Entertainment with bogus results!

# Review of last lecture

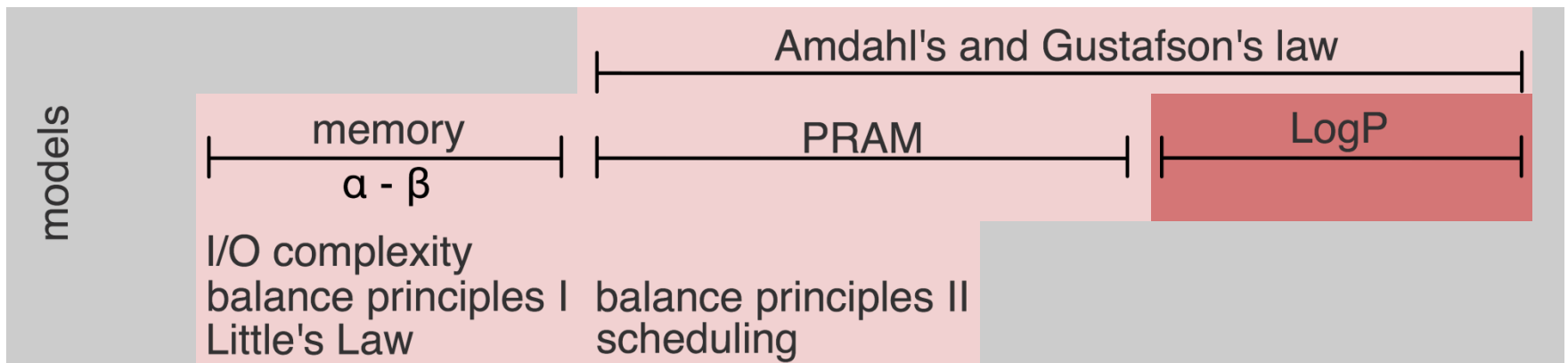
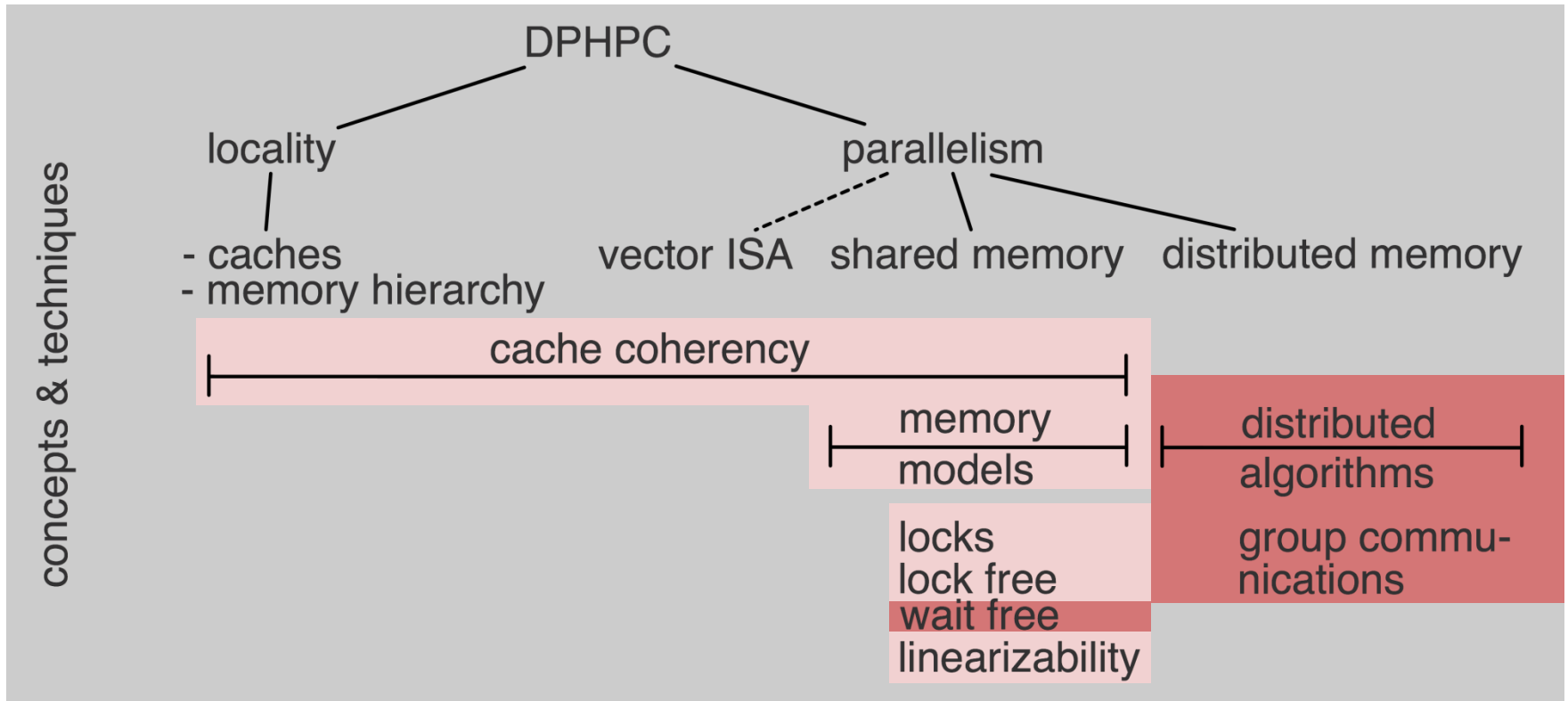
## ■ Abstract models

- Amdahl's and Gustafson's Law
- Little's Law
- Work/depth models and Brent's theorem
- I/O complexity and balance (Kung)
- Balance principles

## ■ Balance principles

- Outlook to the future
- Memory and data-movement will be more important

# DPHPC Overview



# Goals of this lecture

- **Recap MCS**

- Properties of locks

- **Lock-free tricks**

- List example but they generalize well

- **Finish wait-free/lock-free**

- Consensus hierarchy
- The promised proof!

- **Distributed memory**

- Models and concepts
- Designing (close-to) optimal communication algorithms

# MCS Lock (1991)

## ■ Make queue explicit

- Acquire lock by appending to queue
- Spin on own node until locked is reset

## ■ Similar advantages as CLH but

- Only  $2N + M$  words
- Spinning position is fixed!

*Benefits cache-less NUMA*

## ■ What are the issues?

- Releasing lock spins
- More atomics!

```
typedef struct qnode {
    struct qnode *next;
    int succ_blocked;
} qnode;
```

```
qnode *lck = NULL;
```

```
void lock(qnode *lck, qnode *qn) {
    qn->next = NULL;
    qnode *pred = FetchAndSet(lck, qn);
    if(pred != NULL) {
        qn->locked = 1;
        pred->next = qn;
        while(qn->locked);
    }
}
```

```
void unlock(qnode * lck, qnode *qn) {
    if(qn->next == NULL) { // if we're the last waiter
        if(CAS(lck, qn, NULL)) return;
        while(qn->next == NULL); // wait for pred arrival
    }
    qn->next->locked = 0; // free next waiter
    qn->next = NULL;
}
```

# Lessons Learned!

## ■ Key Lesson:

- Reducing memory (coherency) traffic is most important!
- Not always straight-forward (need to reason about CL states)

## ■ MCS: 2006 Dijkstra Prize in distributed computing

- *“an outstanding paper on the principles of distributed computing, whose significance and impact on the theory and/or practice of distributed computing has been evident for at least a decade”*
- *“probably the most influential practical mutual exclusion algorithm ever”*
- *“vastly superior to all previous mutual exclusion algorithms”*
- fast, fair, scalable → widely used, always compared against!

# Time to Declare Victory?

- **Down to memory complexity of  $2N+M$** 
  - Probably close to optimal
- **Only local spinning**
  - Several variants with low expected contention
- **But: we assumed sequential consistency ☹️**
  - Reality causes trouble sometimes
  - Sprinkling memory fences may harm performance
  - Open research on minimally-synching algorithms!  
*Come and talk to me if you're interested*



# More Practical Optimizations

## ■ Let's step back to “data race”

- (recap) two operations A and B on the same memory cause a data race if one of them is a write (“conflicting access”) and neither  $A \rightarrow B$  nor  $B \rightarrow A$
- So we put conflicting accesses into a CR and lock it!

*This also guarantees memory consistency in C++/Java!*

## ■ Let's say you implement a web-based encyclopedia

- Consider the “average two accesses” – do they conflict?

# Reader-Writer Locks

- **Allows multiple concurrent reads**

- Multiple reader locks concurrently in CR
- Guarantees mutual exclusion between writer and writer locks and reader and writer locks

- **Syntax:**

- `read_(un)lock()`
- `write_(un)lock()`

# A Simple RW Lock

## ■ Seems efficient!?

- Is it? What's wrong?
- Polling CAS!

## ■ Is it fair?

- Readers are preferred!
- Can always delay writers (again and again and again)

```
const W = 1;
const R = 2;
volatile int lock=0; // LSB is writer flag!
```

```
void read_lock(lock_t lock) {
    AtomicAdd(lock, R);
    while(lock & W);
}
```

```
void write_lock(lock_t lock) {
    while(!CAS(lock, 0, W));
}
```

```
void read_unlock(lock_t lock) {
    AtomicAdd(lock, -R);
}
```

```
void write_unlock(lock_t lock) {
    AtomicAdd(lock, -W);
}
```

# Fixing those Issues?

- Polling issue:
  - Combine with MCS lock idea of queue polling
- Fairness:
  - Count readers and writers

(1991)

## Scalable Reader-Writer Synchronization for Shared-Memory Multiprocessors

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### Abstract

Reader-writer synchronization relaxes the constraints of mutual exclusion to permit more than one process to inspect a shared object concurrently, as long as none of them changes its value. On uniprocessors, mutual exclusion and reader-writer locks are typically designed to de-schedule blocked processes; however, on shared-memory multiprocessors it is often advantageous to have processes busy wait. Unfortunately, implementations of busy-wait locks on shared-memory multiprocessors typically cause memory and network contention that degrades performance. Several researchers have shown how to implement scalable mutual exclusion locks that exploit locality in the memory hierarchies of shared-memory multiprocessors to eliminate contention for memory and for the processor-memory interconnect. In this paper we present reader-writer locks that similarly exploit locality to achieve scalability, with variants for reader preference, writer preference, and reader-writer fairness. Performance results on a BBN TC2000 multiprocessor demonstrate that our algorithms provide low latency and excellent scalability.

communication bandwidth, introducing performance bottlenecks that become markedly more pronounced in larger machines and applications. When many processors busy-wait on a single synchronization variable, they create a *hot spot* that gets a disproportionate share of the processor-memory bandwidth. Several studies [1, 4, 10] have identified synchronization hot spots as a major obstacle to high performance on machines with both bus-based and multi-stage interconnection networks.

Recent papers, ours among them [9], have addressed the construction of scalable, contention-free busy-wait locks for mutual exclusion. These locks employ atomic `fetch_and_φ` instructions<sup>1</sup> to construct queues of waiting processors, each of which spins only on *locally-accessible* flag variables, thereby inducing no contention. In the locks of Anderson [2] and Graunke and Thakkar [5], which achieve local spinning only on cache-coherent machines, each blocking processor chooses a unique location on which to spin, and this location becomes resident in the processor's cache. Our MCS mutual exclusion lock (algorithm 1) exhibits the dual advantages of (1) spinning on locally-accessible locations even on distributed shared-memory multiprocessors without coherent caches, and (2) requiring only  $O(P+N)$  space for  $N$  locks and  $P$  processors, rather than  $O(NP)$ .

The final algorithm (Alg. 4)  
has a flaw that was  
corrected in 2003!

# Deadlocks

- Kansas state legislature: *“When two trains approach each other at a crossing, both shall come to a full stop and neither shall start up again until the other has gone.”*

[according to Botkin, Harlow "A Treasury of Railroad Folklore" (pp. 381)]



**What are necessary conditions for deadlock?**

# Deadlocks

- **Necessary conditions:**
  - Mutual Exclusion
  - Hold one resource, request another
  - No preemption
  - Circular wait in dependency graph
- **One condition missing will prevent deadlocks!**
  - → Different avoidance strategies (which?)

# Issues with Spinlocks

- **Spin-locking is very wasteful**
  - The spinning thread occupies resources
  - Potentially the PE where the waiting thread wants to run → requires context switch!
- **Context switches due to**
  - Expiration of time-slices (forced)
  - Yielding the CPU

# What is this?





# Why is the 1997 Mars Rover in our lecture?

- It landed, received program, and worked ... until it spuriously rebooted!
  - → watchdog
- Scenario (vxWorks RT OS):
  - Single CPU
  - Two threads A,B sharing common bus, using locks
  - (independent) thread C wrote data to flash
  - Priority: A→C→B (A highest, B lowest)
  - Thread C would run into a livelock (infinite loop)
  - Thread B was preempted by C while holding lock
  - Thread A got stuck at lock ☹️

# Priority Inversion

- **If busy-waiting thread has higher priority than thread holding lock ⇒ no progress!**
- **Can be fixed with the help of the OS**
  - E.g., mutex priority inheritance (temporarily boost priority of task in CR to highest priority among waiting tasks)

# Condition Variables

- **Allow threads to yield CPU and leave the OS run queue**
  - Other threads can get them back on the queue!
- **cond\_wait(cond, lock) – yield and go to sleep**
- **cond\_signal(cond) – wake up sleeping threads**
- **Wait and signal are OS calls**
  - Often expensive, which one is more expensive?  
*Wait, because it has to perform a full context switch*

# Condition Variable Semantics

## ■ Hoare-style:

- Signaler passes lock to waiter, signaler suspended
- Waiter runs immediately
- Waiter passes lock back to signaler if it leaves critical section or if it waits again

## ■ Mesa-style (most used):

- Signaler keeps lock
- Waiter simply put on run queue
- Needs to acquire lock, may wait again

# When to Spin and When to Block?

- **Spinning consumes CPU cycles but is cheap**
  - “Steals” CPU from other threads
- **Blocking has high one-time cost and is then free**
  - Often hundreds of cycles (trap, save TCB ...)
  - Wakeup is also expensive (latency)  
*Also cache-pollution*
- **Strategy:**
  - Poll for a while and then block

# When to Spin and When to Block?

- What is a “while”?
- Optimal time depends on the future
  - When will the active thread leave the CR?
  - Can compute optimal offline schedule
  - Actual problem is an online problem
- Competitive algorithms
  - An algorithm is  $c$ -competitive if for a sequence of actions  $x$  and a constant  $a$  holds:
$$C(x) \leq c * C_{opt}(x) + a$$
  - What would a good spinning algorithm look like and what is the competitiveness?

# Competitive Spinning

- **If  $T$  is the overhead to process a wait, then a locking algorithm that spins for time  $T$  before it blocks is 2-competitive!**
  - Karlin, Manasse, McGeoch, Owicki: “Competitive Randomized Algorithms for Non-Uniform Problems”, SODA 1989
- **If randomized algorithms are used, then  $e/(e-1)$ -competitiveness ( $\sim 1.58$ ) can be achieved**
  - See paper above!

# Generalized Locks: Semaphores

- **Controlling access to more than one resource**
  - Described by Dijkstra 1965
- **Internal state is an atomic counter  $C$**
- **Two operations:**
  - $P()$  – block until  $C > 0$ ; decrement  $C$  (atomically)
  - $V()$  – signal and increment  $C$
- **Binary or 0/1 semaphore equivalent to lock**
  - $C$  is always 0 or 1, i.e.,  $V()$  will not increase it further
- **Trivia:**
  - If you're lucky (aehem, speak Dutch), mnemonics:  
*Verhogen (increment) and Prolaag (probeer te verlagen = try to reduce)*



# Semaphore Implementation

- **Can be implemented with mutual exclusion!**
  - And can be used to implement mutual exclusion 😊
- **... or with test and set and many others!**
- **Also has fairness concepts:**
  - Order of granting access to waiting (queued) threads
  - strictly fair (starvation impossible, e.g., FIFO)
  - weakly fair (starvation possible, e.g., random)

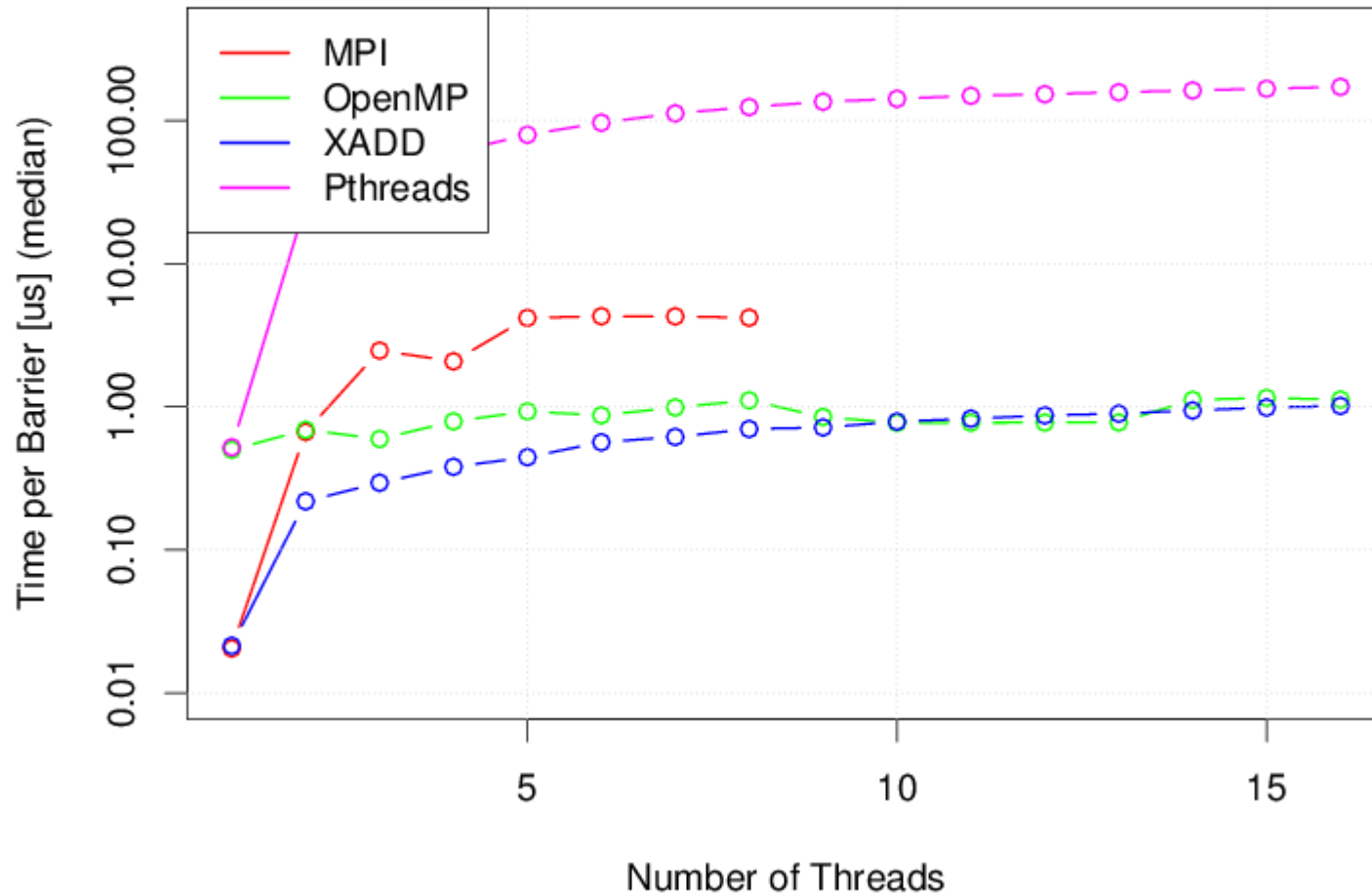
# Case Study 1: Barrier

- **Barrier semantics:**
  - No process proceeds before all processes reached barrier
  - Similar to mutual exclusion but not exclusive, rather “synchronized”
- **Often needed in parallel high-performance programming**
  - Especially in SPMD programming style
- **Parallel programming “frameworks” offer barrier semantics (pthread, OpenMP, MPI)**
  - `MPI_Barrier()` (process-based)
  - `pthread_barrier`
  - `#pragma omp barrier`
  - ...
- **Simple implementation: lock xadd + spin**

*Problem: when to re-use the counter?*

*Cannot just set it to 0 ☹️ → Trick: “lock xadd -1” when done 😊*

# Barrier Performance



# Case Study 2: Reasoning about Semantics

## Comments on a Problem in Concurrent Programming Control

Dear Editor:

I would like to comment on Mr. Dijkstra's solution [Solution of a problem in concurrent programming control. *Comm ACM* 8 (Sept. 1965), 569] to a messy problem that is hardly academic. We are using it now on a multiple computer complex.

When there are only two computers, the algorithm may be simplified to the following:

**Boolean array**  $b(0; 1)$  **integer**  $k, i, j,$

**comment** This is the program for computer  $i$ , which may be either 0 or 1, computer  $j \neq i$  is the other one, 1 or 0;

$C0$ :  $b(i) := \text{false};$

$C1$ : **if**  $k \neq i$  **then begin**

$C2$ : **if not**  $b(j)$  **then go to**  $C2$ ;

**else**  $k := i$ ; **go to**  $C1$  **end**;

**else** critical section;

$b(i) := \text{true};$

remainder of program;

**go to**  $C0$ ;

**end**

**CACM**

**Volume 9 Issue 1, Jan. 1966**

Mr. Dijkstra has come up with a clever solution to a really practical problem.

HARRIS HYMAN

*Munitype*

*New York, New York*

# Case Study 2: Reasoning about Semantics

- **Is the proposed algorithm correct?**
  - We may proof it manually
    - Using tools from the last lecture*
    - reason about the state space of H*
  - Or use automated proofs (model checking)
    - E.g., SPIN (Promela syntax)*

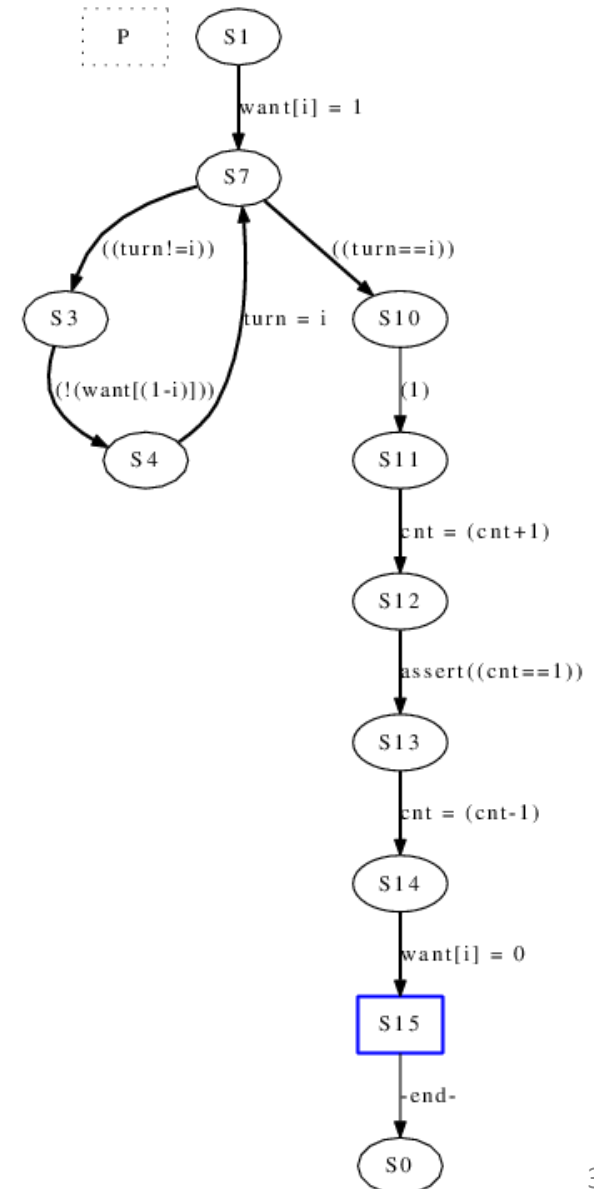
```
bool want[2];
bool turn;
byte cnt;

proctype P(bool i)
{
  want[i] = 1;
  do
    :: (turn != i) ->
      (!want[1-i]);
      turn = i
    :: (turn == i) ->
      break
  od;
  skip; /* critical section */
  cnt = cnt+1;
  assert(cnt == 1);
  cnt = cnt-1;
  want[i] = 0
}

init { run P(0); run P(1) }
```

# Case Study 2: Reasoning about Semantics

- Spin tells us quickly that it found a problem
  - A sequentially consistent order that violates mutual exclusion!
- It's not always that easy
  - This example comes from the SPIN tutorial
  - More than two threads make it much more demanding!
- More in the recitation!

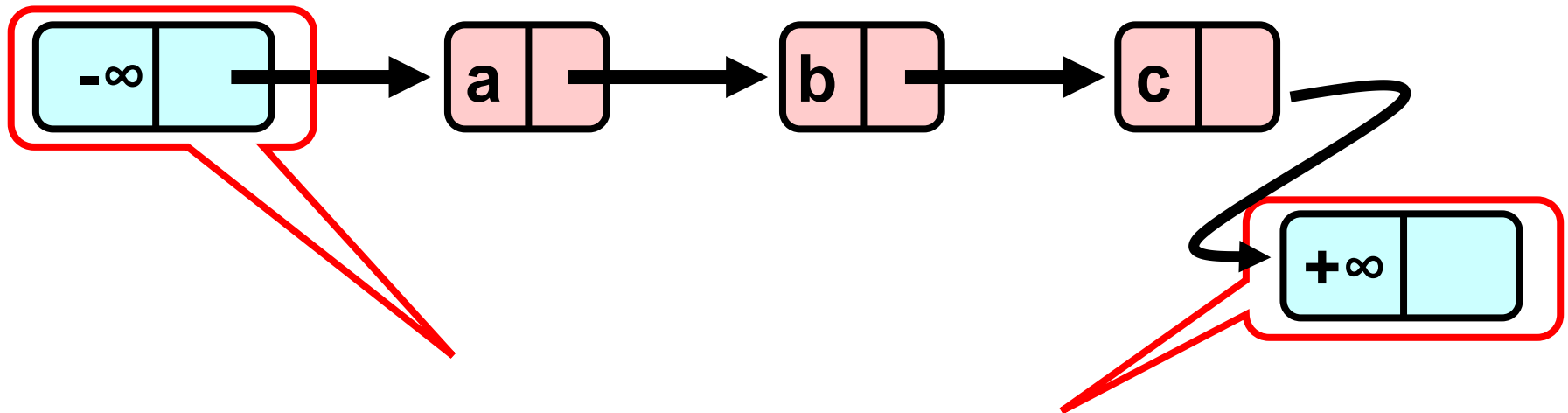


# Locks in Practice

- **Running example: List-based set of integers**
  - `S.insert(v)` – return true if `v` was inserted
  - `S.remove(v)` – return true if `v` was removed
  - `S.contains(v)` – return true iff `v` in `S`
- **Simple ordered linked list**
  - Do not use this at home (poor performance)
  - Good to demonstrate locking techniques
    - E.g., skip lists would be faster but more complex*

# Set Structure in Memory

- This and many of the following illustrations are provided by Maurice Herlihy in conjunction with the book “The Art of Multiprocessor Programming”



**Sorted with Sentinel nodes  
(min & max possible keys)**



# Sequential Set

```
boolean add(S, x) {
    node *pred = S.head;
    node *curr = pred.next;
    while(curr.key < x) {
        pred = curr;
        curr = pred.next;
    }
    if(curr.key == x)
        return false;
    else {
        node n = new node();
        n.key = x;
        n.next = curr;
        pred.next = n;
    }
    return true;
}
```

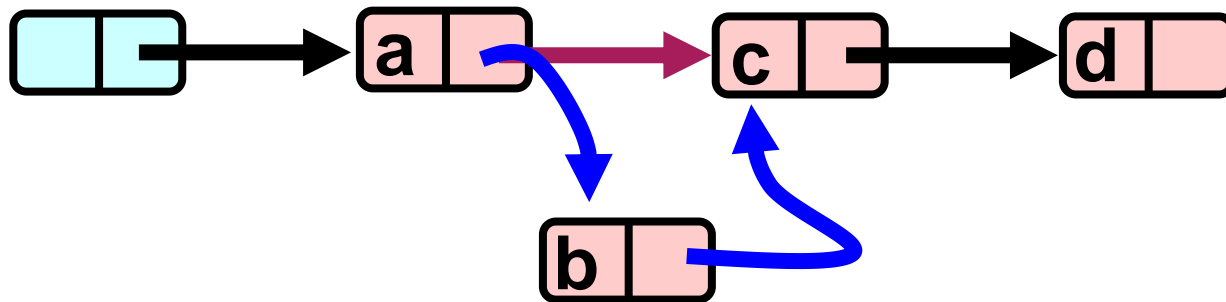
```
boolean remove(S, x) {
    node *pred = S.head;
    node *curr = pred.next;
    while(curr.key < x) {
        pred = curr;
        curr = pred.next;
    }
    if(curr.key == x) {
        pred.next = curr.next;
        free(curr);
        return true;
    }
    return false;
}
```

```
boolean contains(S, x) {
    int *curr = S.head;
    while(curr.key < x)
        curr = curr.next;
    if(curr.key == x)
        return true;
    return false;
}
```

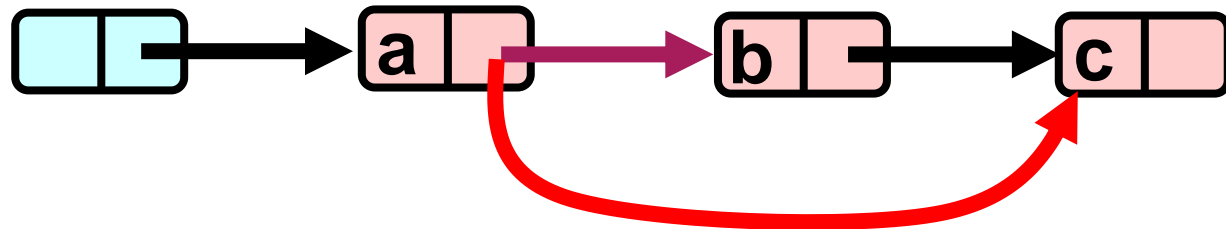
```
typedef struct {
    int key;
    node *next;
} node;
```

# Sequential Operations

add ( )



remove ( )



# Concurrent Sets

- **What can happen if multiple threads call set operations at the “same time”?**
  - Operations can conflict!
- **Which operations conflict?**
  - (add, remove), (add, add), (remove, remove), (remove, contains) will conflict
  - (add, contains) may miss update (which is fine)
  - (contains, contains) does not conflict
- **How can we fix it?**

# Coarse-grained Locking

```
boolean add(S, x) {  
    lock(S);  
    node *pred = S.head;  
    node *curr = pred.next;  
    while(curr.key < x) {  
        pred = curr;  
        curr = pred.next;  
    }  
    if(curr.key == x)  
        unlock(S);  
    return false;  
    else {  
        node node = malloc();  
        node.key = x;  
        node.next = curr;  
        pred.next = node;  
    }  
    unlock(S);  
    return true;  
}
```

```
boolean remove(S, x) {  
    lock(S);  
    node *pred = S.head;  
    node *curr = pred.next;  
    while(curr.key < x) {  
        pred = curr;  
        curr = pred.next;  
    }  
    if(curr.key == x) {  
        pred.next = curr.next;  
        unlock(S);  
        free(curr);  
        return true;  
    }  
    unlock(S);  
    return false;  
}
```

```
boolean contains(S, x) {  
    lock(S);  
    int *curr = S.head;  
    while(curr.key < x)  
        curr = curr.next;  
    if(curr.key == x) {  
        unlock(S);  
        return true;  
    }  
    unlock(S);  
    return false;  
}
```

# Coarse-grained Locking

## ■ Correctness proof?

- Assume sequential version is correct

*Alternative: define set of invariants and proof that initial condition as well as all transformations adhere (pre- and post conditions)*

- Proof that all accesses to shared data are in CRs

*This may prevent some optimizations*

## ■ Is the algorithm deadlock-free? Why?

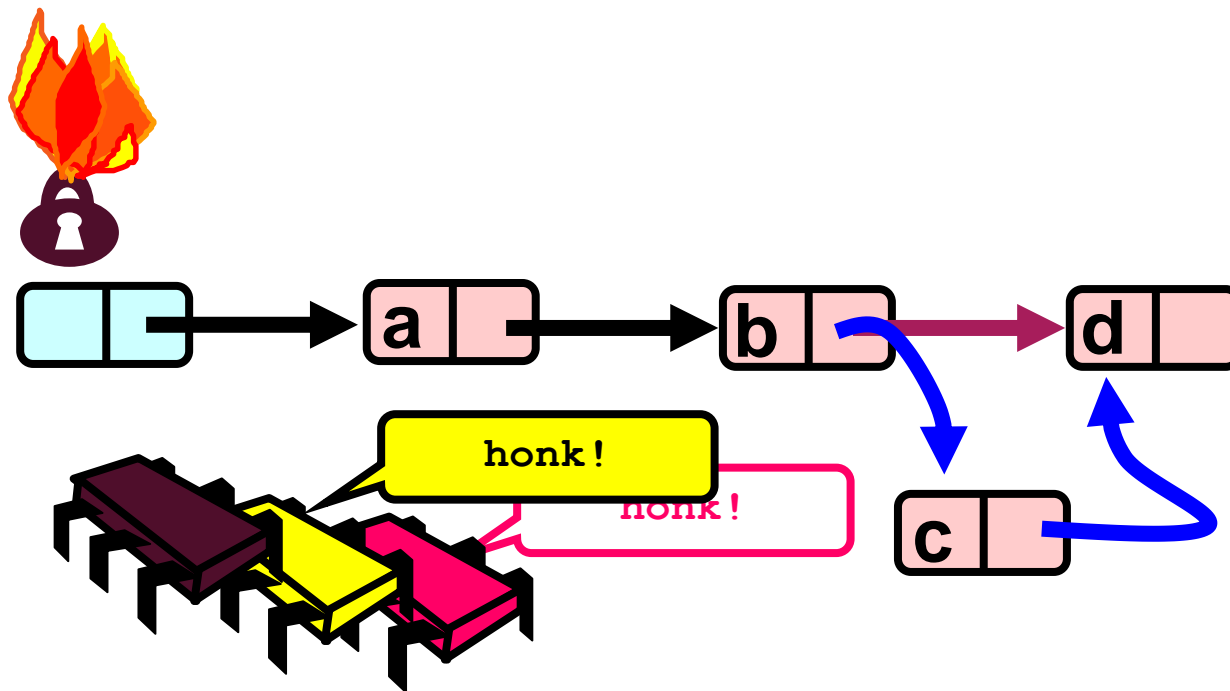
- Locks are acquired in the same order (only one lock)

## ■ Is the algorithm starvation-free and/or fair? Why?

- It depends on the properties of the used locks!

# Coarse-grained Locking

- Is the algorithm performing well with many concurrent threads accessing it?



Simple but **hotspot + bottleneck**

# Coarse-grained Locking

- Is the algorithm performing well with many concurrent threads accessing it?
  - No, access to the whole list is serialized
- **BUT: it's easy to implement and proof correct**
  - Those benefits should **never** be underestimated
  - May be just good enough
  - *“We should forget about small efficiencies, say about 97% of the time: **premature optimization is the root of all evil**. Yet we should not pass up our opportunities in that critical 3%. A good programmer will not be lulled into complacency by such reasoning, he will be wise to look carefully at the critical code; but only after that code has been identified”* — Donald Knuth (in *Structured Programming with Goto Statements*)

# How to Improve?

- **Will present some “tricks”**
  - Apply to the list example
  - But often generalize to other algorithms
  - Remember the trick, not the example!
- **See them as “concurrent programming patterns” (not literally)**
  - Good toolbox for development of concurrent programs
  - They become successively more complex



# Tricks Overview

## 1. Fine-grained locking

- Split object into “lockable components”
- Guarantee mutual exclusion for conflicting accesses to same component

## 2. Reader/writer locking

## 3. Optimistic synchronization

## 4. Lazy locking

## 5. Lock-free

# Tricks Overview

## 1. Fine-grained locking

## 2. Reader/writer locking

- Multiple readers hold lock (traversal)
- contains() only needs read lock
- Locks may be upgraded during operation

*Must ensure starvation-freedom for writer locks!*

## 3. Optimistic synchronization

## 4. Lazy locking

## 5. Lock-free

# Tricks Overview

1. **Fine-grained locking**
2. **Reader/writer locking**
3. **Optimistic synchronization**
  - Traverse without locking  
*Need to make sure that this is correct!*
  - Acquire lock if update necessary  
*May need re-start from beginning, tricky*
4. **Lazy locking**
5. **Lock-free**

# Tricks Overview

1. **Fine-grained locking**
2. **Reader/writer locking**
3. **Optimistic synchronization**
4. **Lazy locking**
  - Postpone hard work to idle periods
  - Mark node deleted  
*Delete it physically later*
5. **Lock-free**

# Tricks Overview

1. **Fine-grained locking**
2. **Reader/writer locking**
3. **Optimistic synchronization**
4. **Lazy locking**
5. **Lock-free**
  - Completely avoid locks
  - Enables wait-freedom
  - Will need atomics (see later why!)
  - Often very complex, sometimes higher overhead

# Trick 1: Fine-grained Locking

- **Each element can be locked**

- High memory overhead
- Threads can traverse list concurrently like a pipeline

- **Tricky to prove correctness**

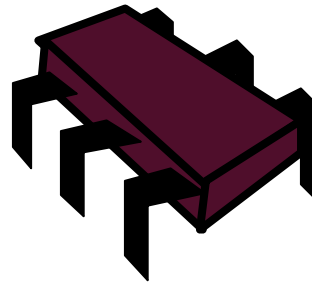
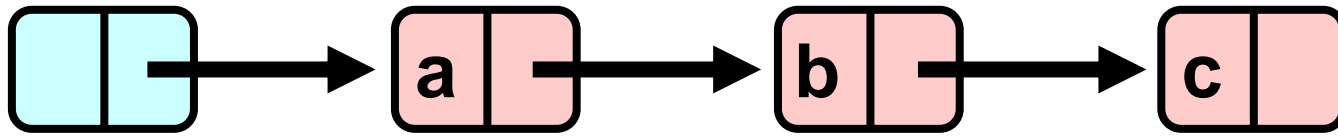
- And deadlock-freedom
- Two-phase locking (acquire, release) often helps

- **Hand-over-hand (coupled locking)**

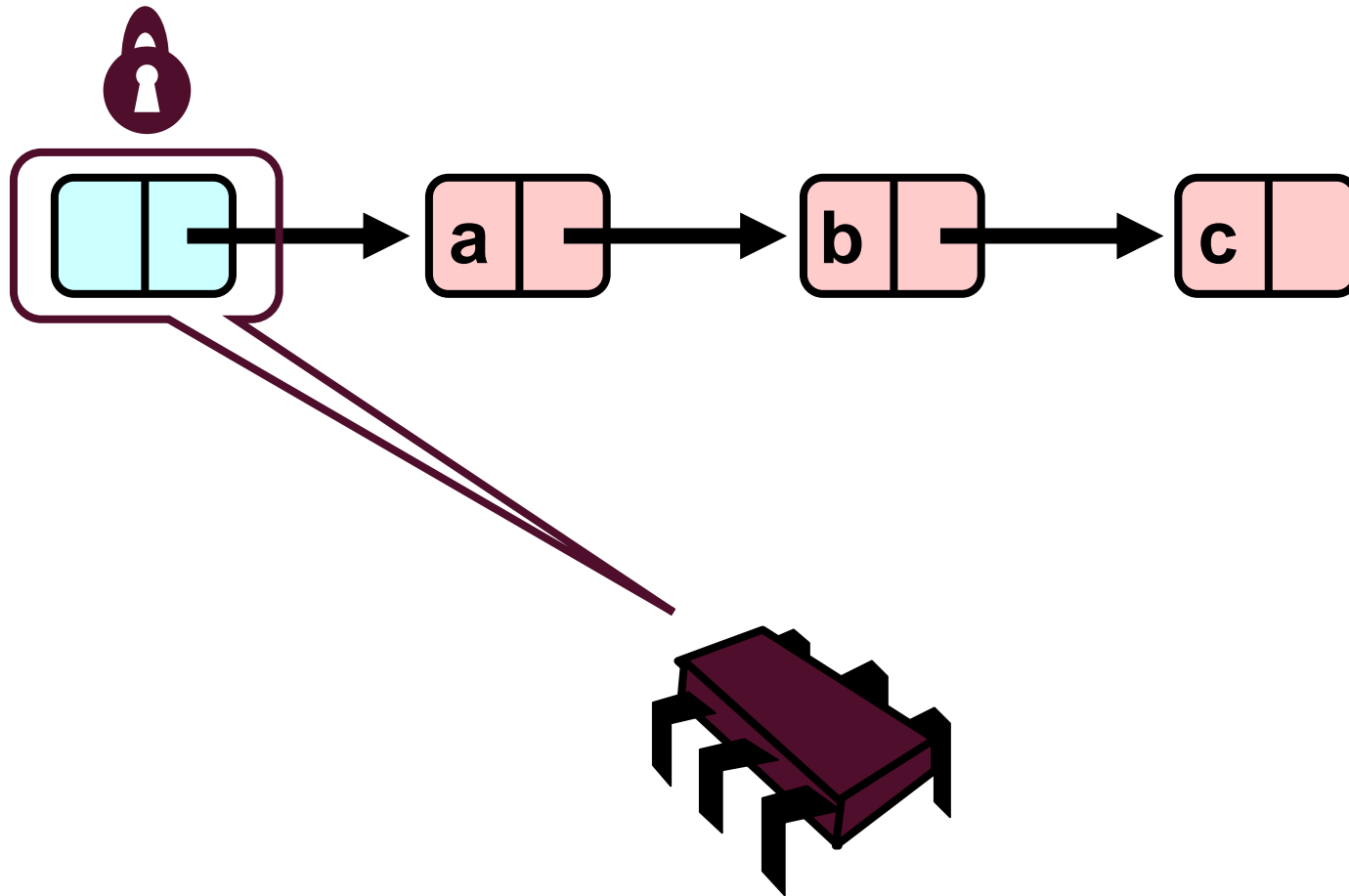
- Not safe to release x's lock before acquiring x.next's lock  
*will see why in a minute*
- Important to acquire locks in the same order

```
typedef struct {  
    int key;  
    node *next;  
    lock_t lock;  
} node;
```

# Hand-over-Hand (fine-grained) locking

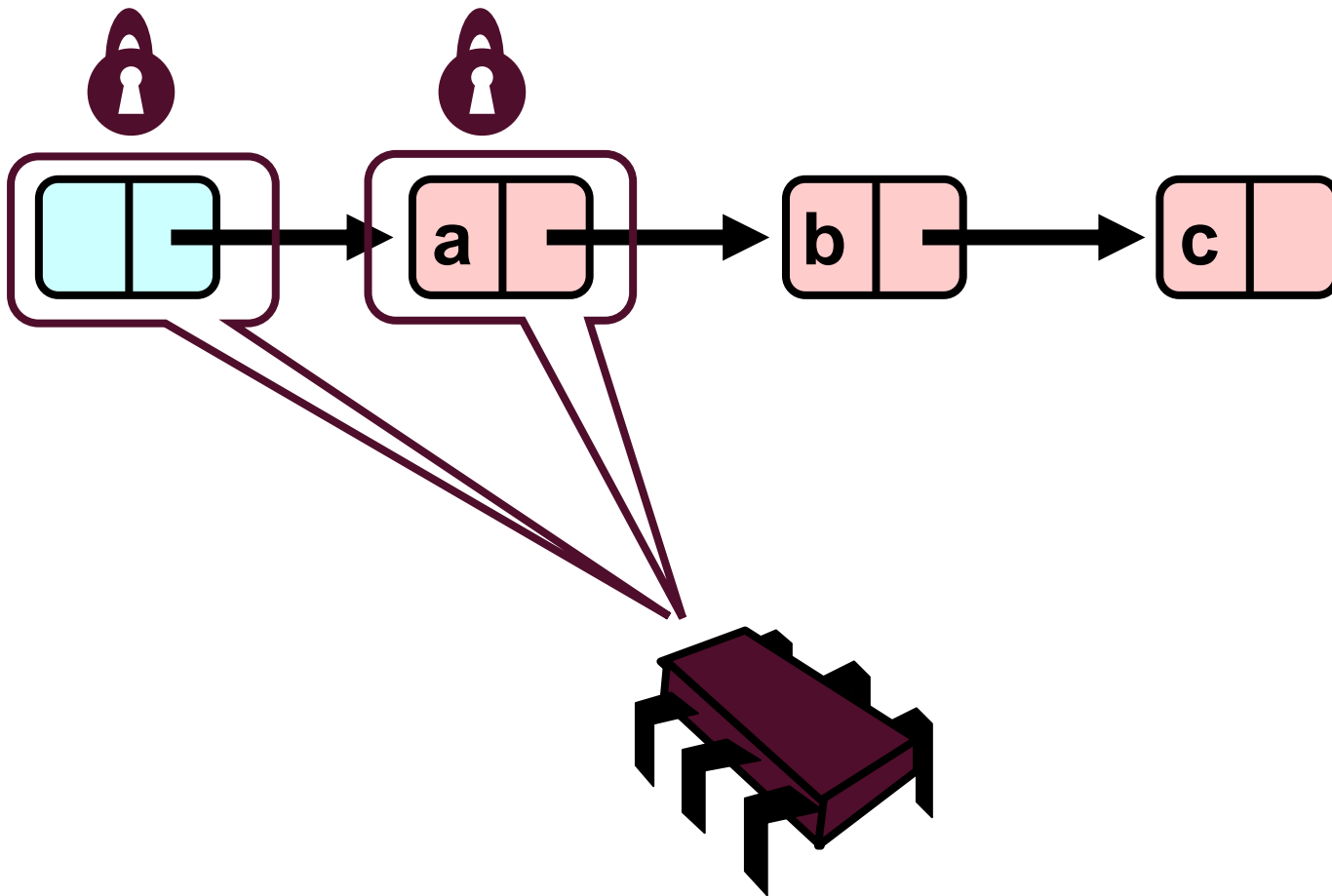


# Hand-over-Hand (fine-grained) locking

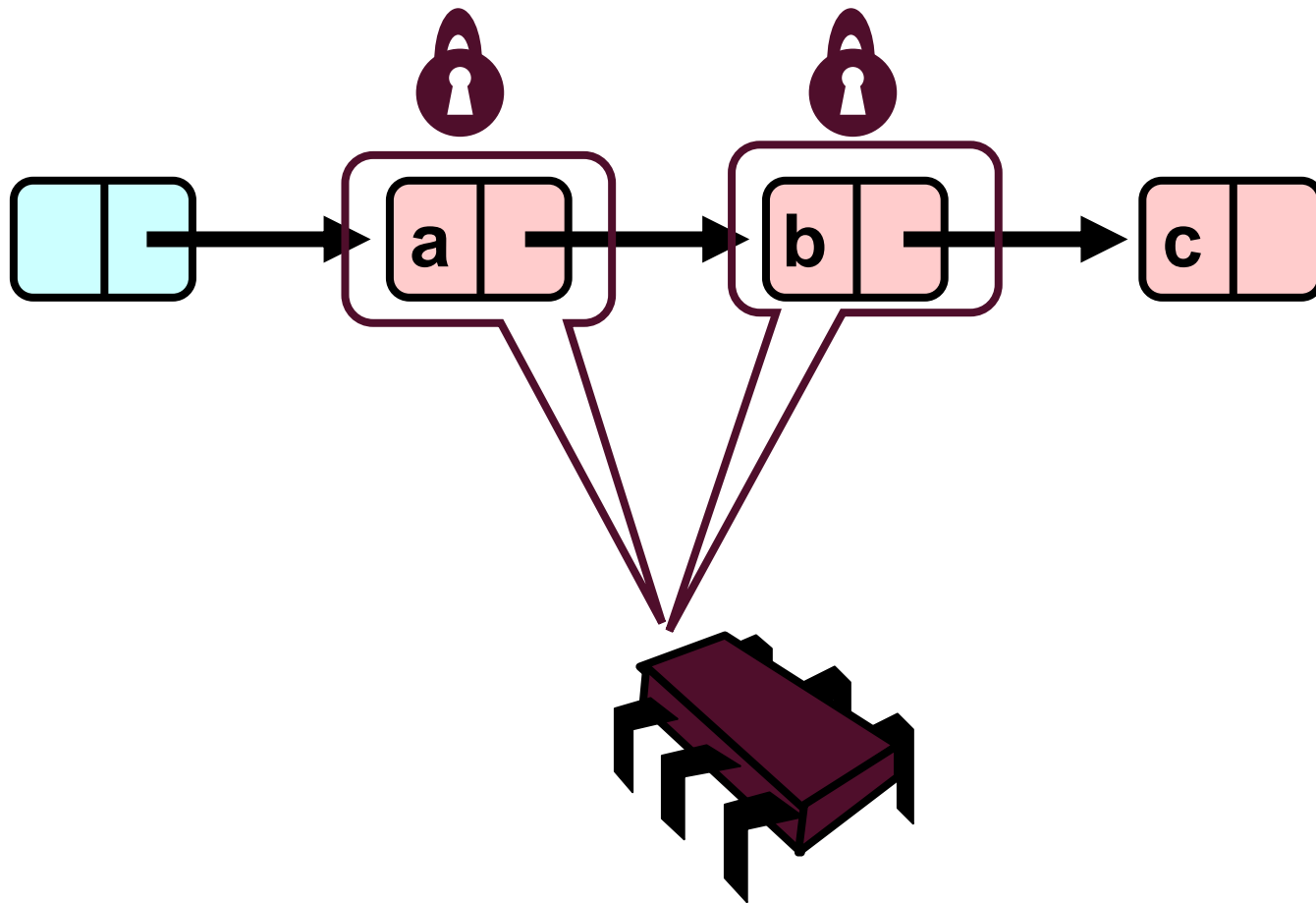




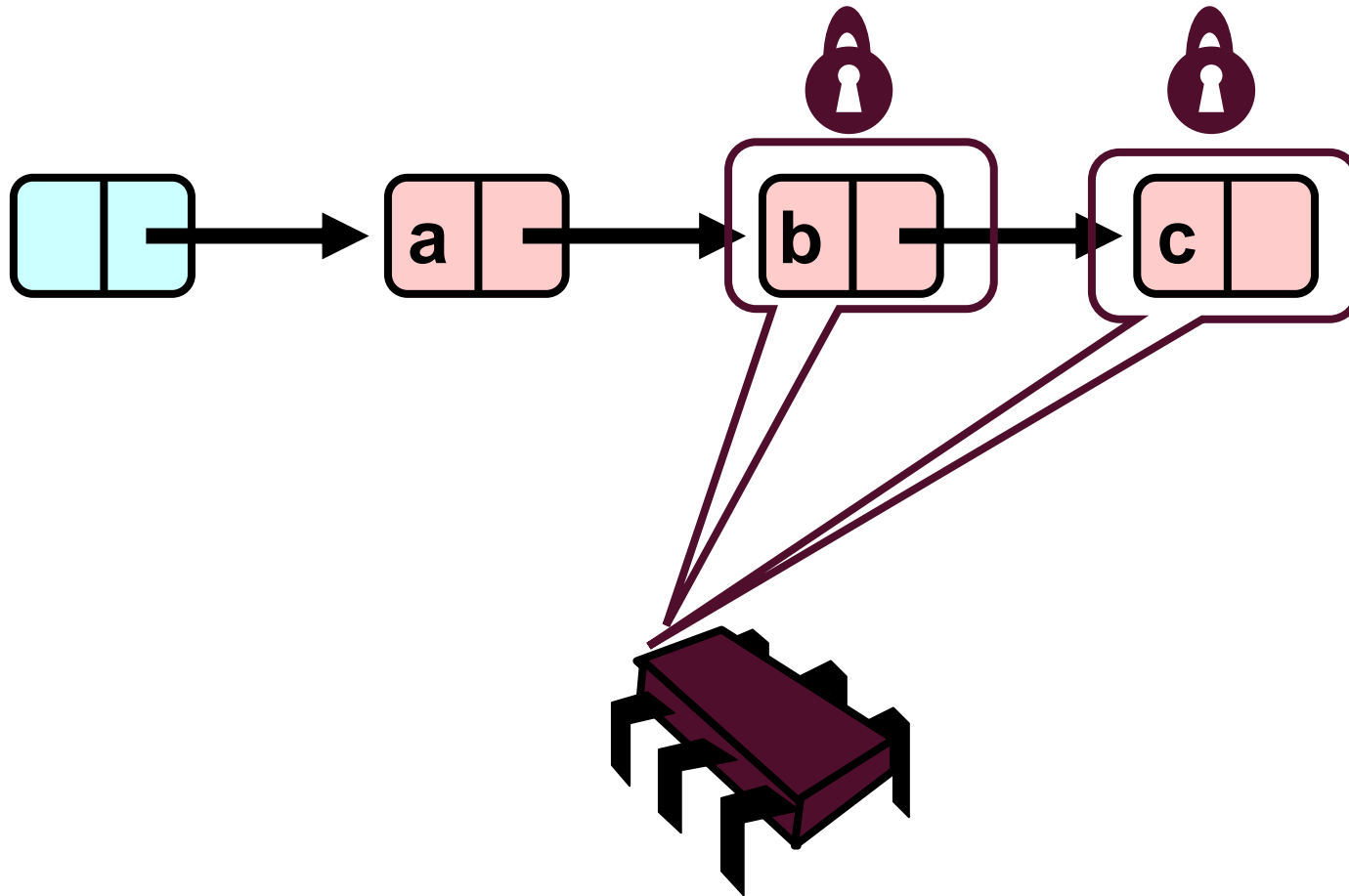
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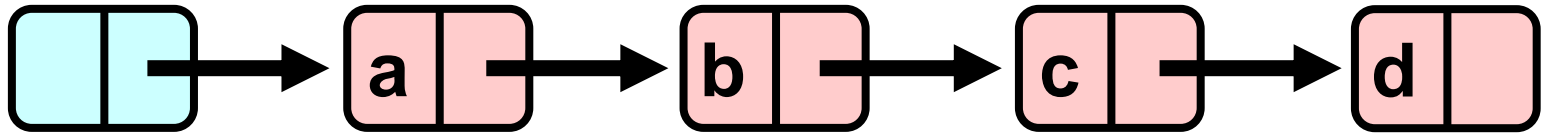
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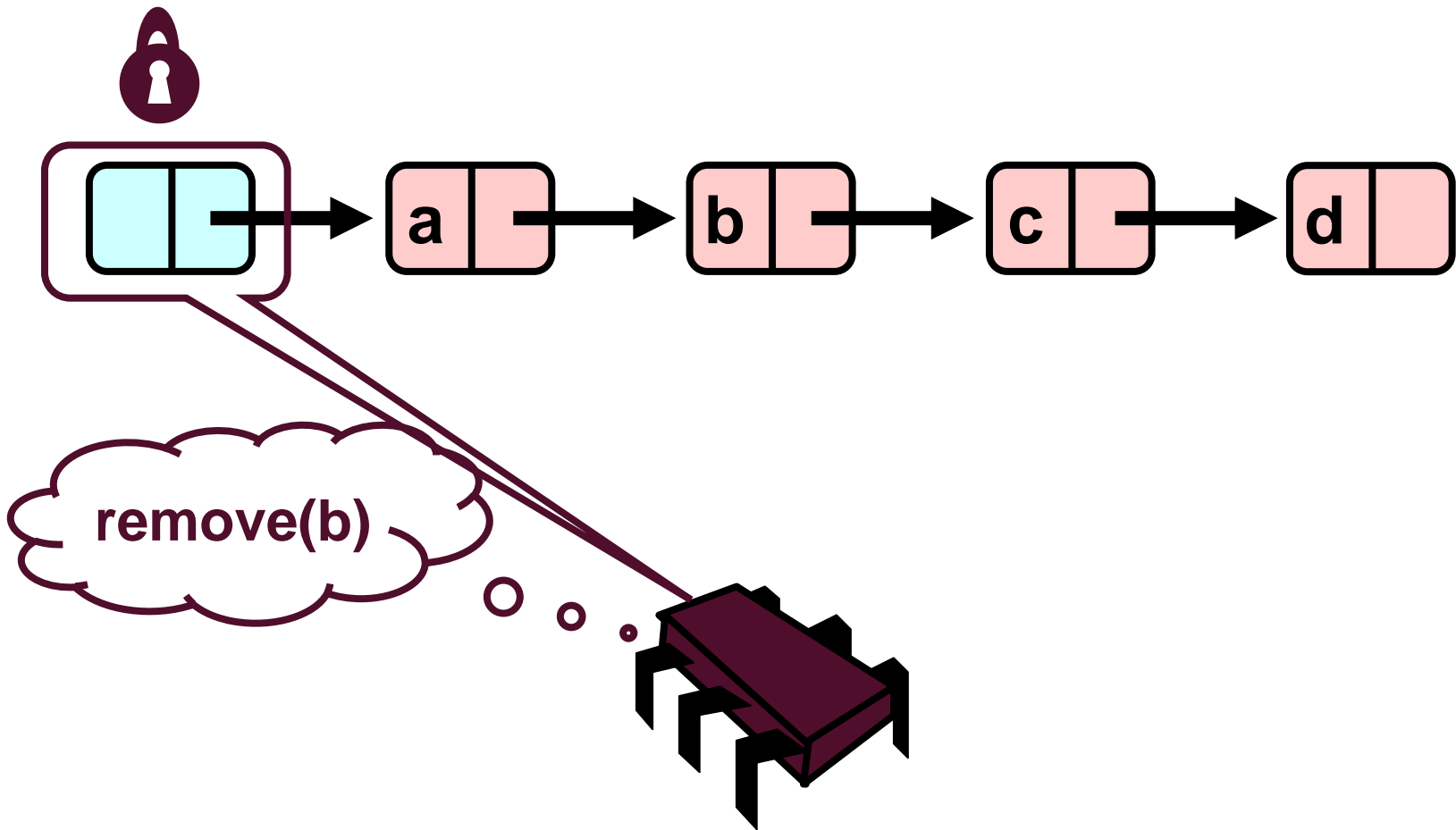
# Hand-over-Hand (fine-grained) locking



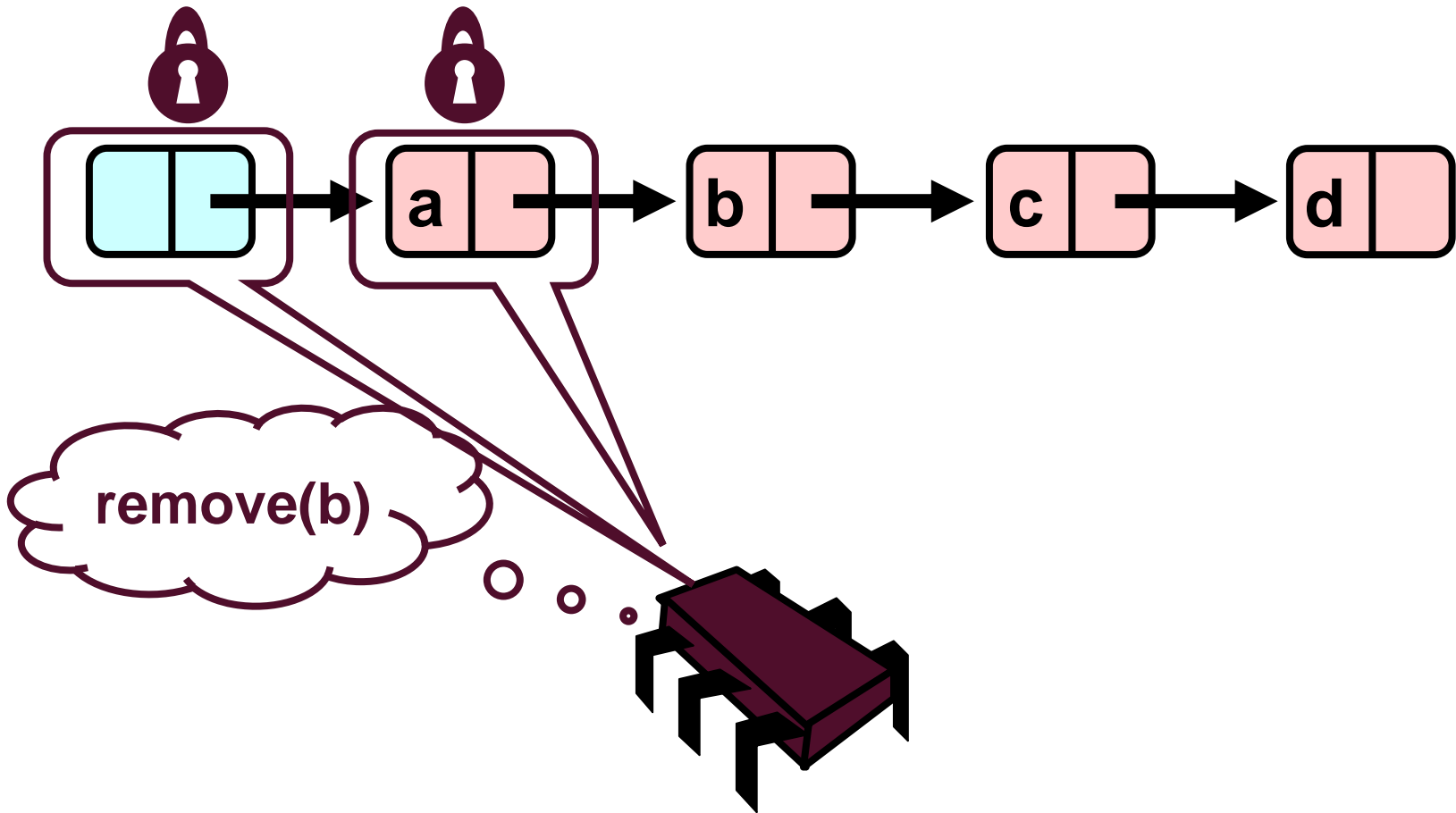
# Removing a Node



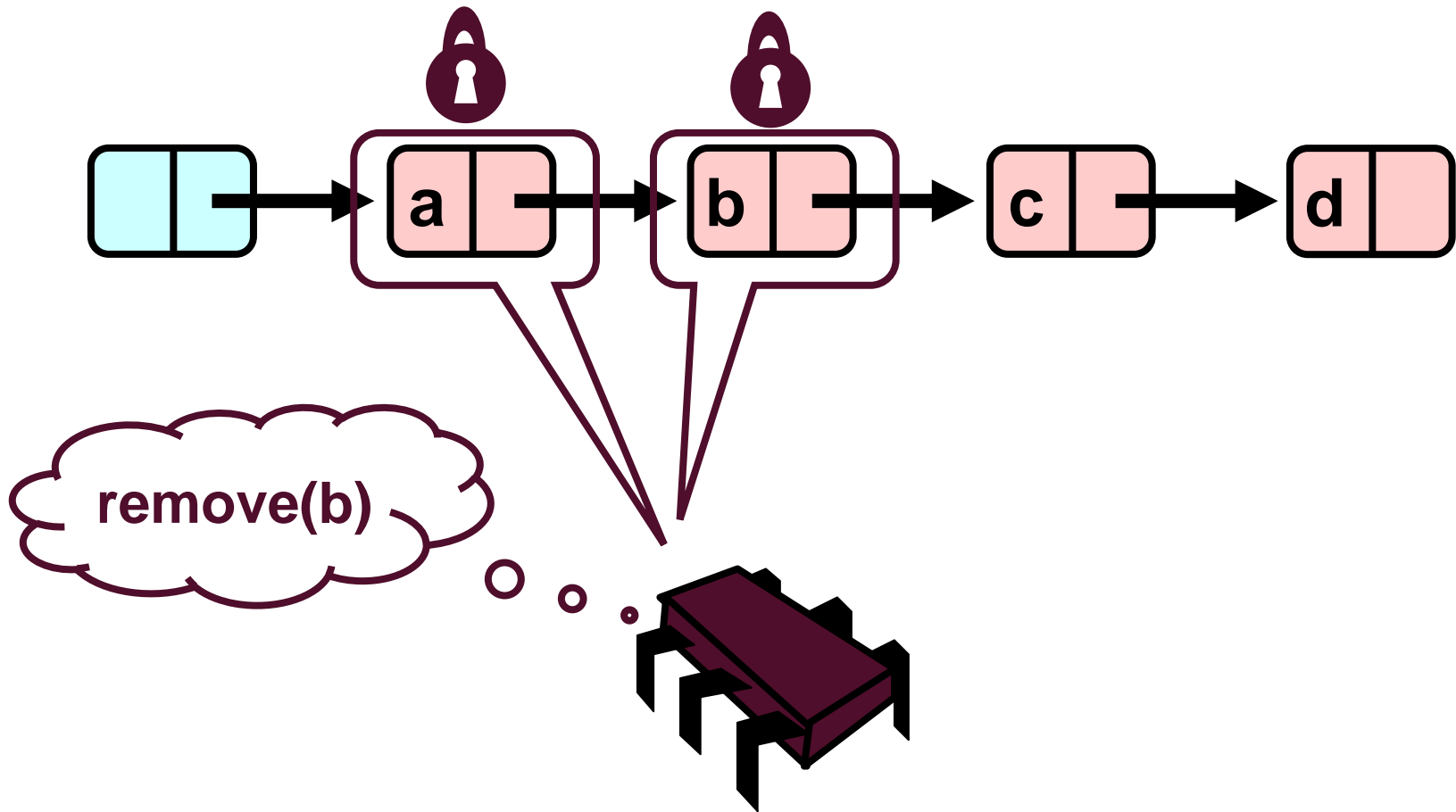
# Removing a Node



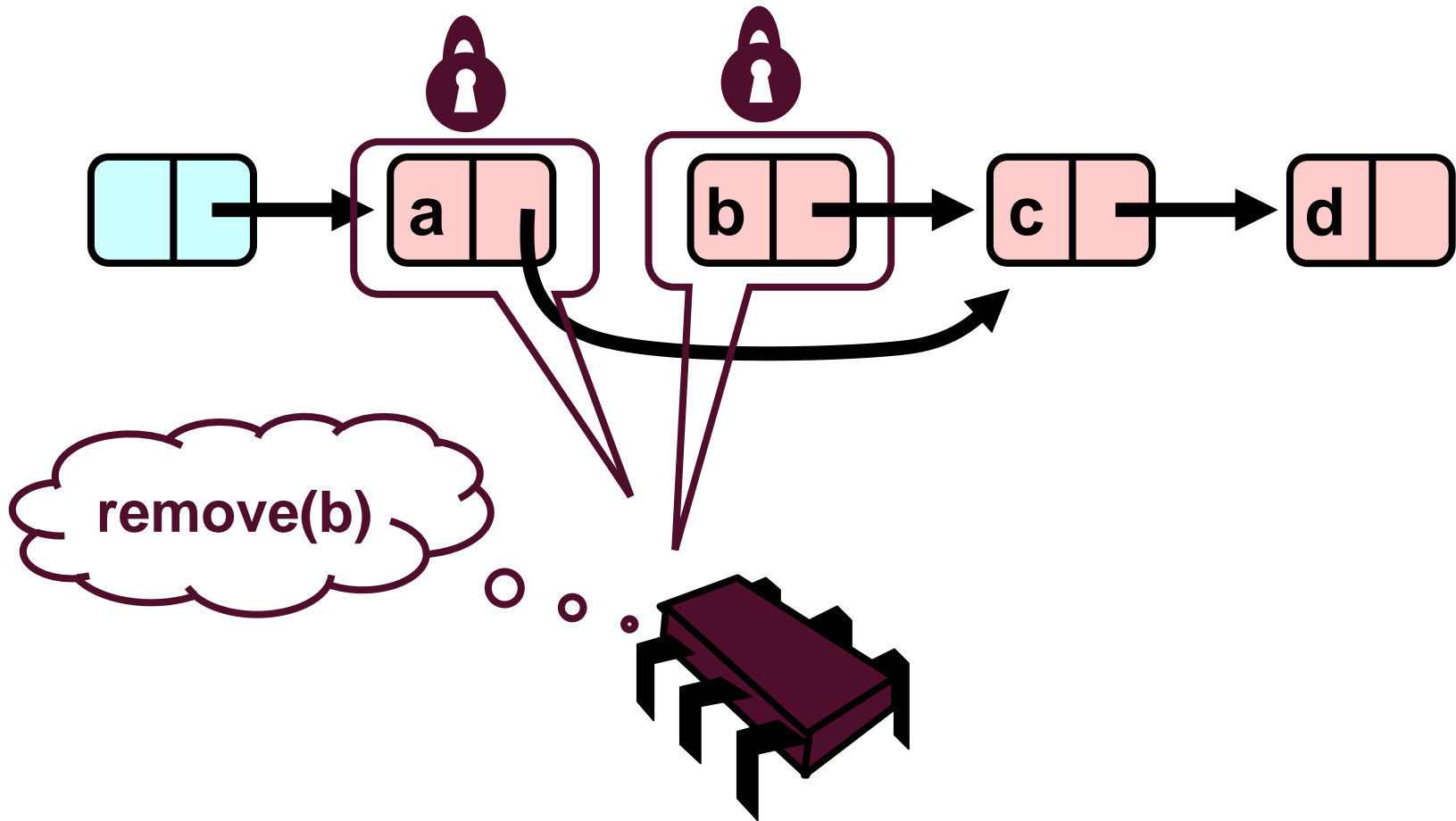
# Removing a Node



# Removing a Node

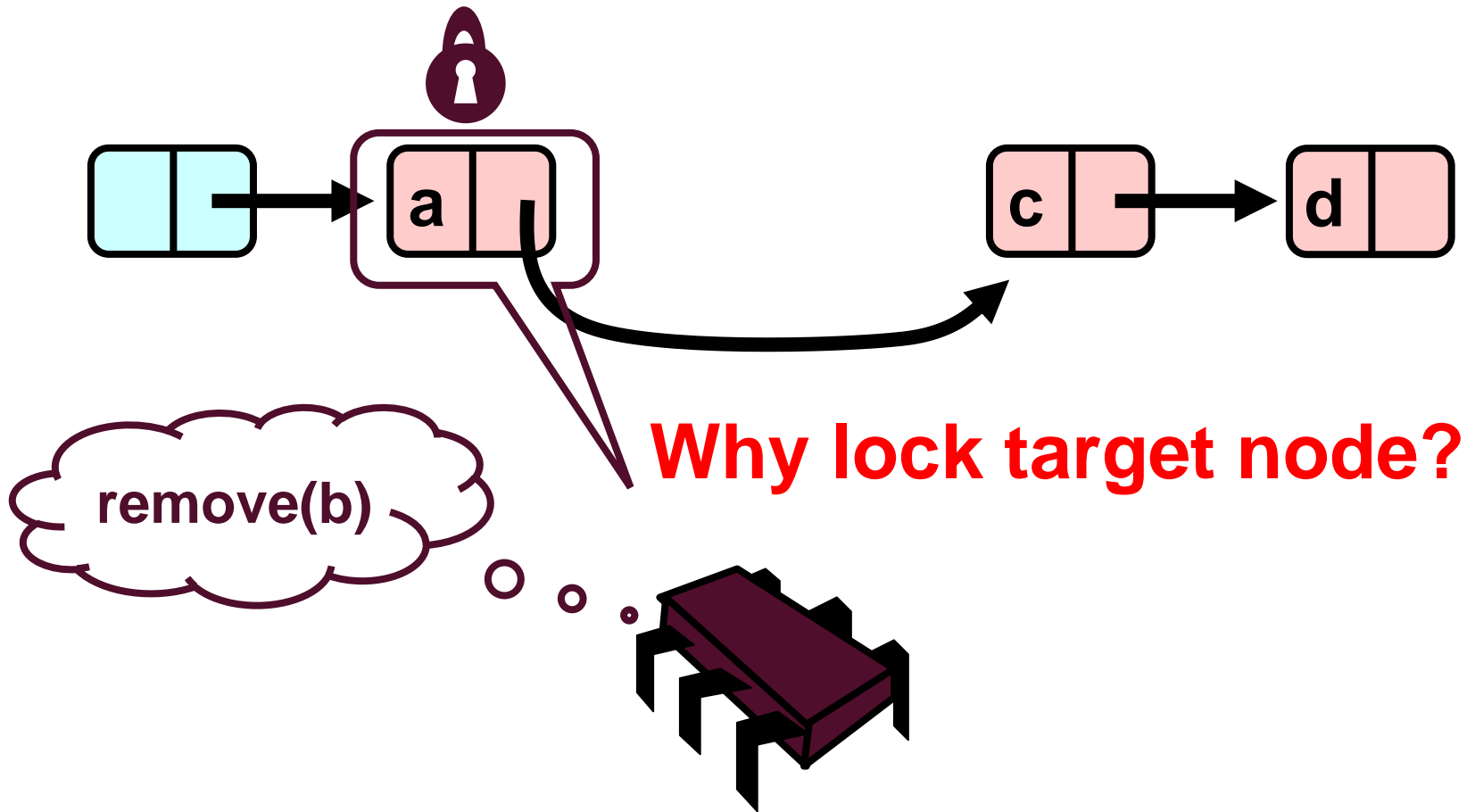


# Removing a Node

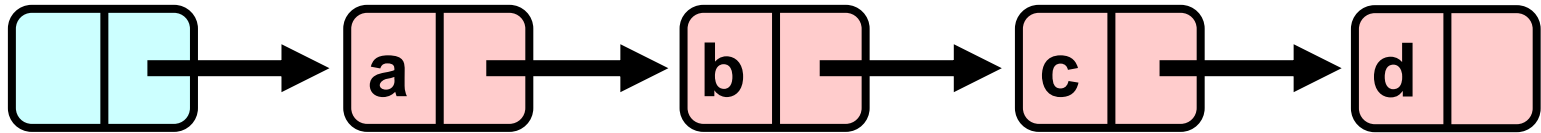




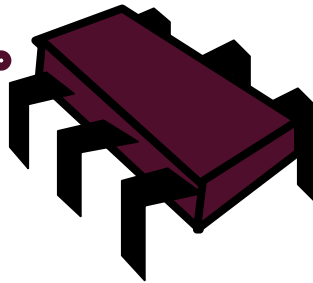
# Removing a Node



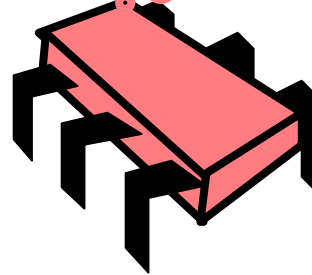
# Concurrent Removes



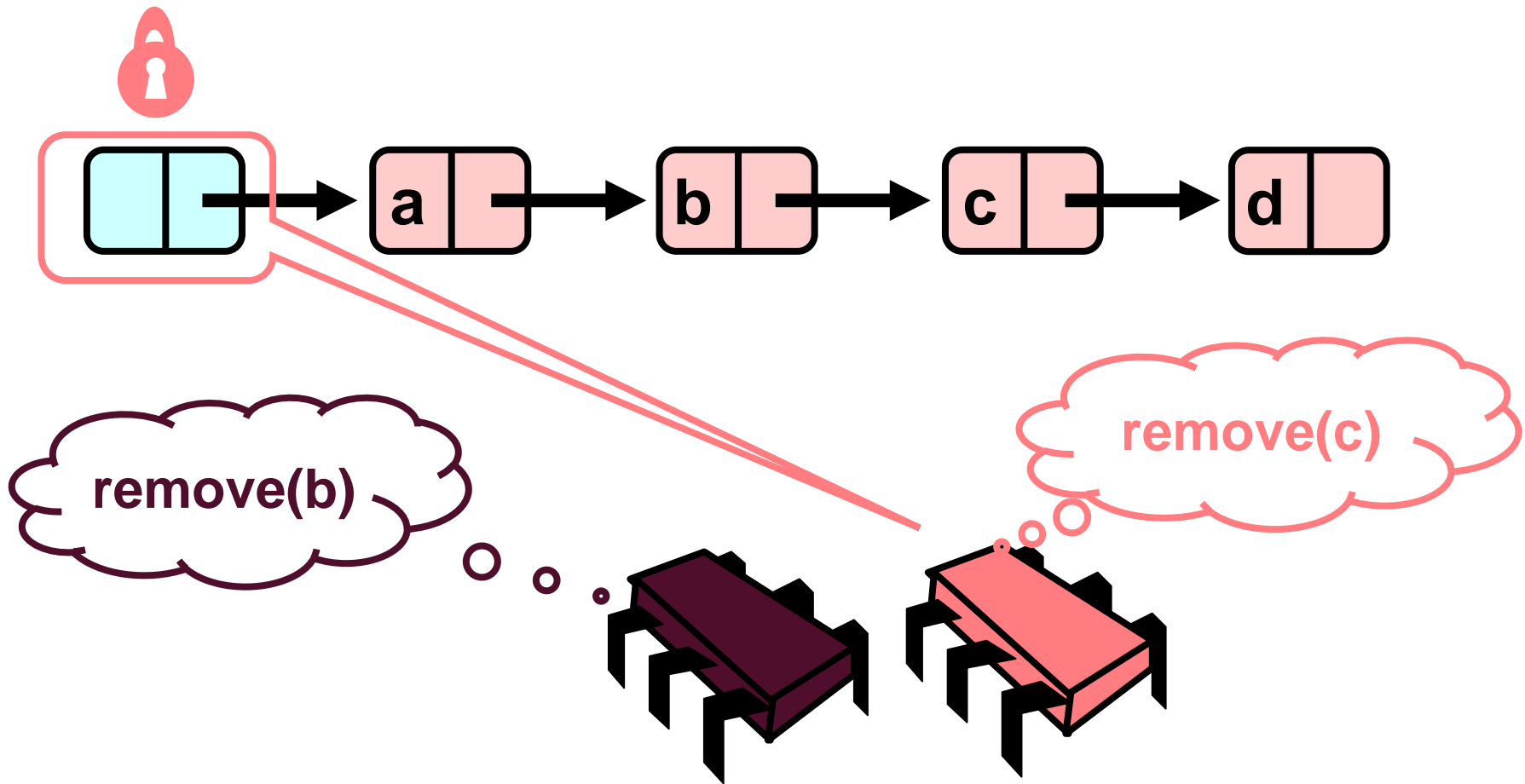
remove(b)



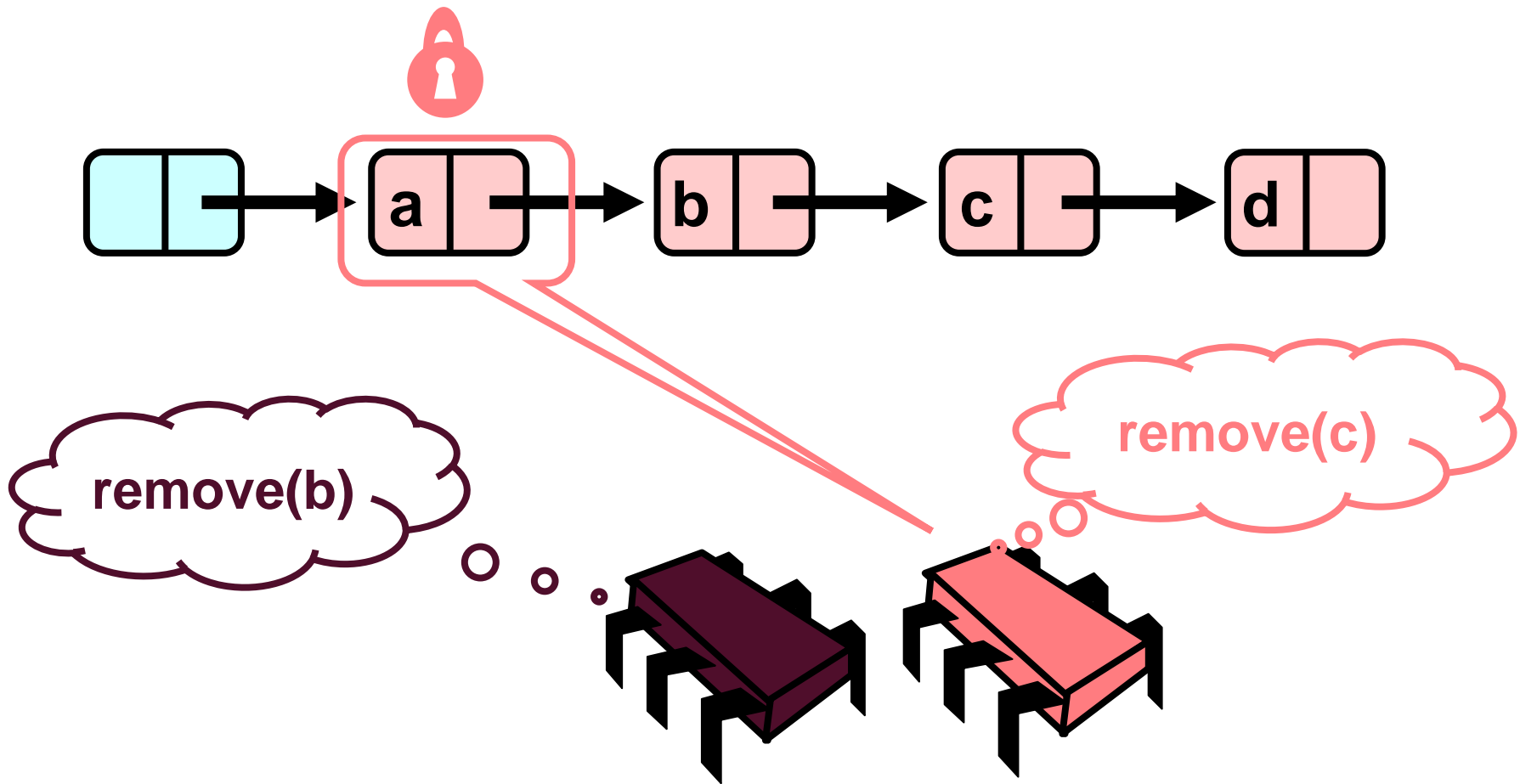
remove(c)



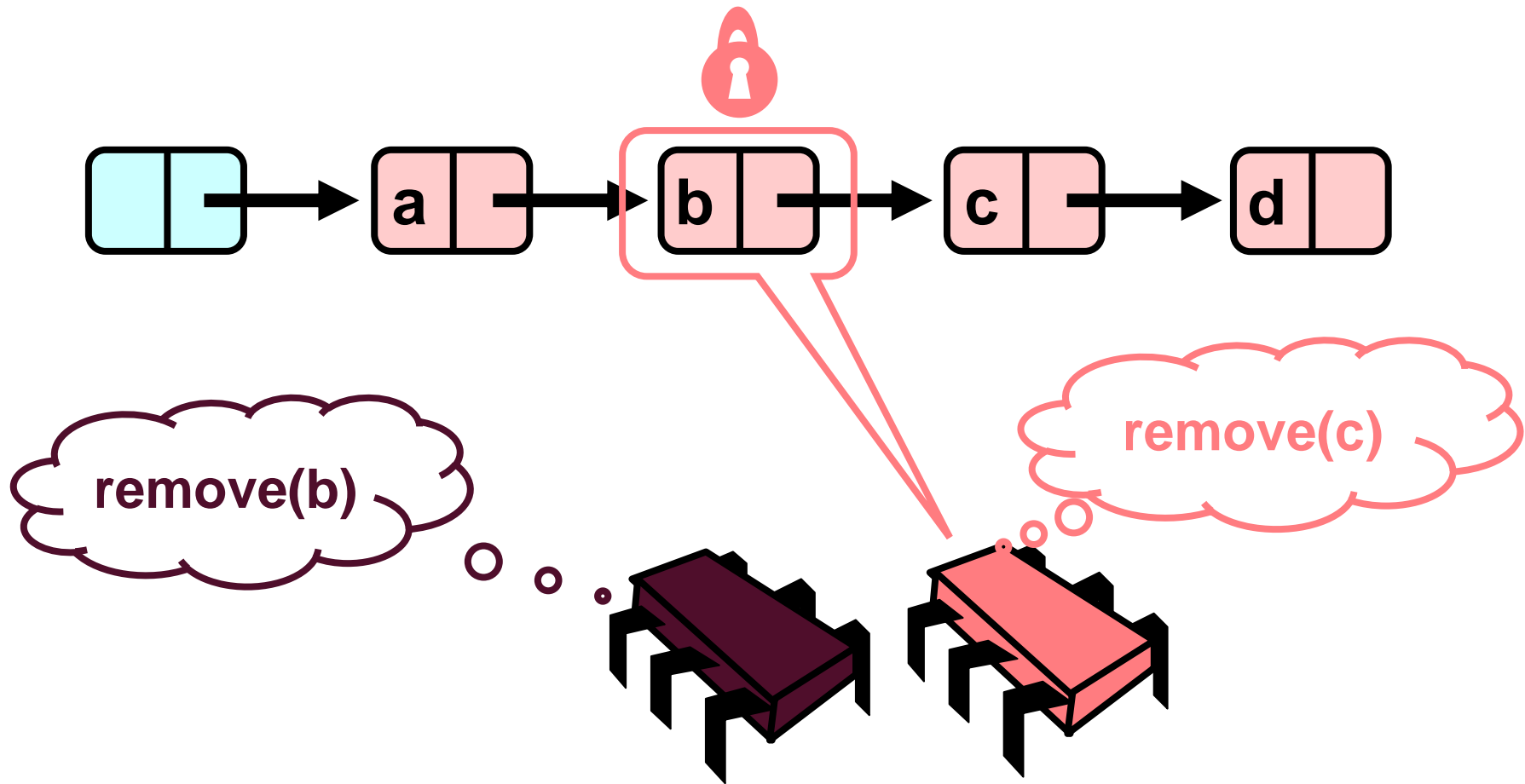
# Concurrent Removes



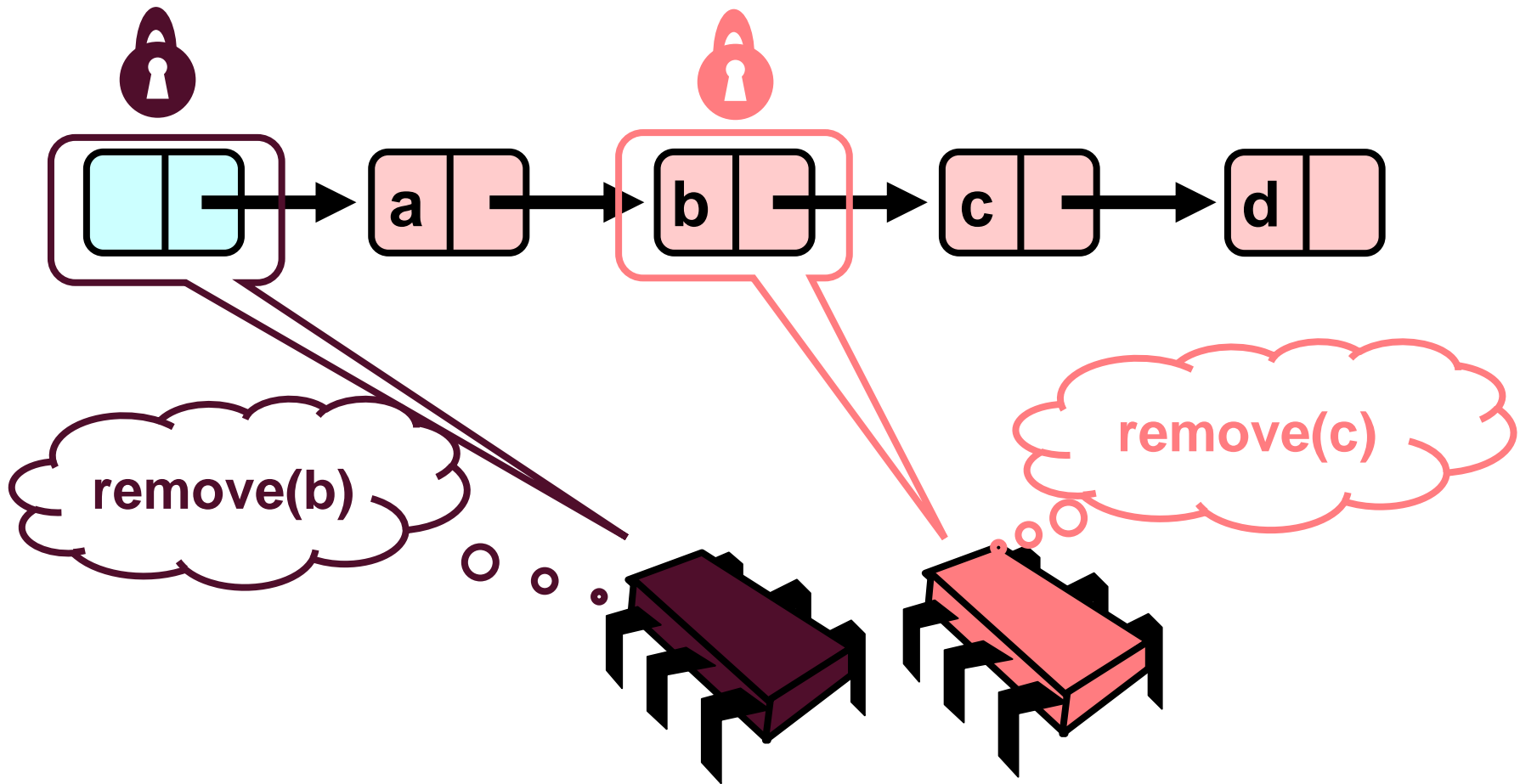
# Concurrent Removes



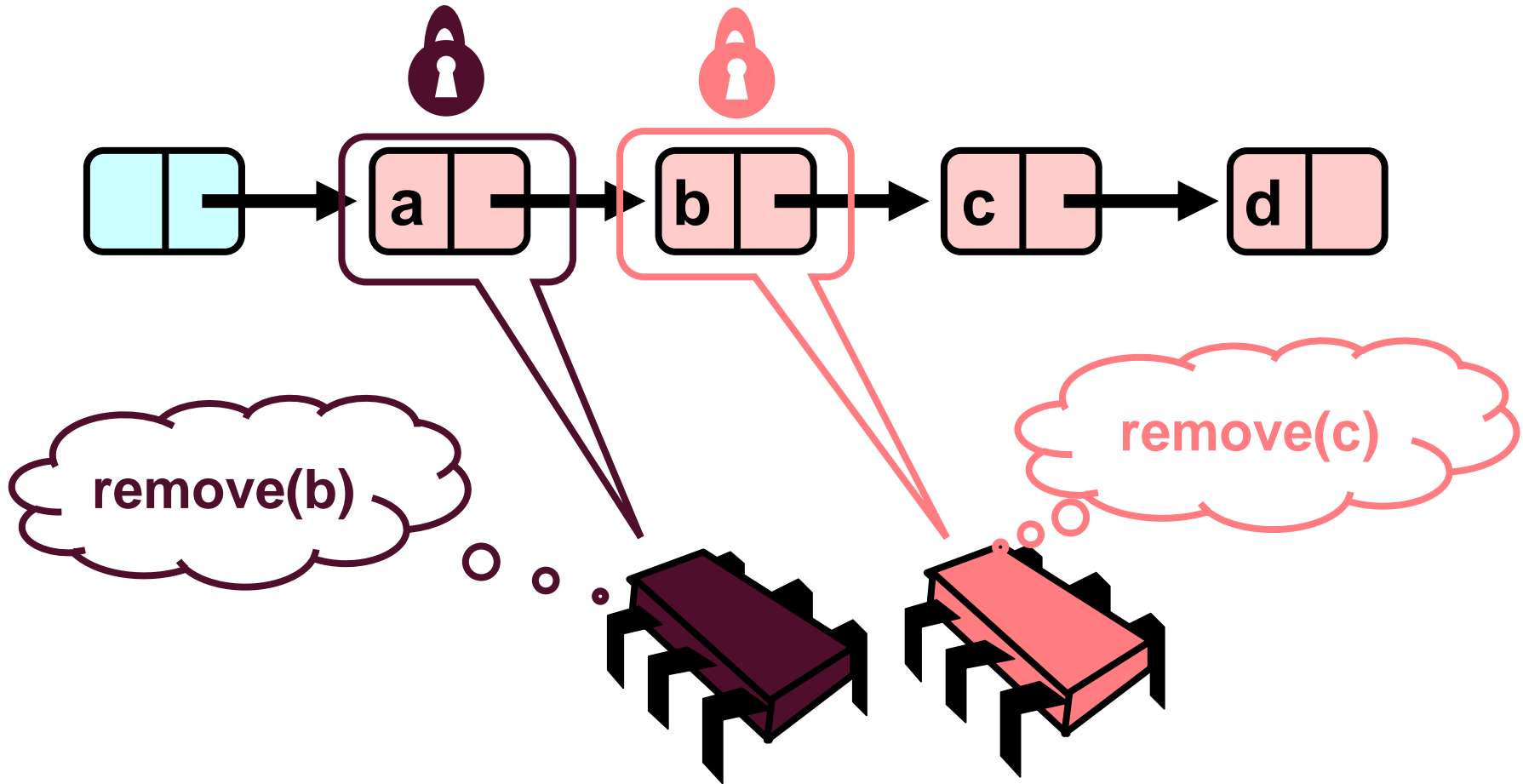
# Concurrent Removes



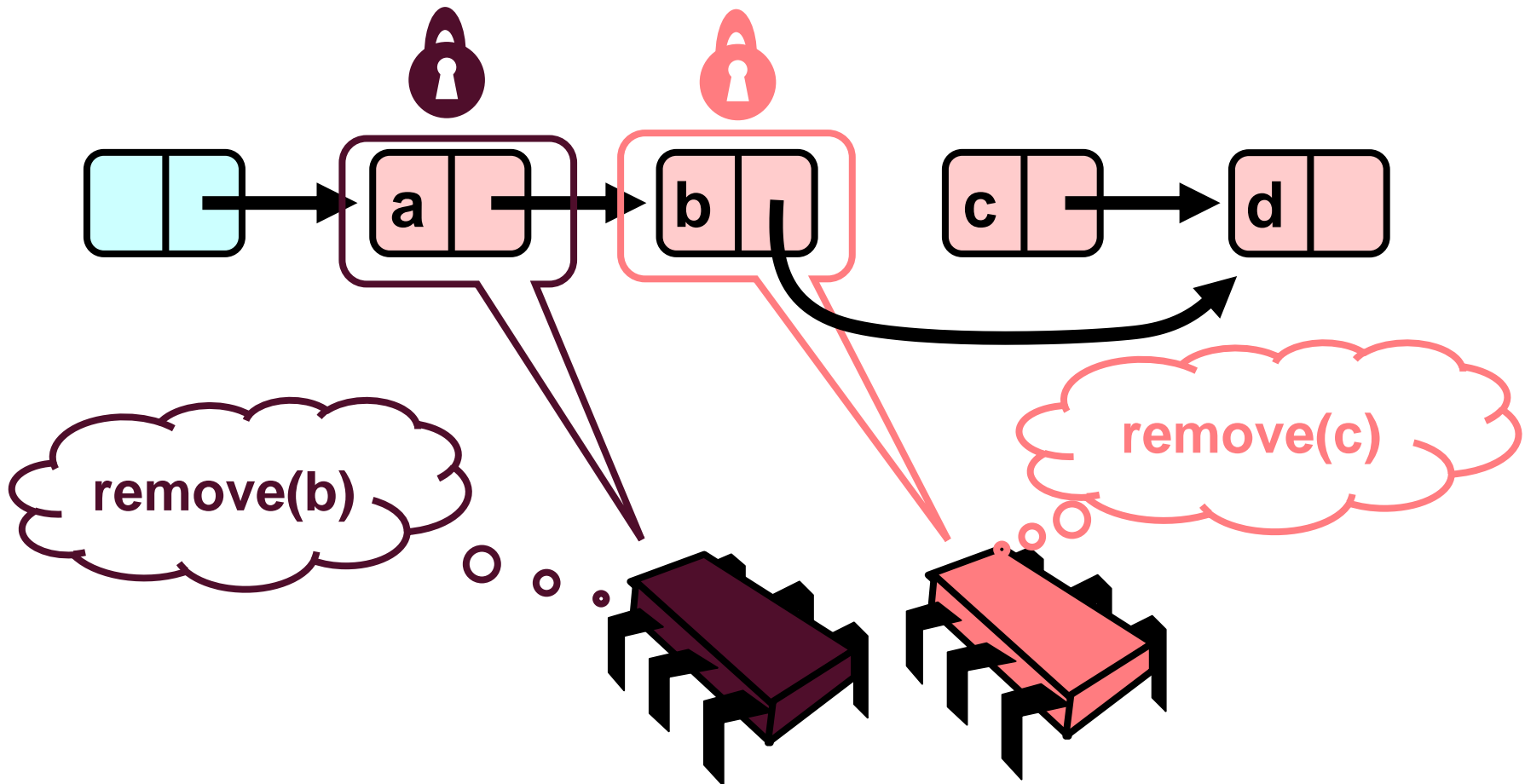
# Concurrent Removes



# Concurrent Removes

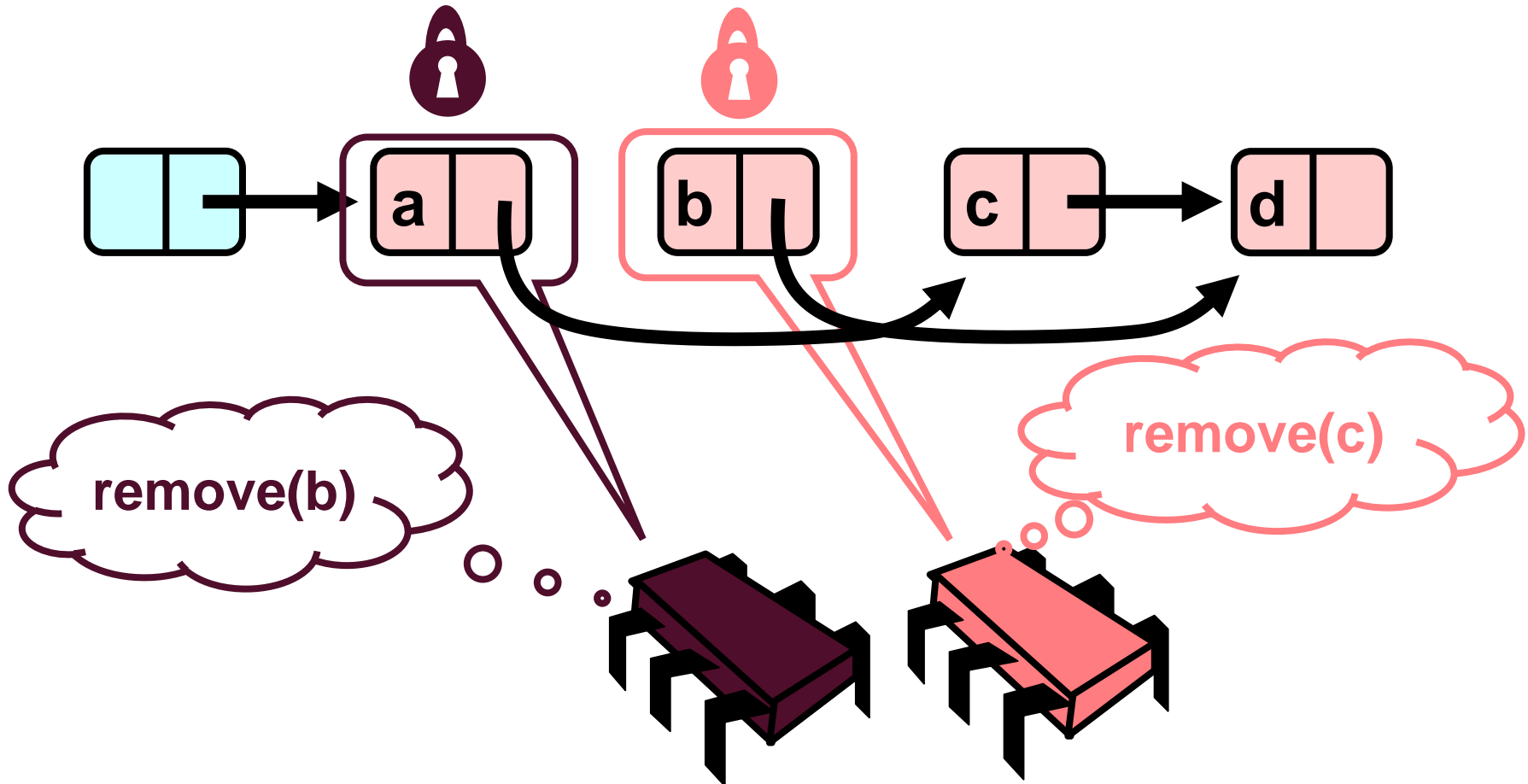


# Concurrent Removes

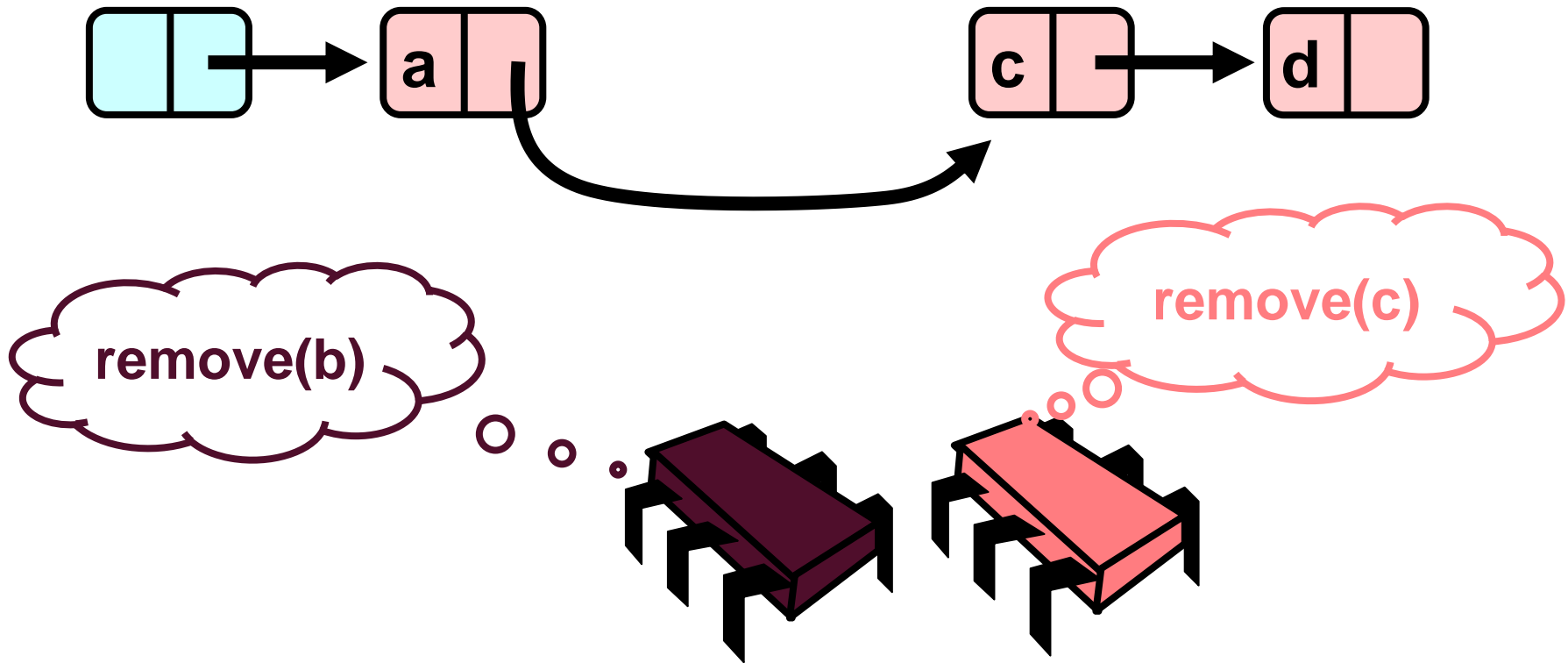




# Concurrent Removes

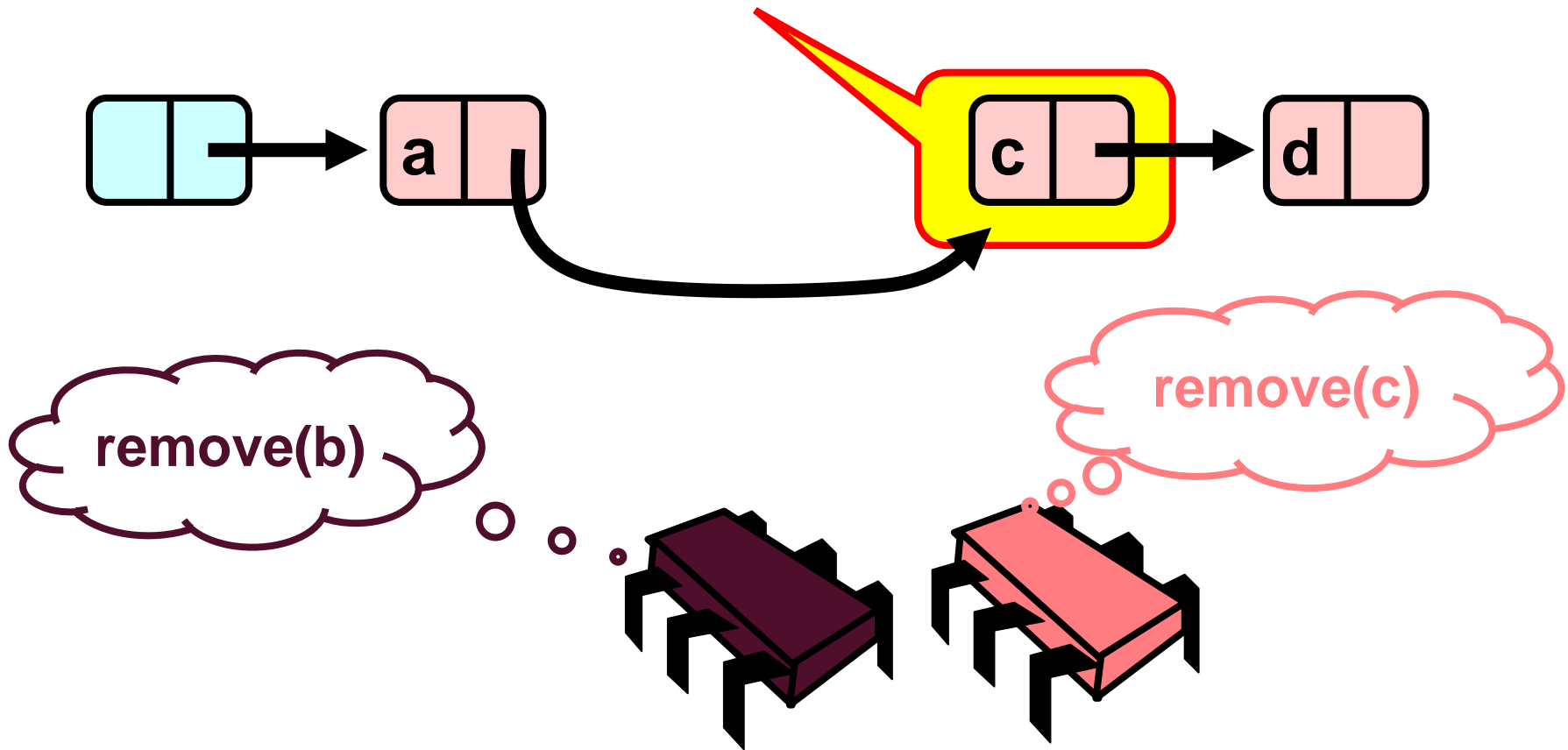


# Uh, Oh



# Uh, Oh

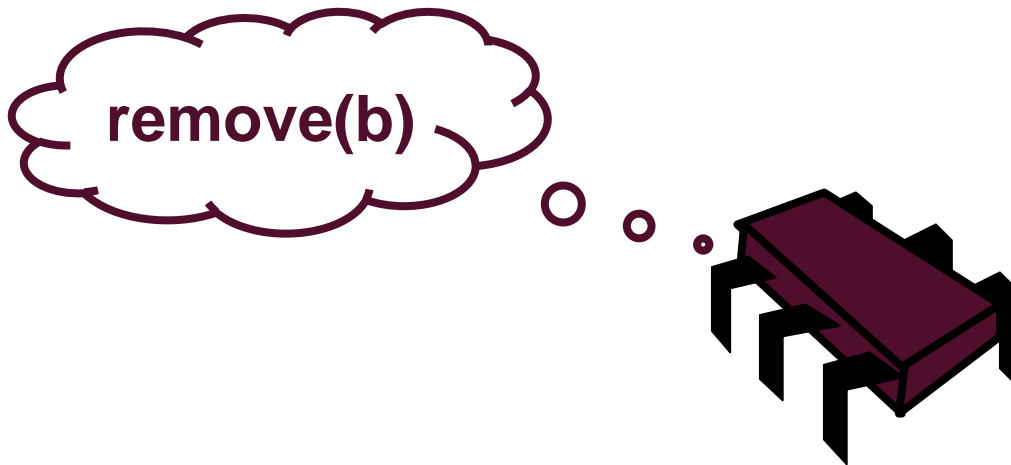
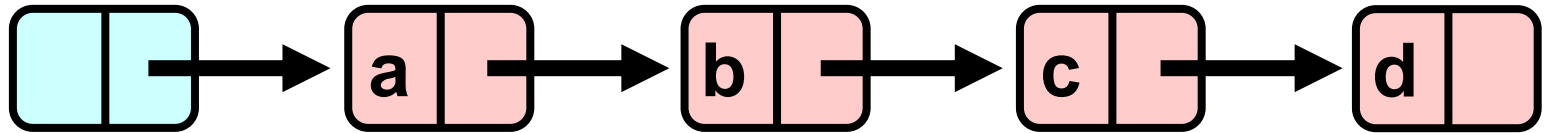
Bad news, **c** not removed



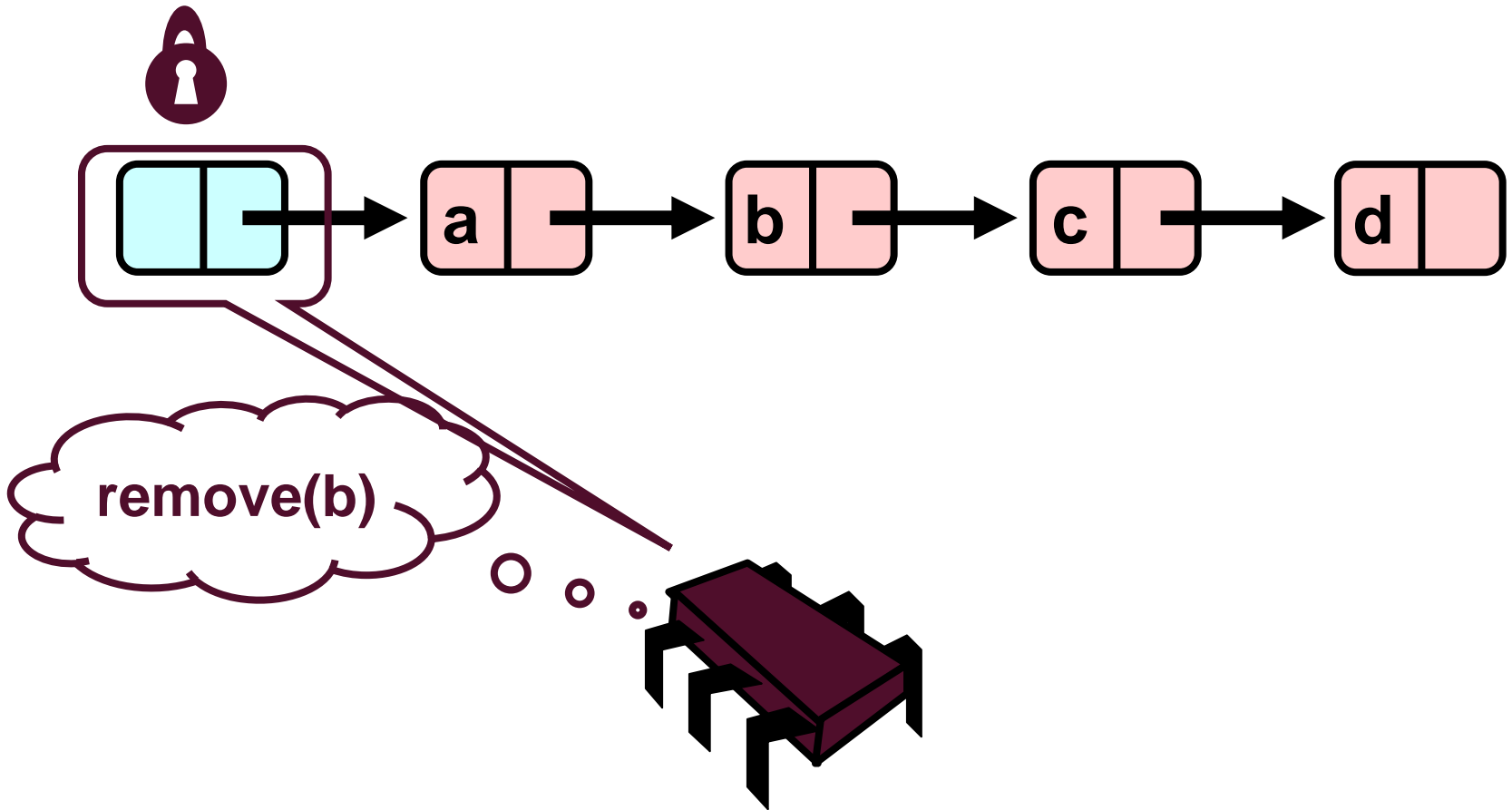
# Insight

- **If a node x is locked**
  - Successor of x cannot be deleted!
- **Thus, safe locking is**
  - Lock node to be deleted
  - And its predecessor!
  - → hand-over-hand locking

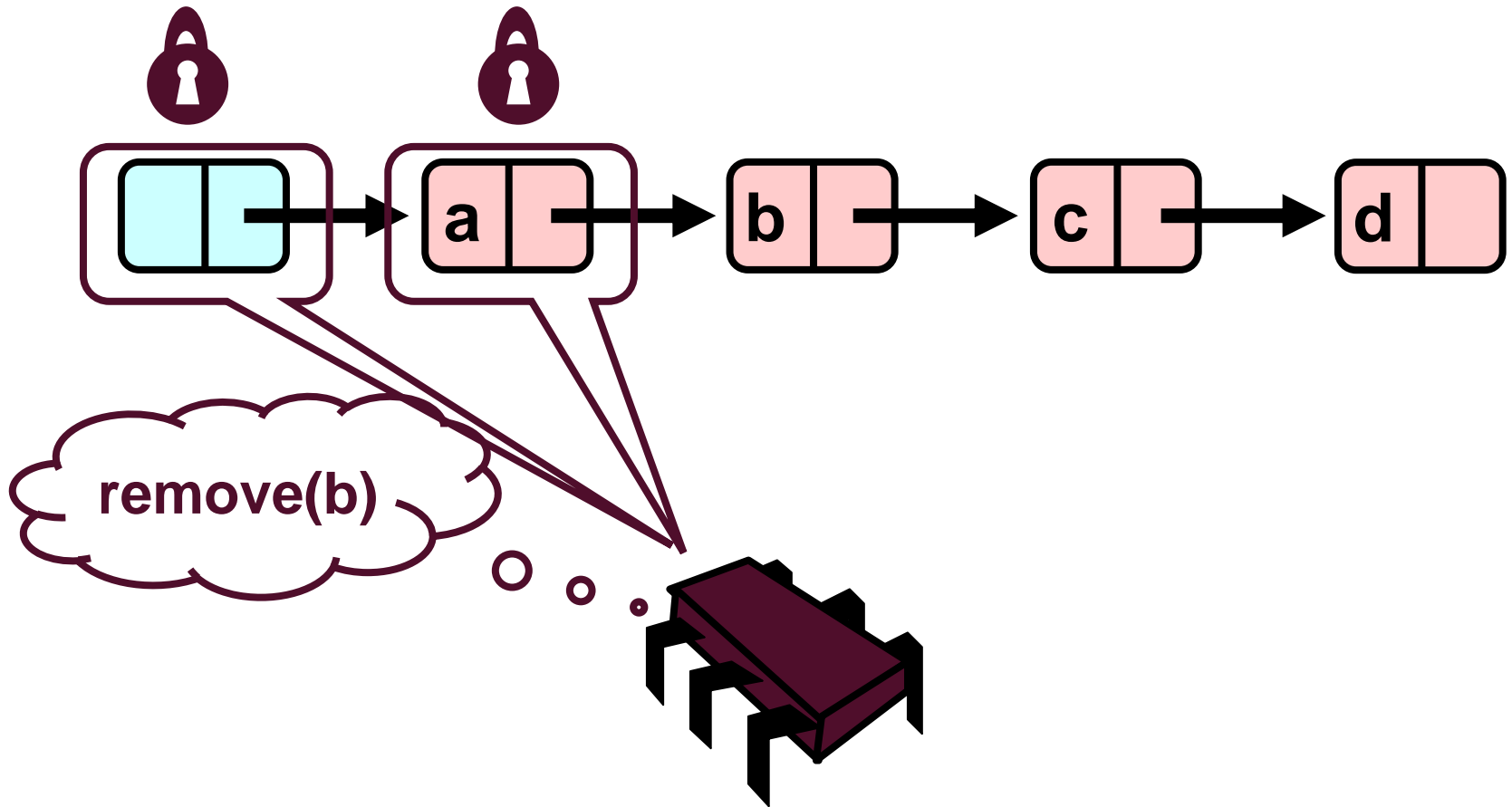
# Hand-Over-Hand Again



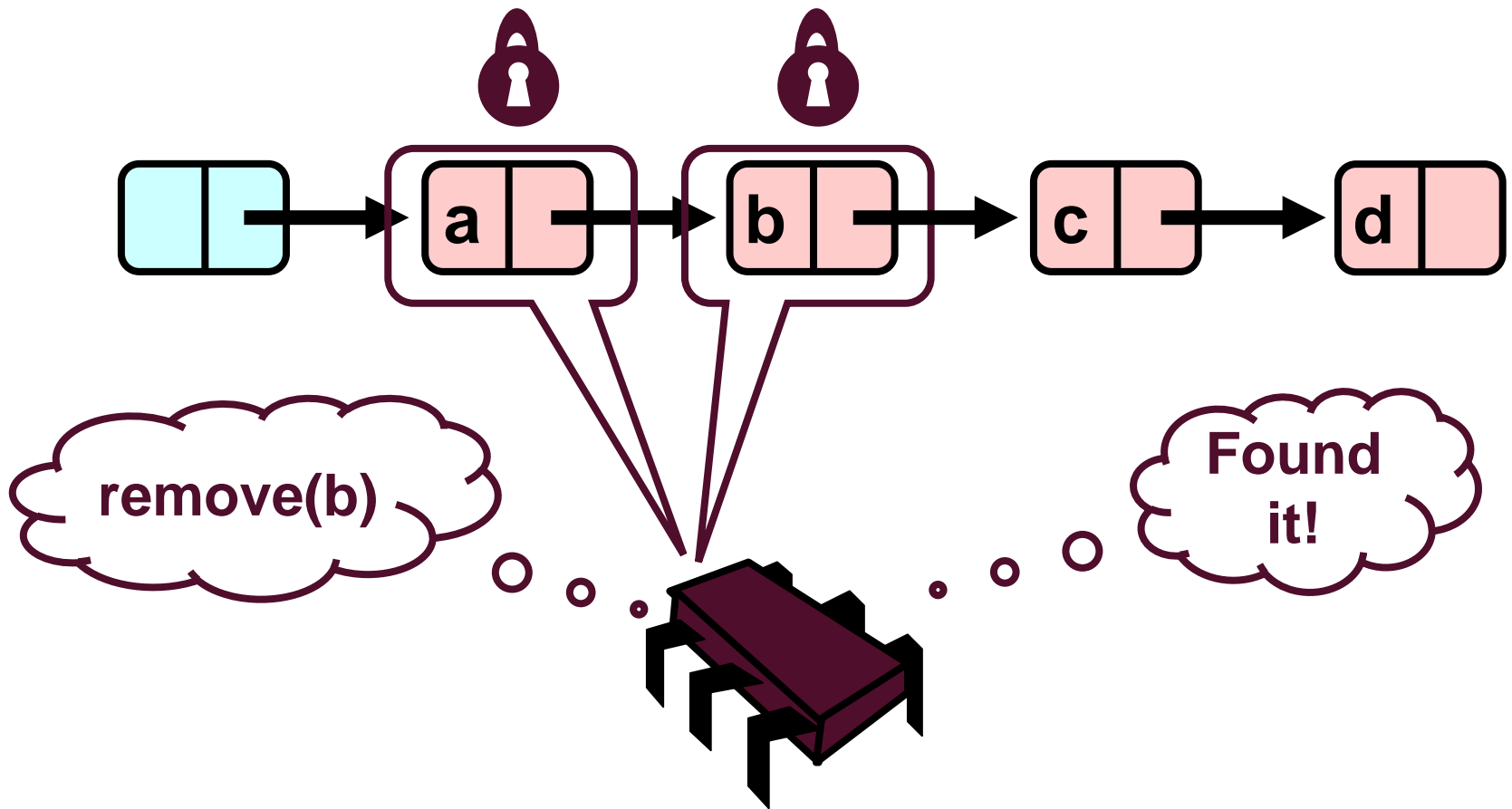
# Hand-Over-Hand Again



# Hand-Over-Hand Again

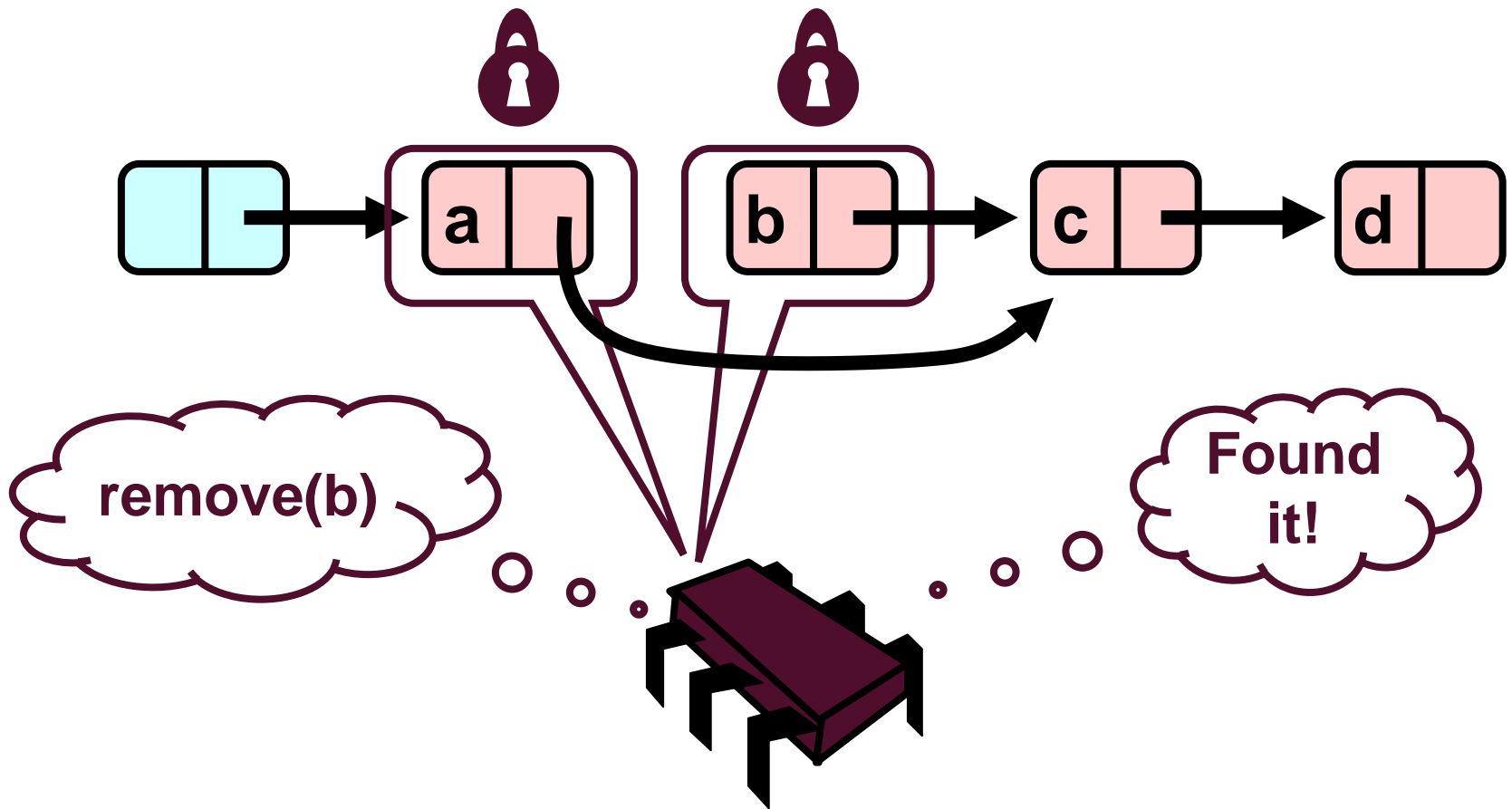


# Hand-Over-Hand Again

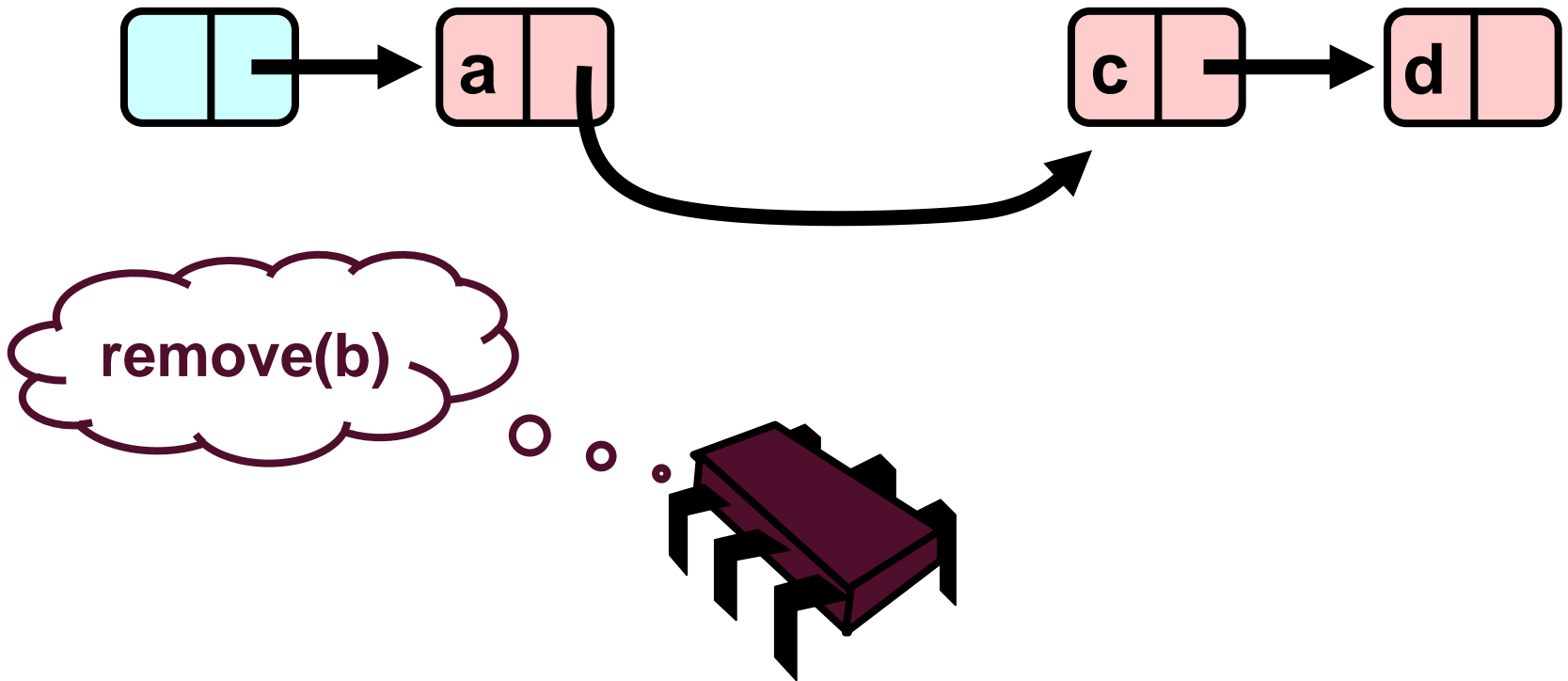




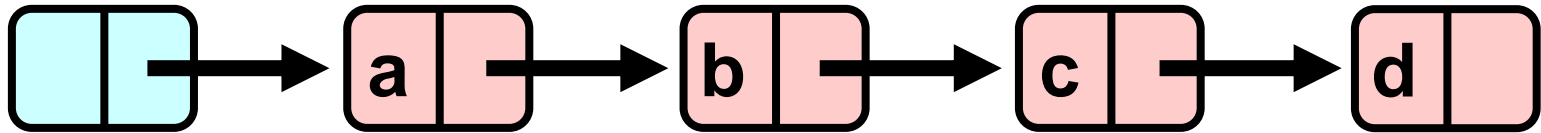
# Hand-Over-Hand Again



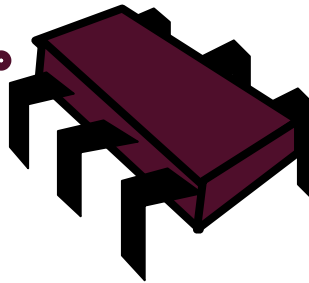
# Hand-Over-Hand Again



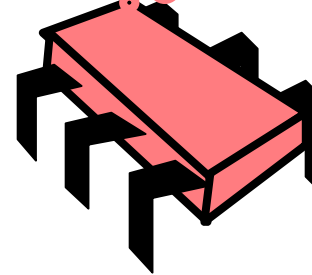
# Removing a Node



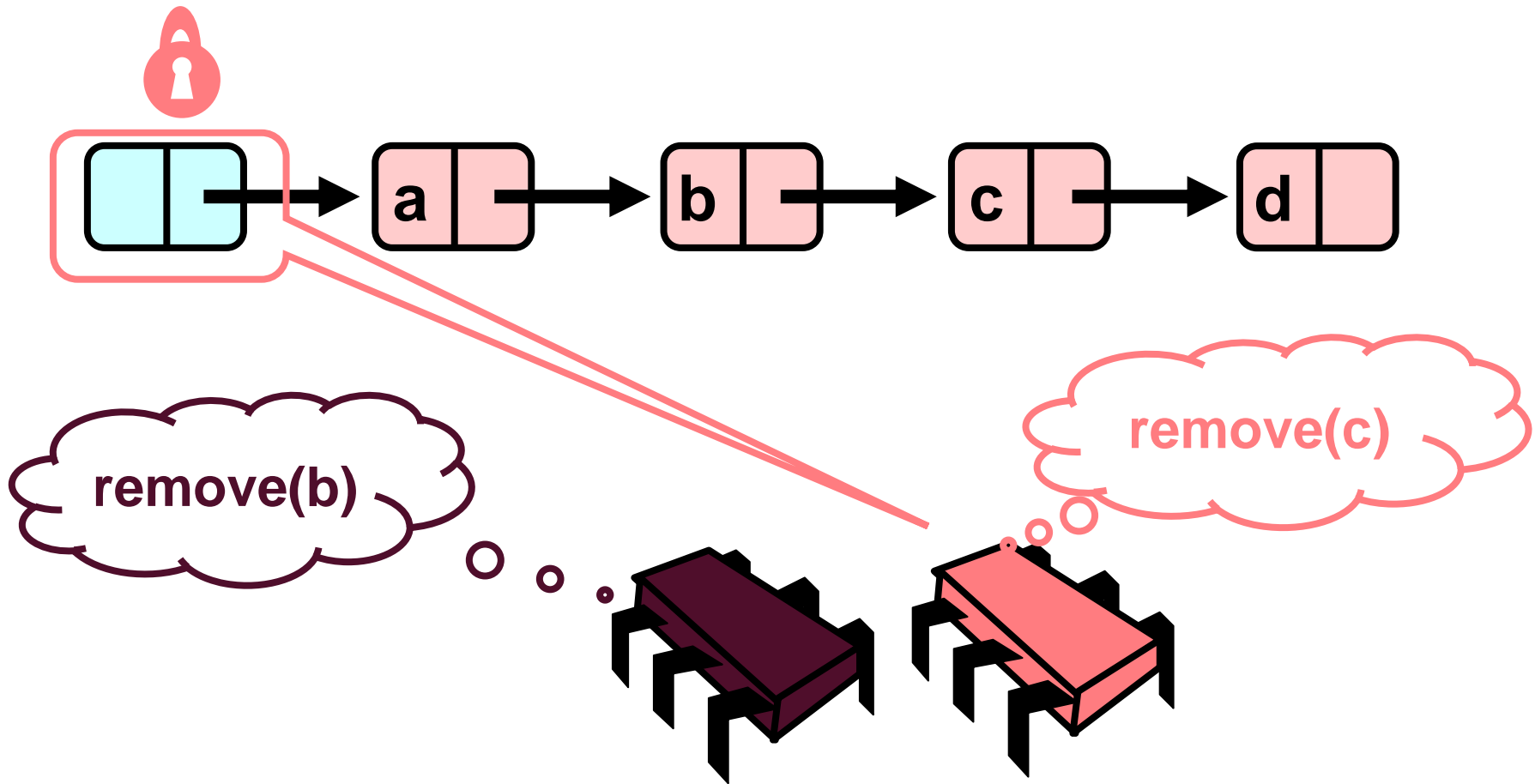
remove(b)



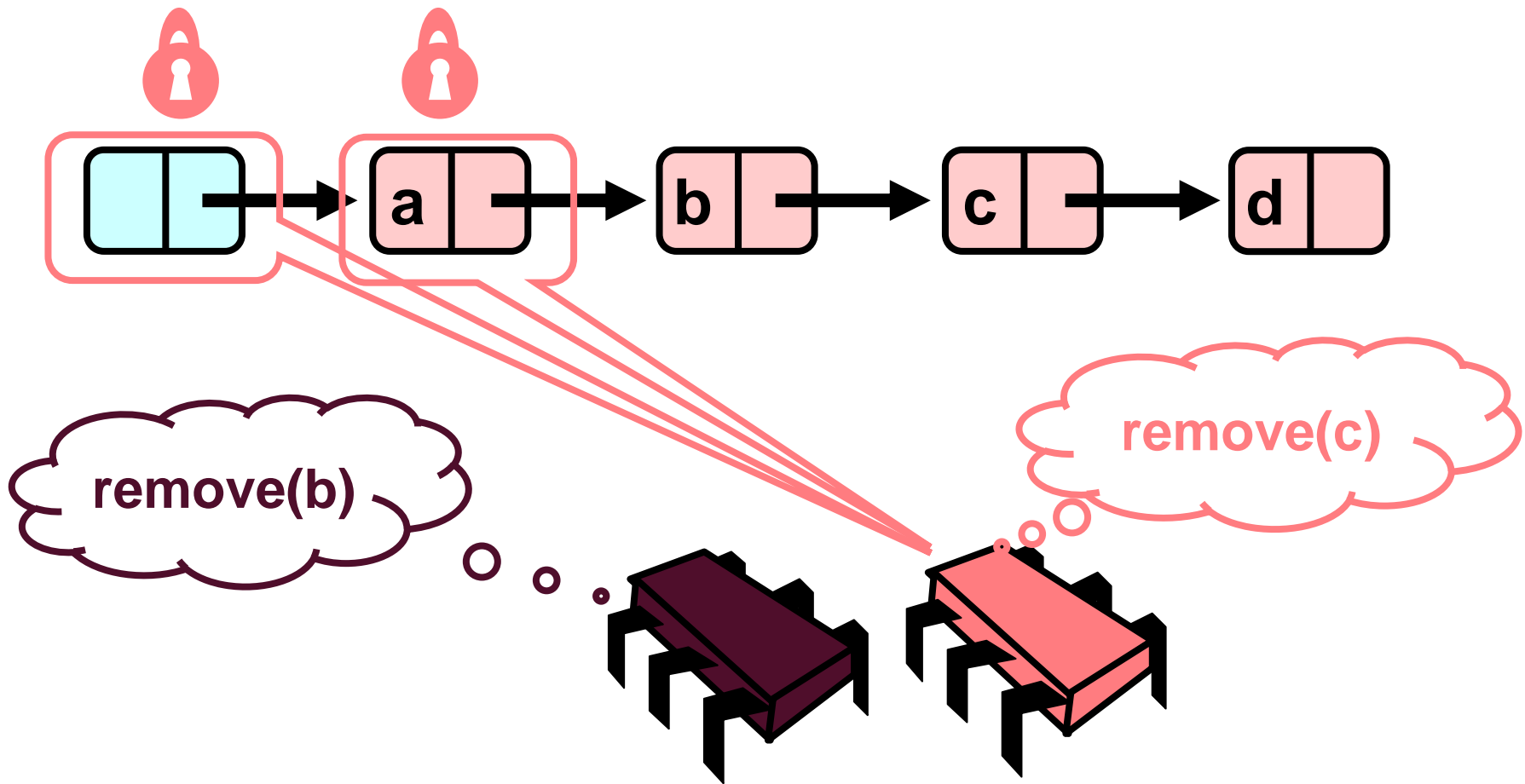
remove(c)



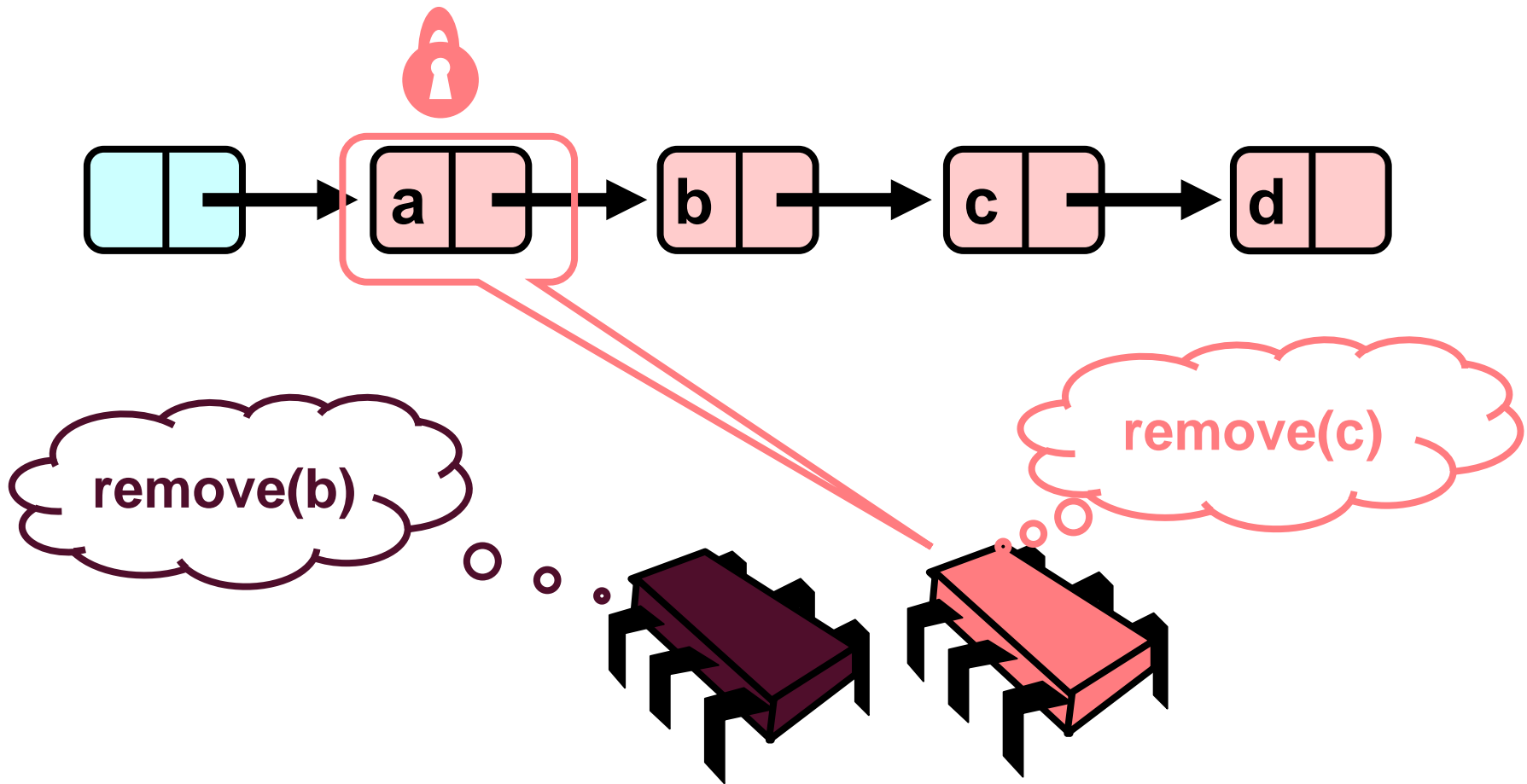
# Removing a Node



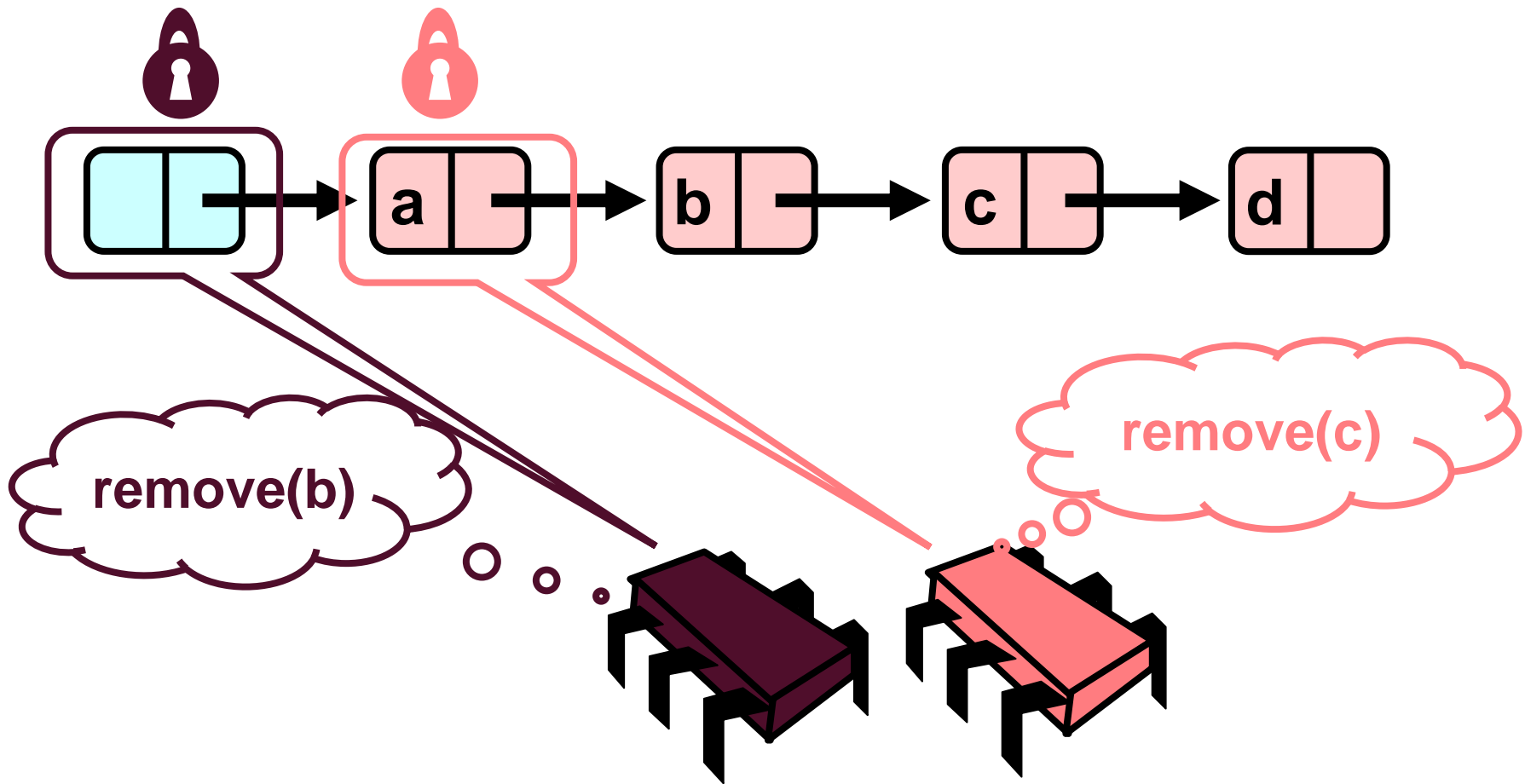
# Removing a Node



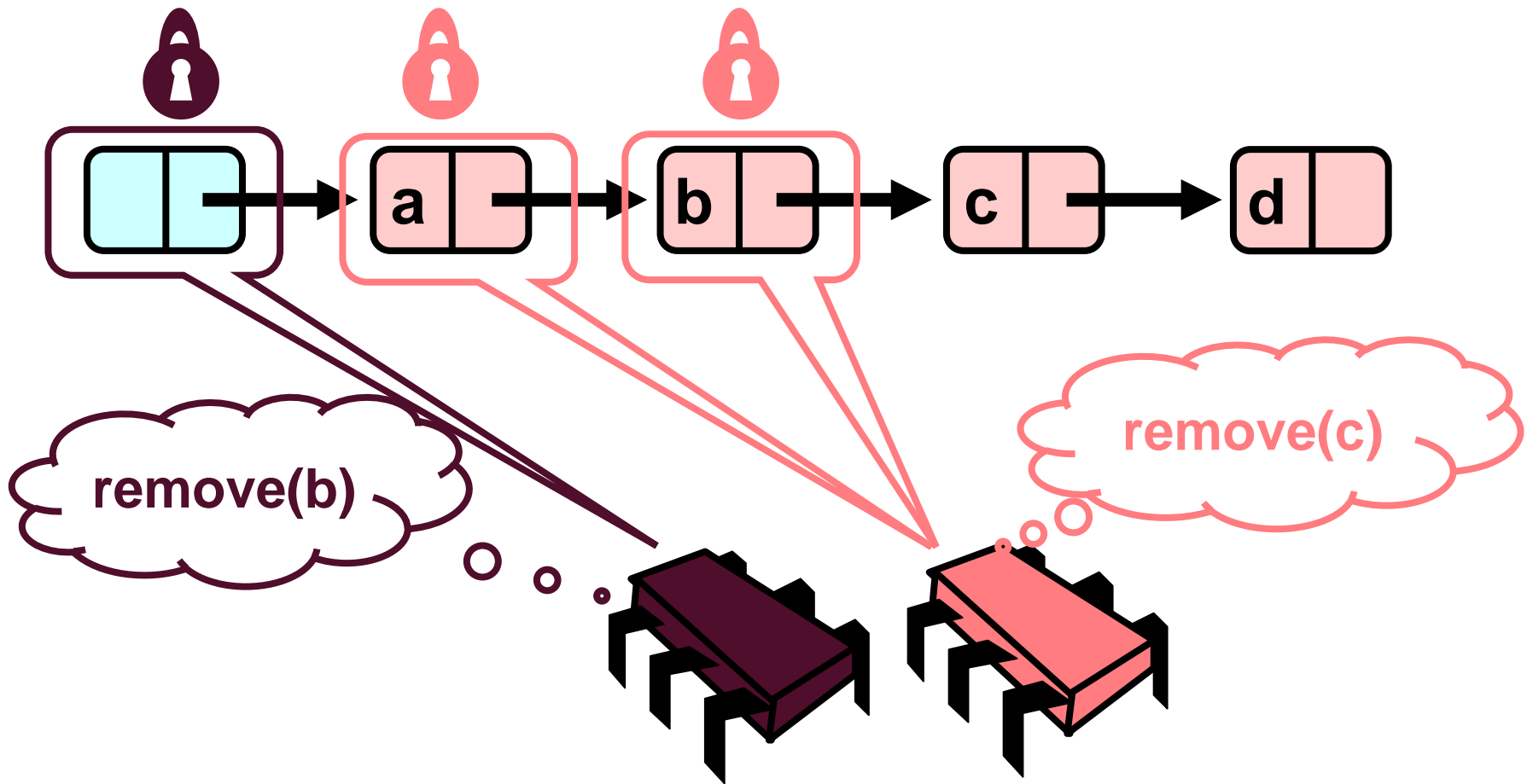
# Removing a Node



# Removing a Node

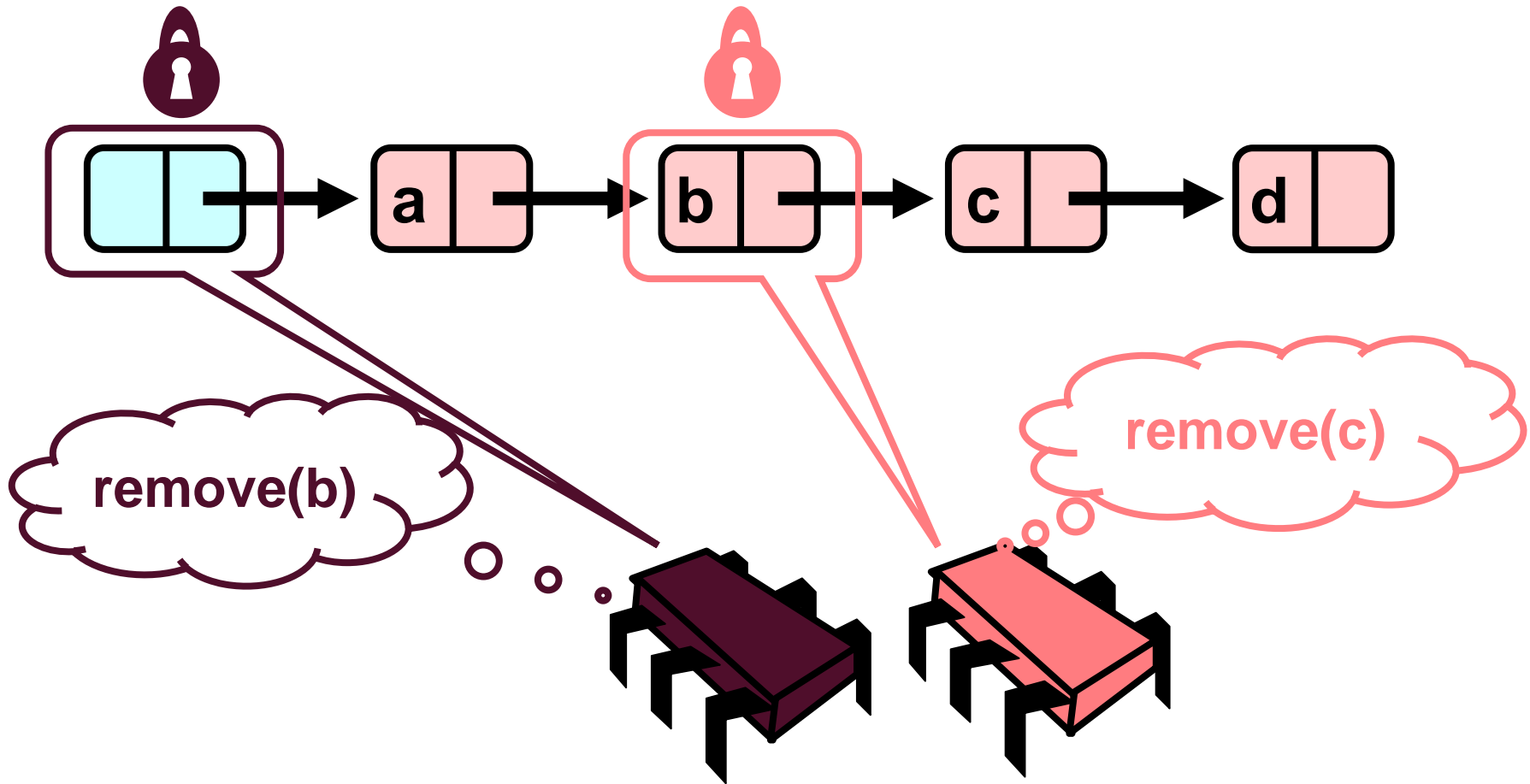


# Removing a Node

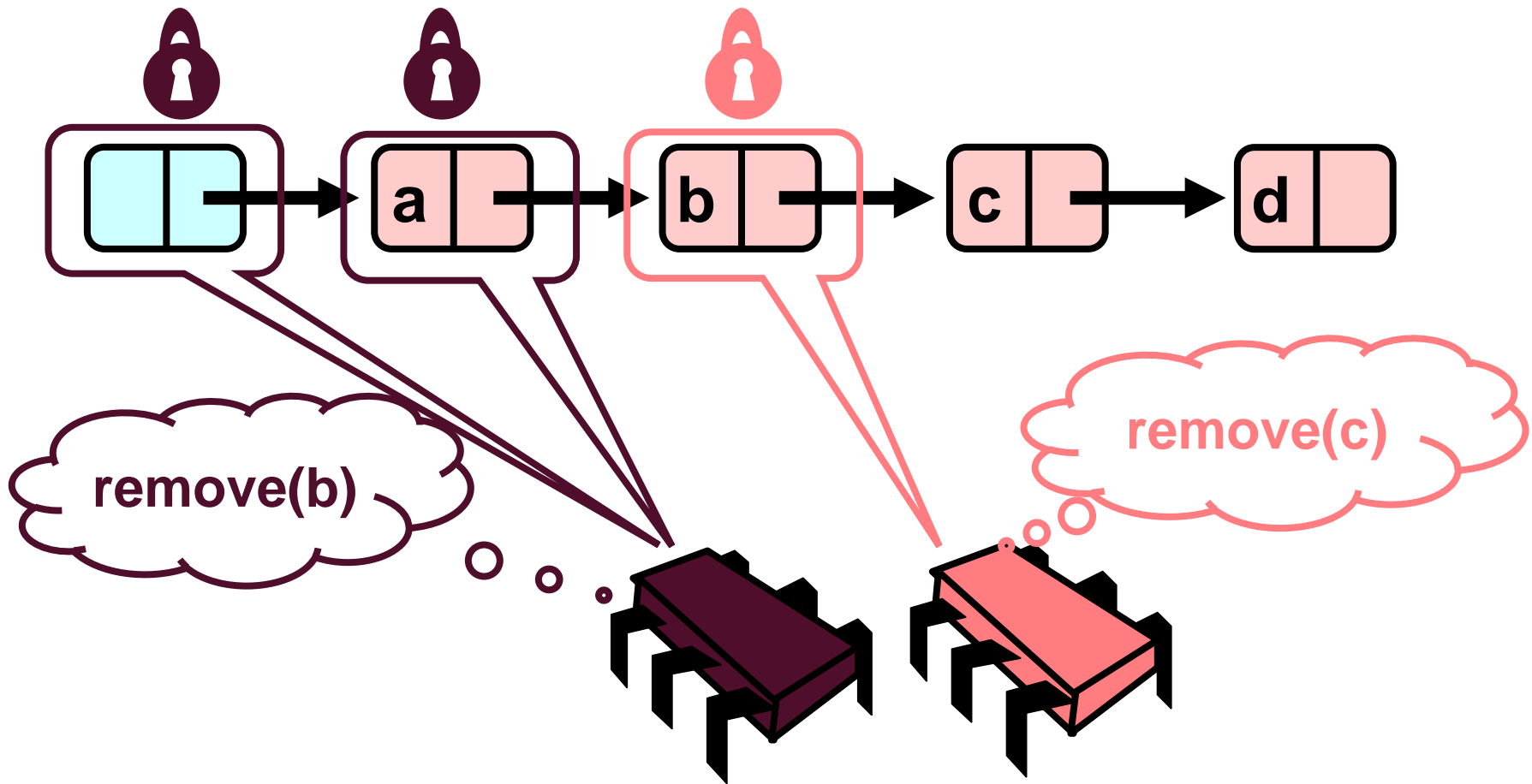




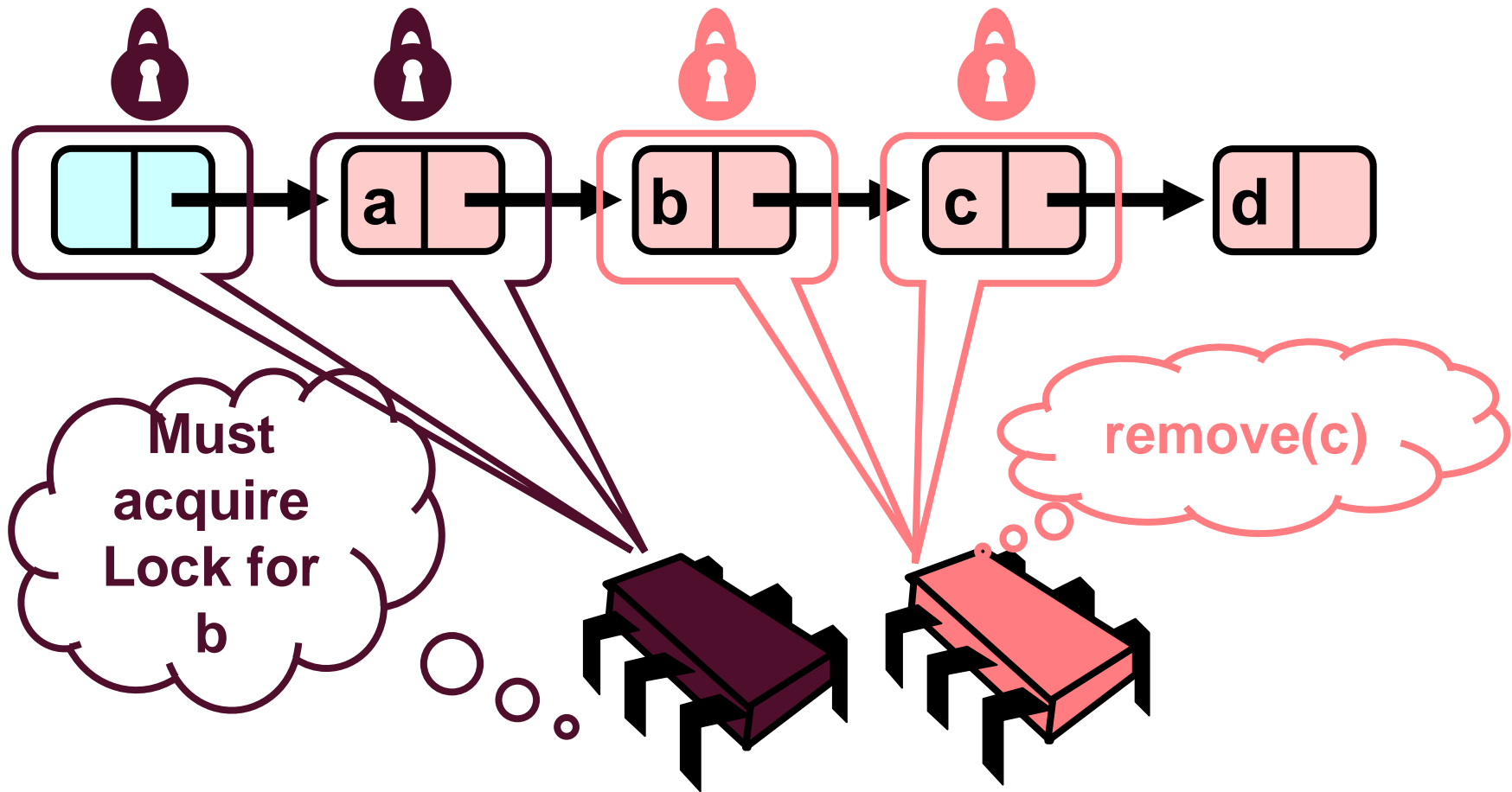
# Removing a Node



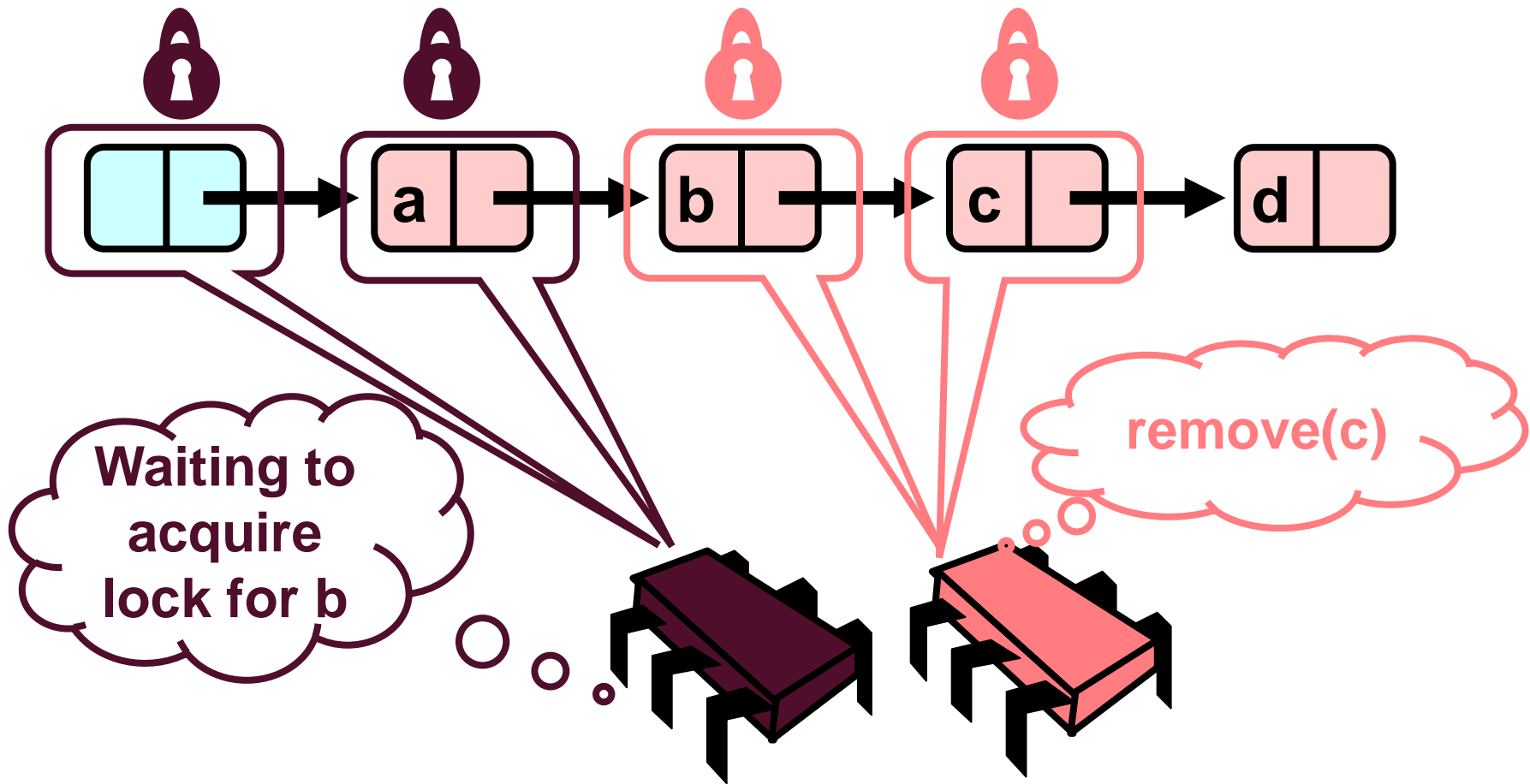
# Removing a Node



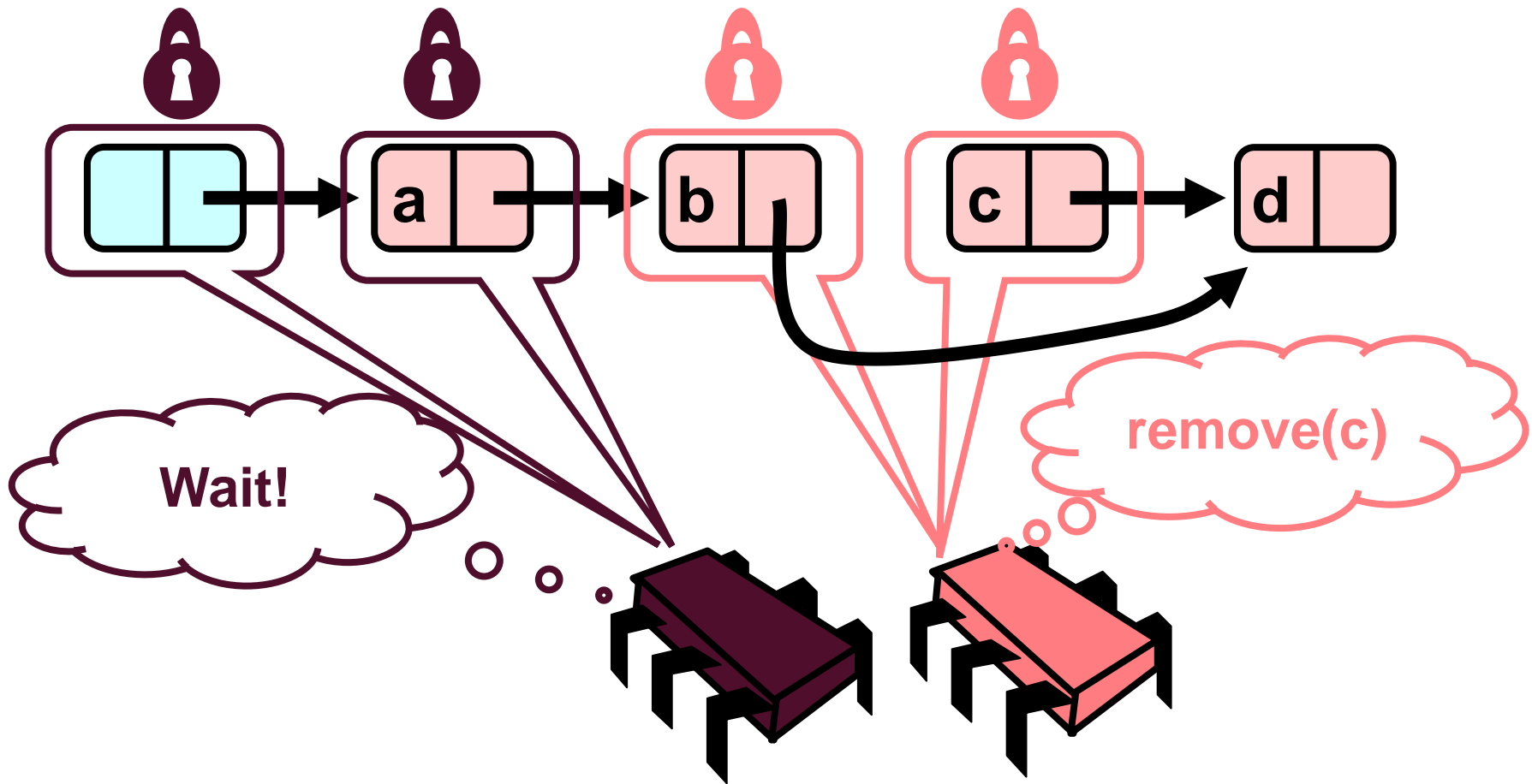
# Removing a Node



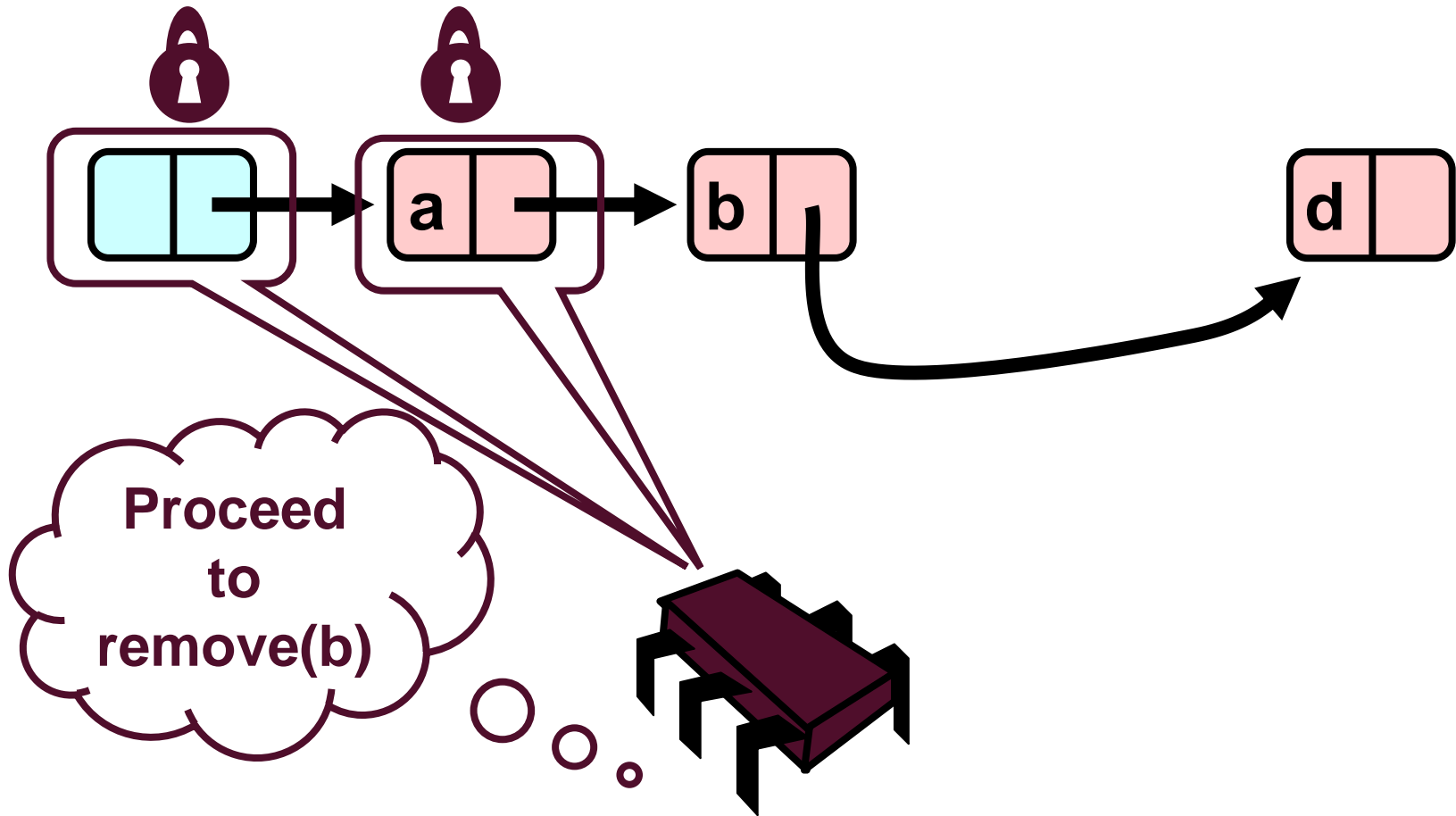
# Removing a Node



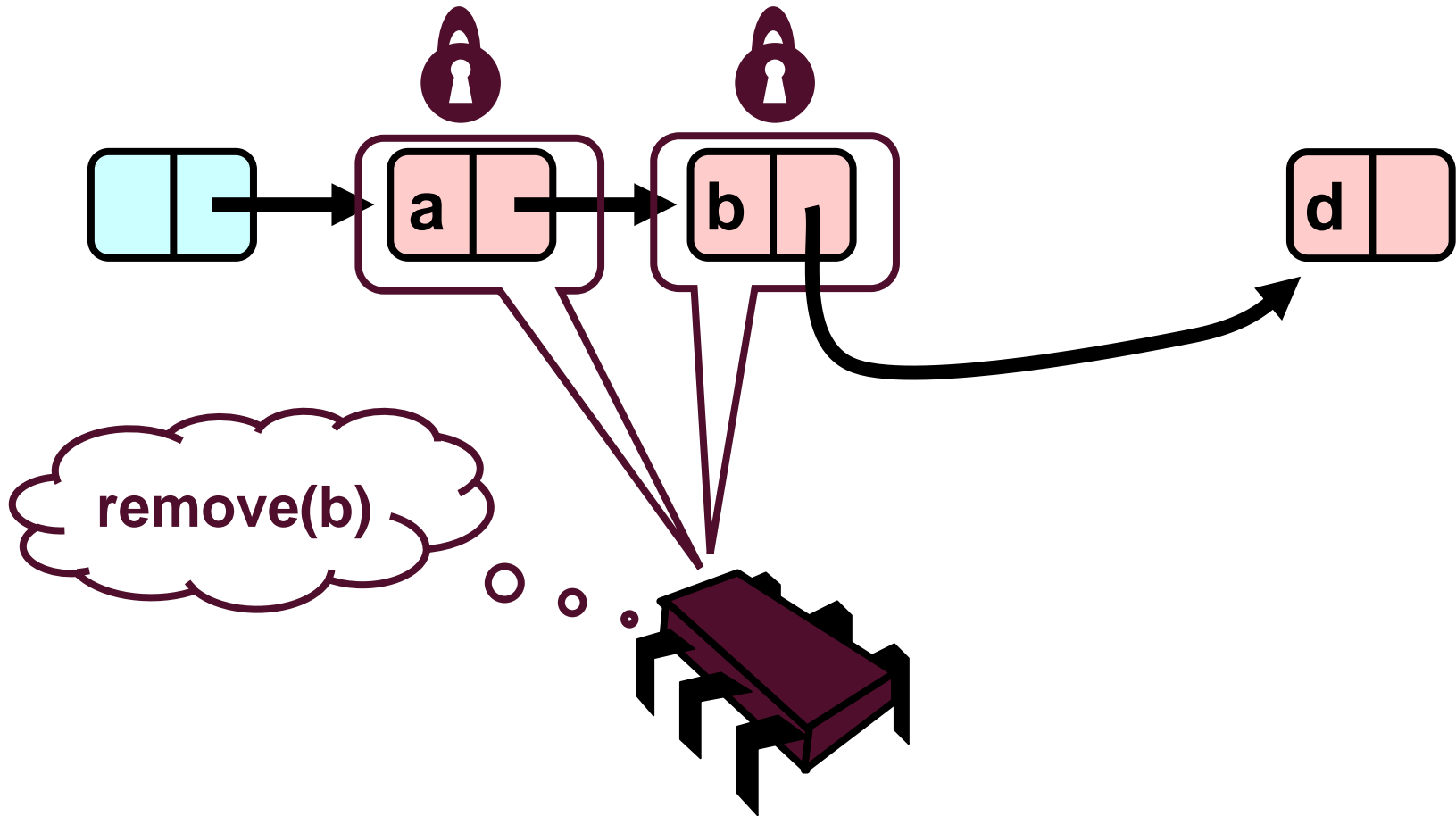
# Removing a Node



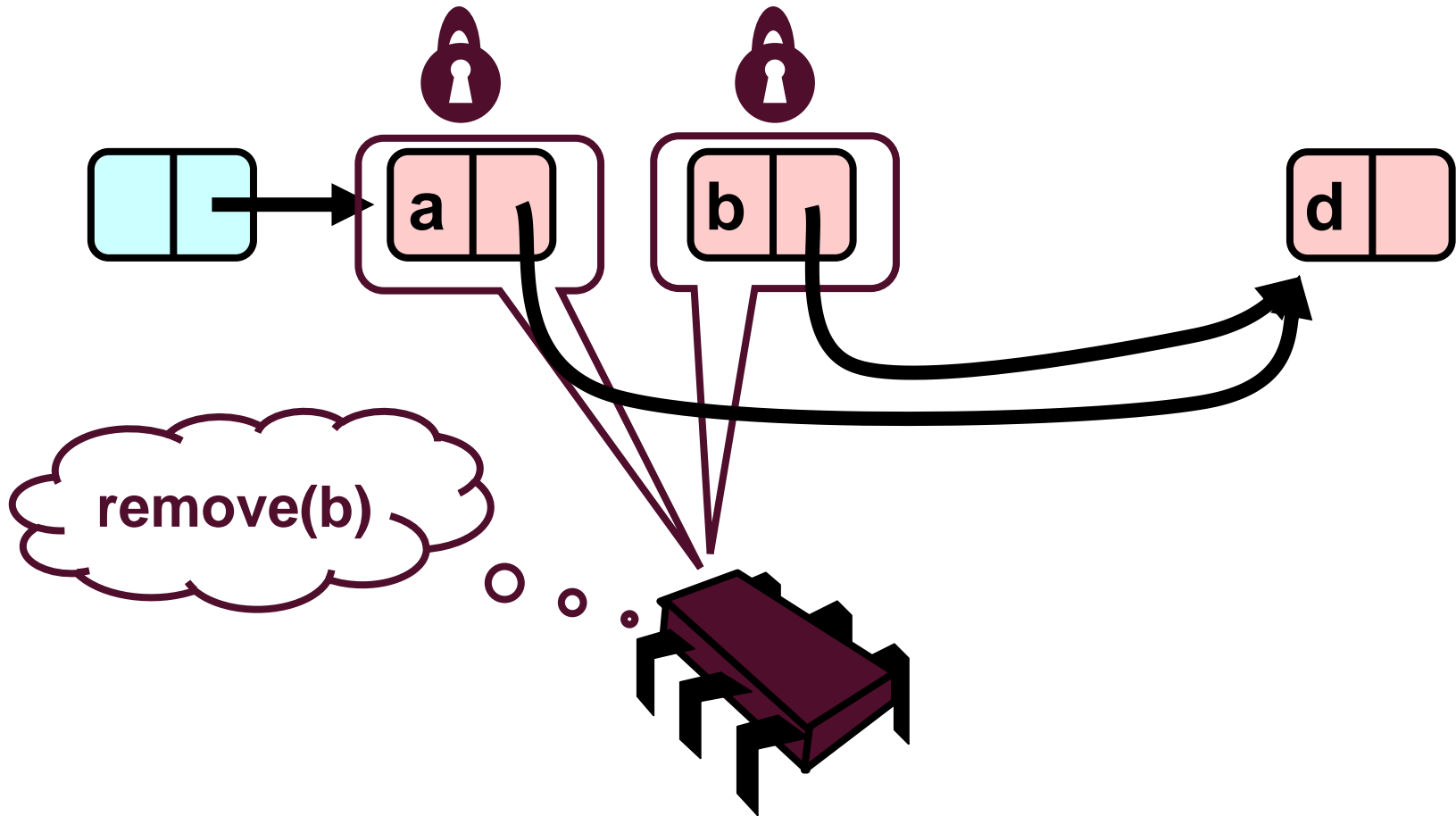
# Removing a Node



# Removing a Node

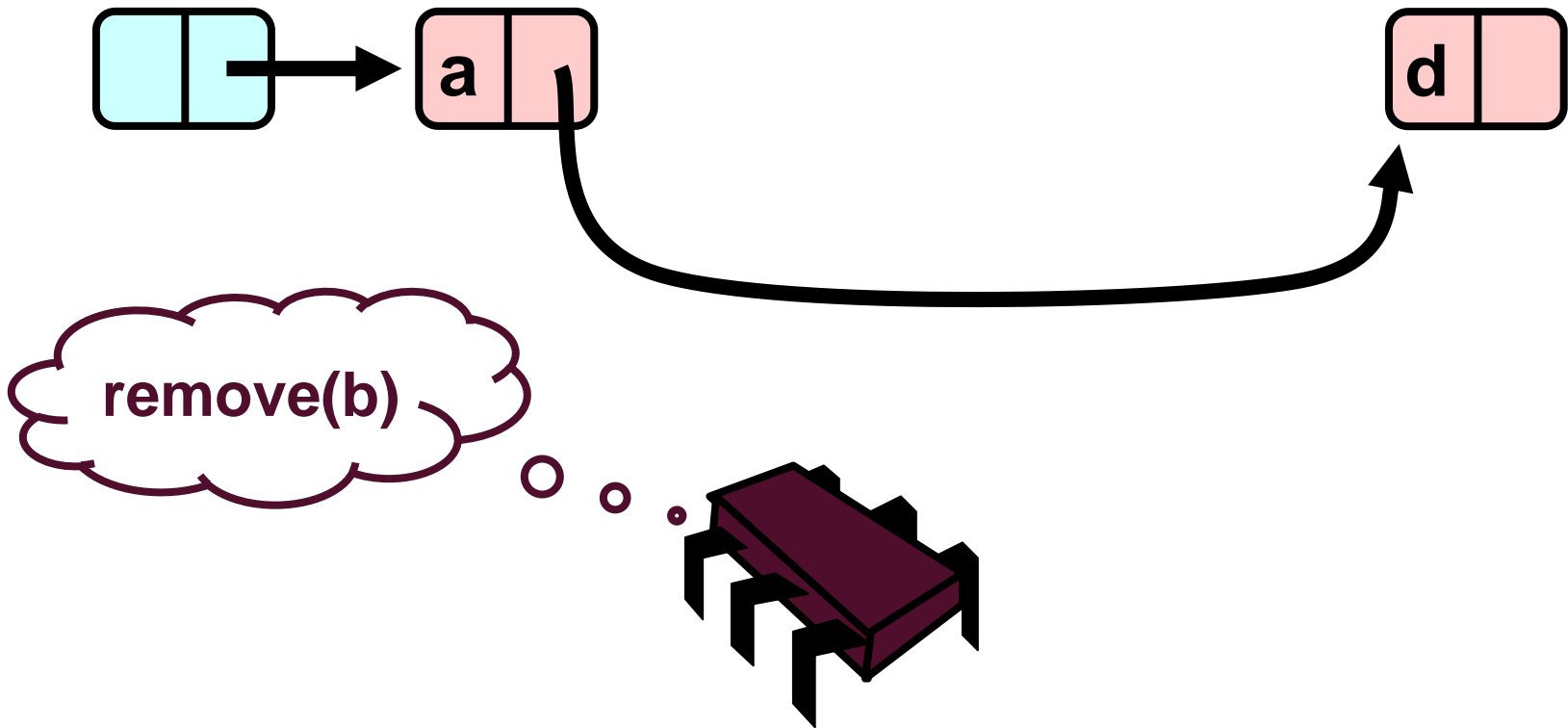


# Removing a Node





# Removing a Node



# What are the Issues?

- **We have fine-grained locking, will there be contention?**
  - Yes, the list can only be traversed sequentially, a remove of the 3<sup>rd</sup> item will block all other threads!
  - This is essentially still serialized if the list is short (since threads can only pipeline on list elements)
- **Other problems, ignoring contention?**
  - Must acquire  $O(|S|)$  locks

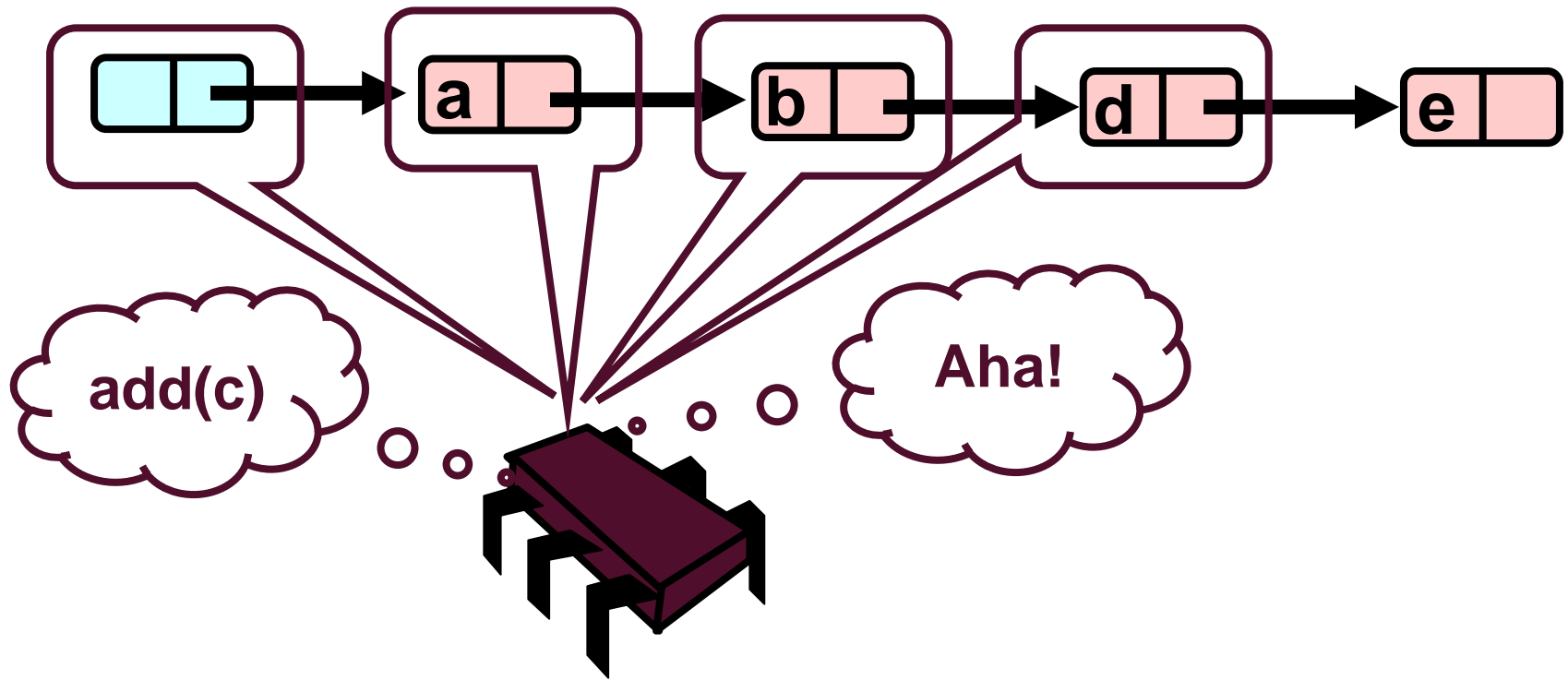
# Trick 2: Reader/Writer Locking

- **Same hand-over-hand locking**
  - Traversal uses reader locks
  - Once add finds position or remove finds target node, upgrade **both** locks to writer locks
  - Need to guarantee deadlock and starvation freedom!
- **Allows truly concurrent traversals**
  - Still blocks behind writing threads
  - Still  $O(|S|)$  lock/unlock operations

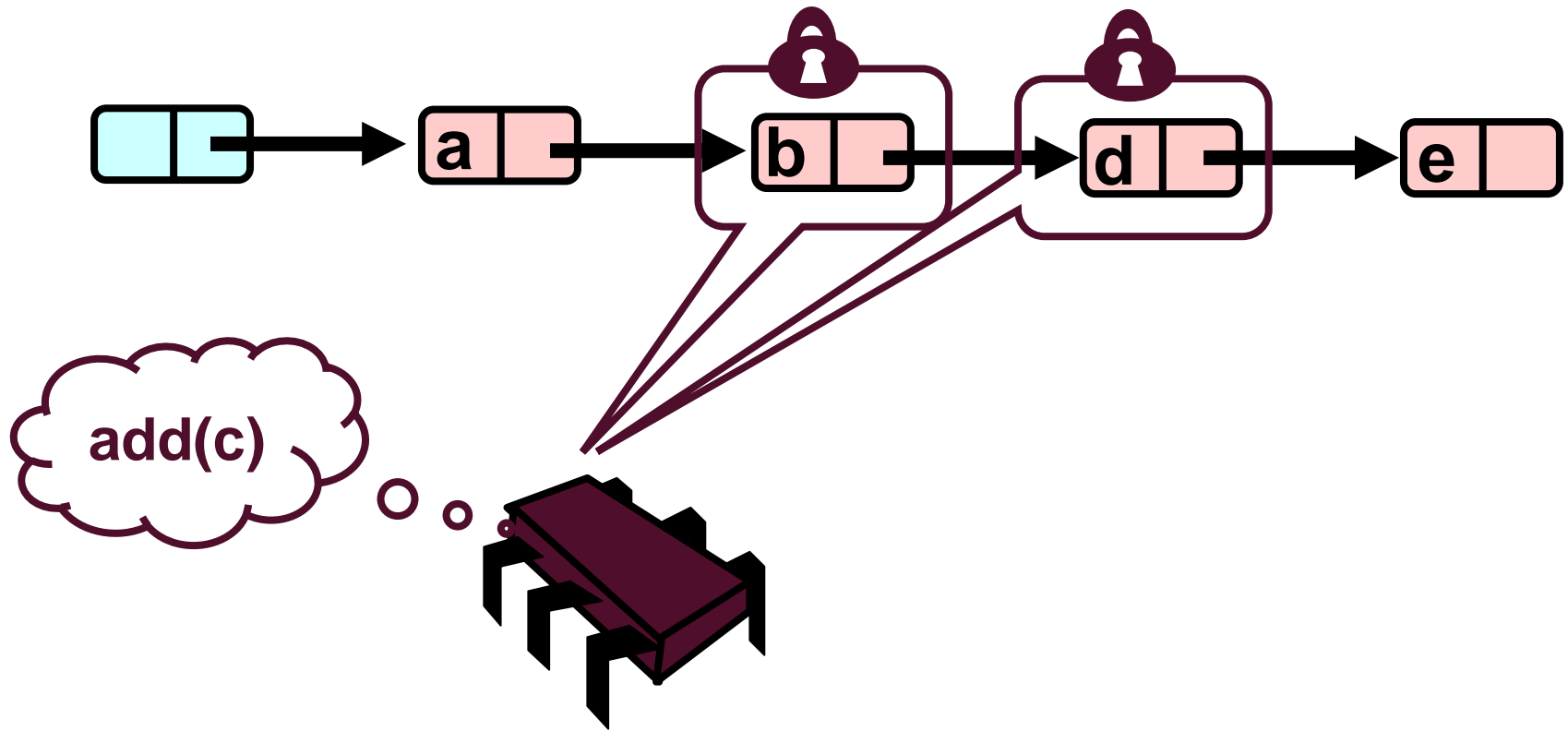
# Trick 3: Optimistic synchronization

- **Similar to reader/writer locking but traverse list without locks**
  - Dangerous! Requires additional checks.
- **Harder to proof correct**

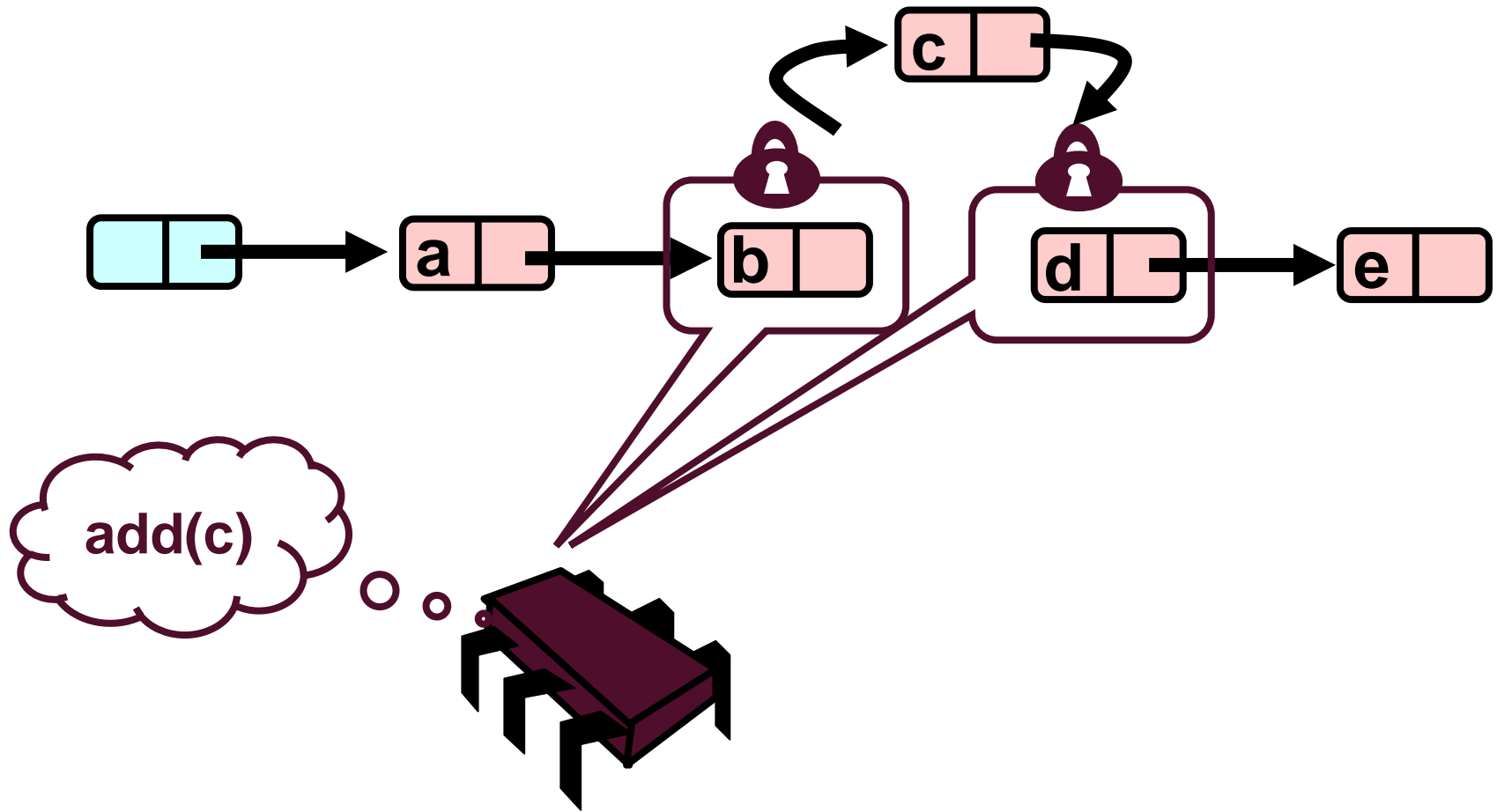
# Optimistic: Traverse without Locking



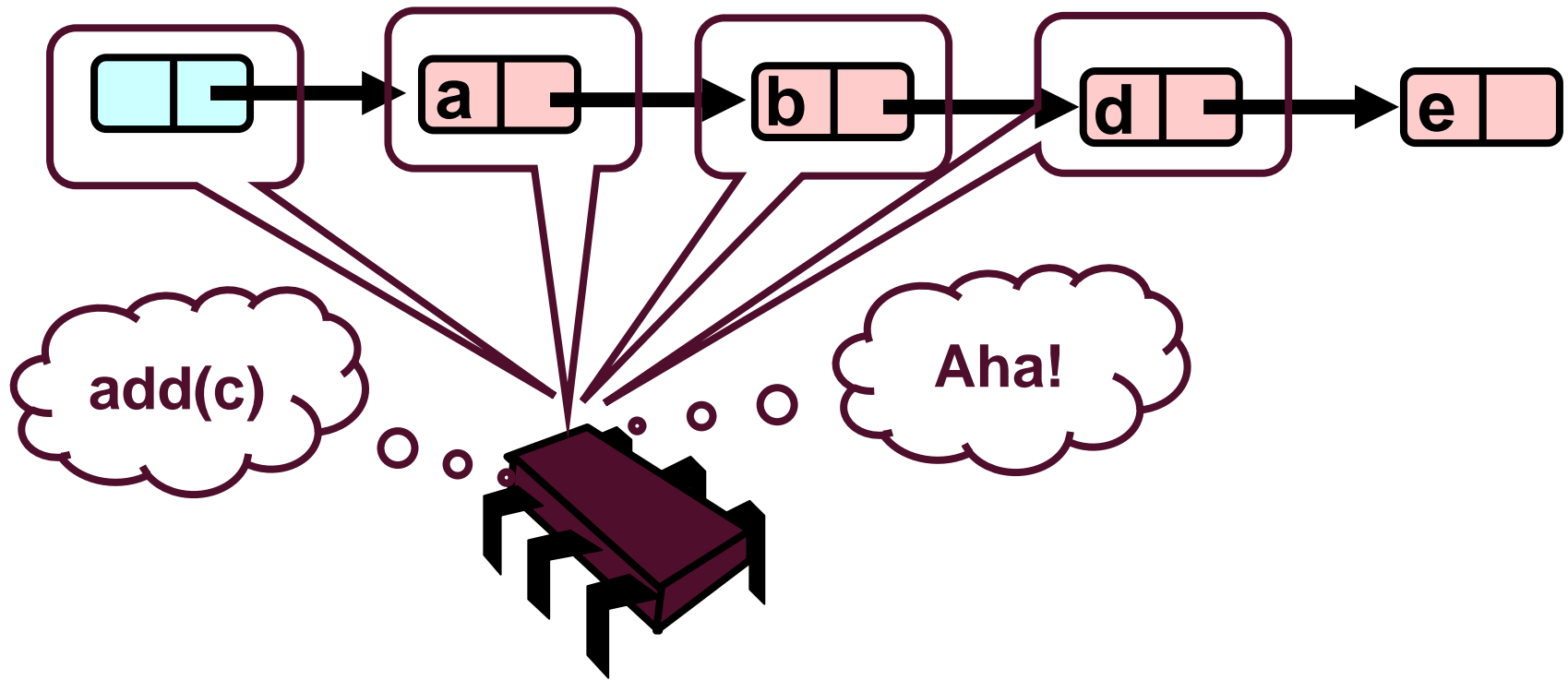
# Optimistic: Lock and Load



# Optimistic: Lock and Load

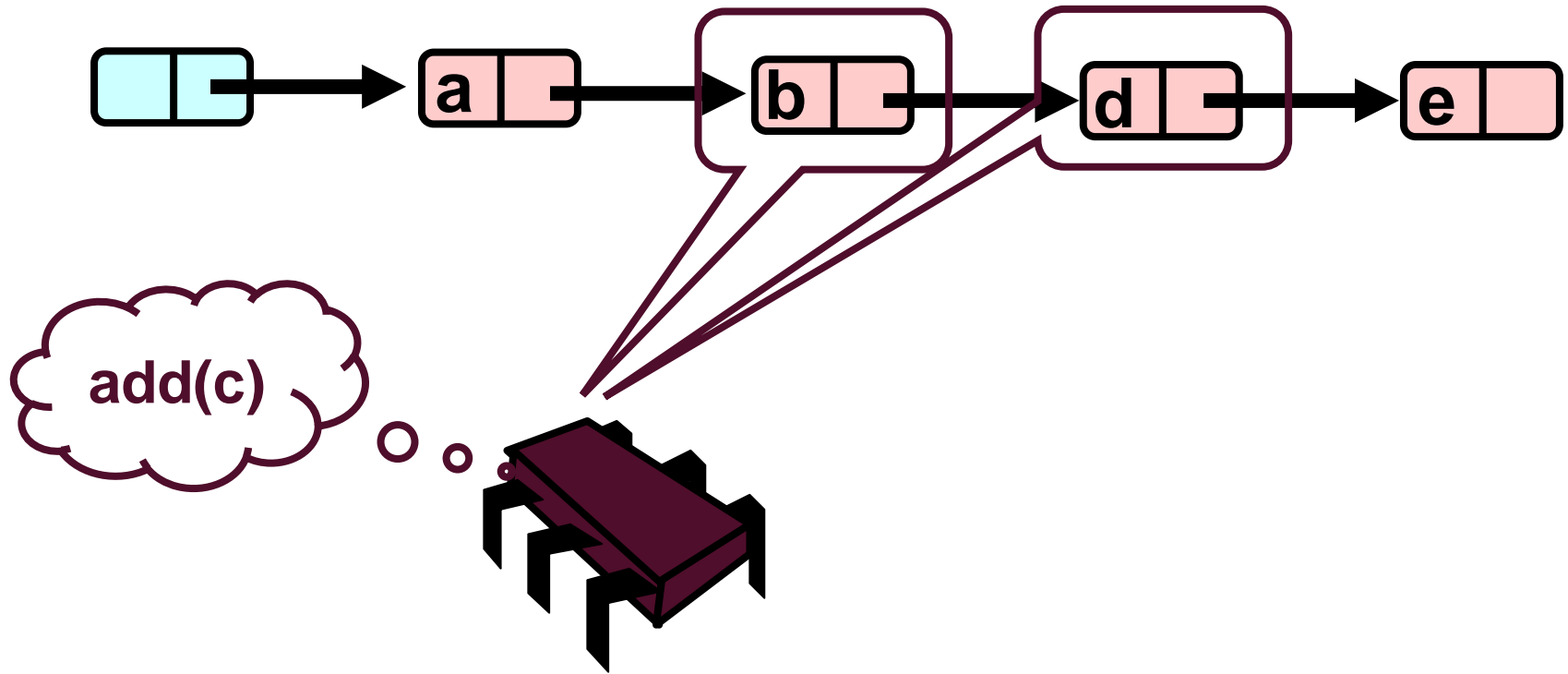


# What could go wrong?

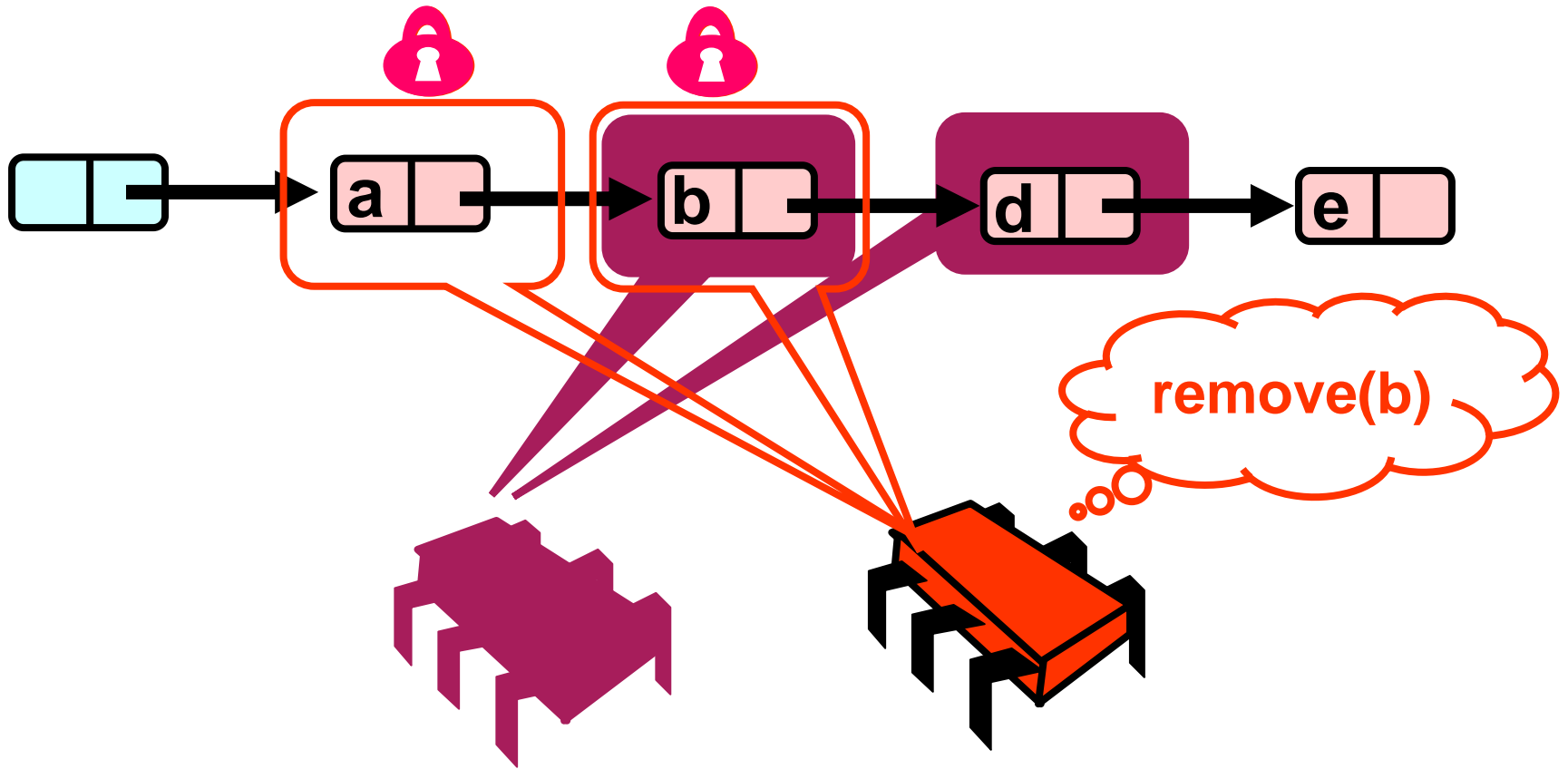




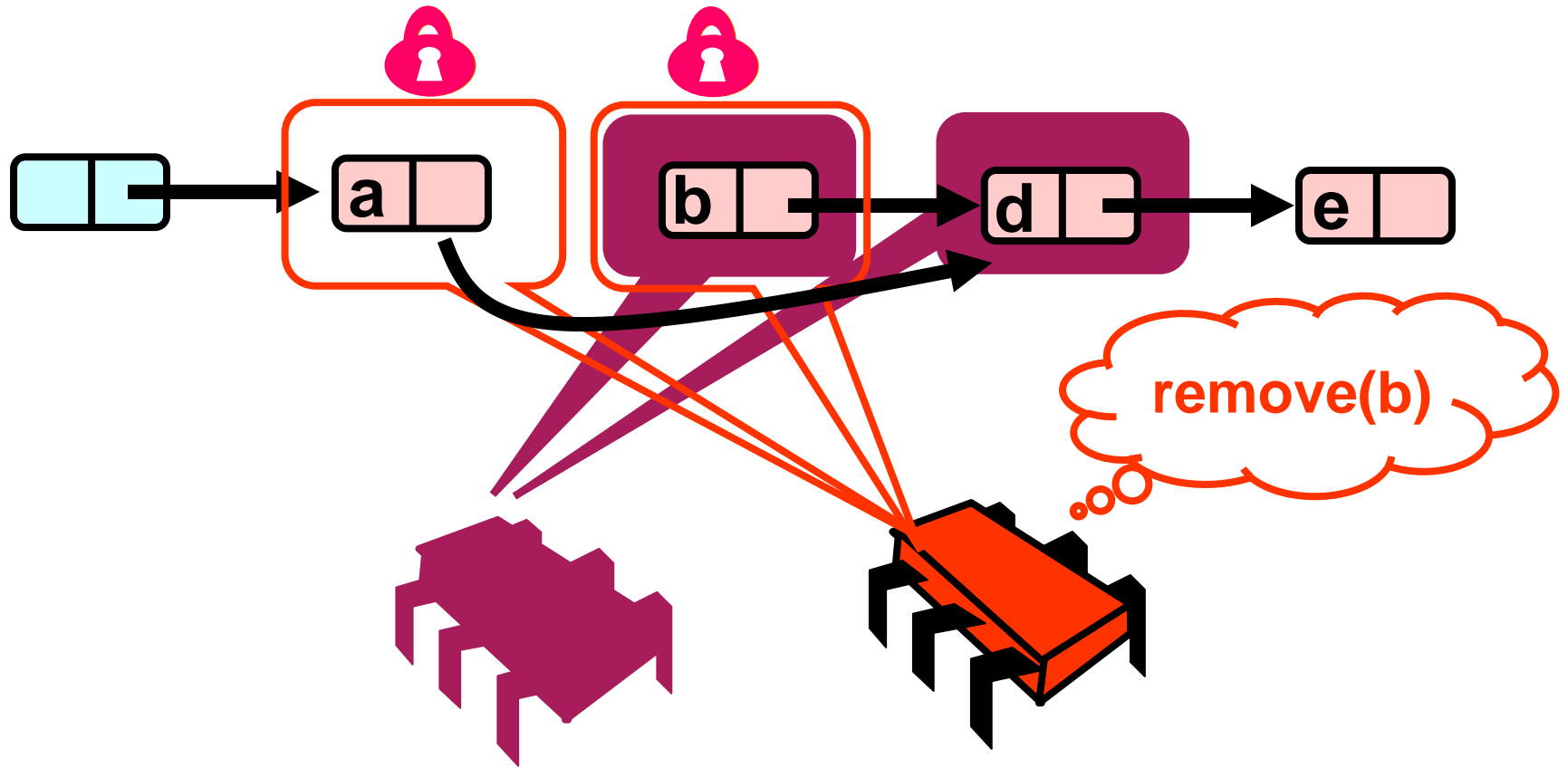
# What could go wrong?



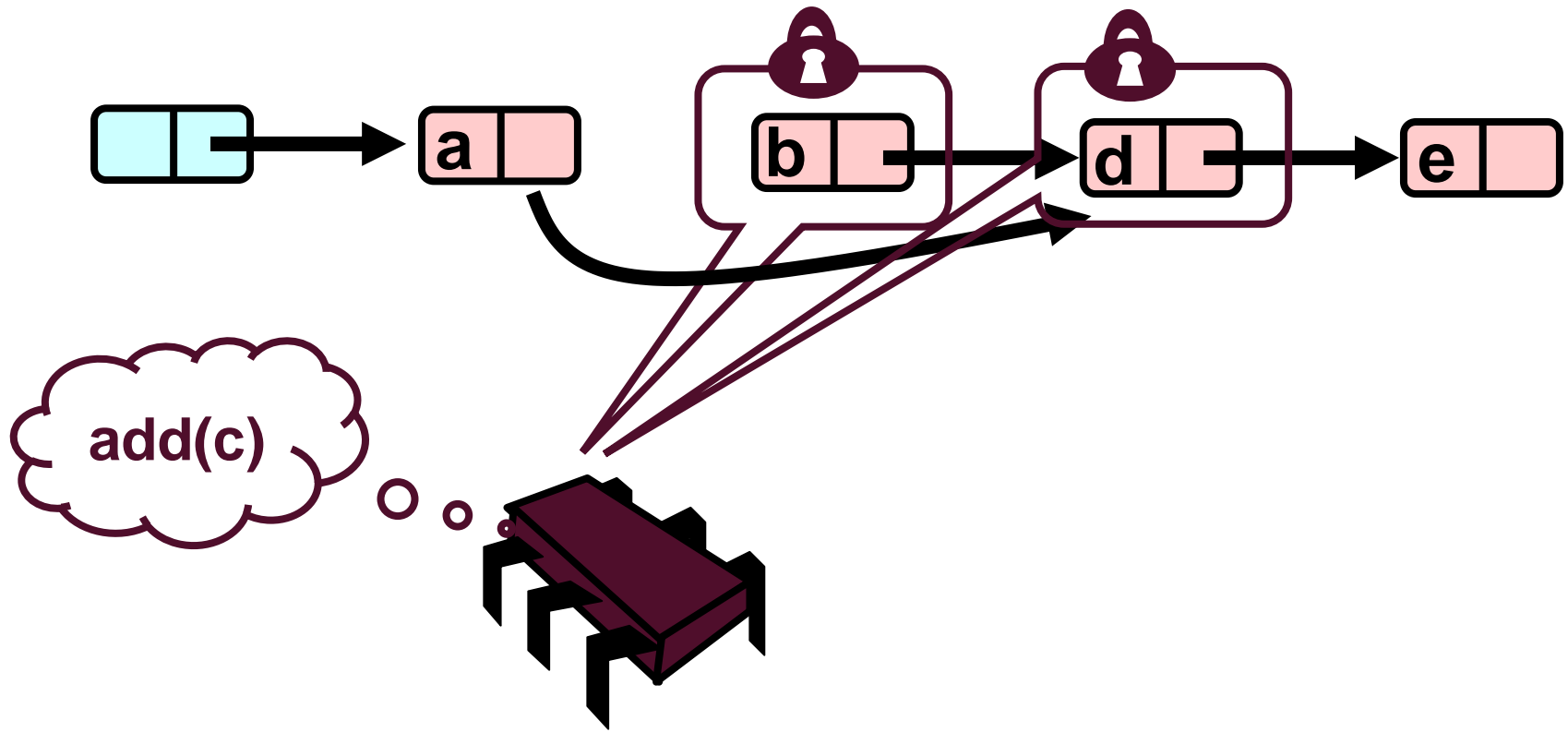
# What could go wrong?



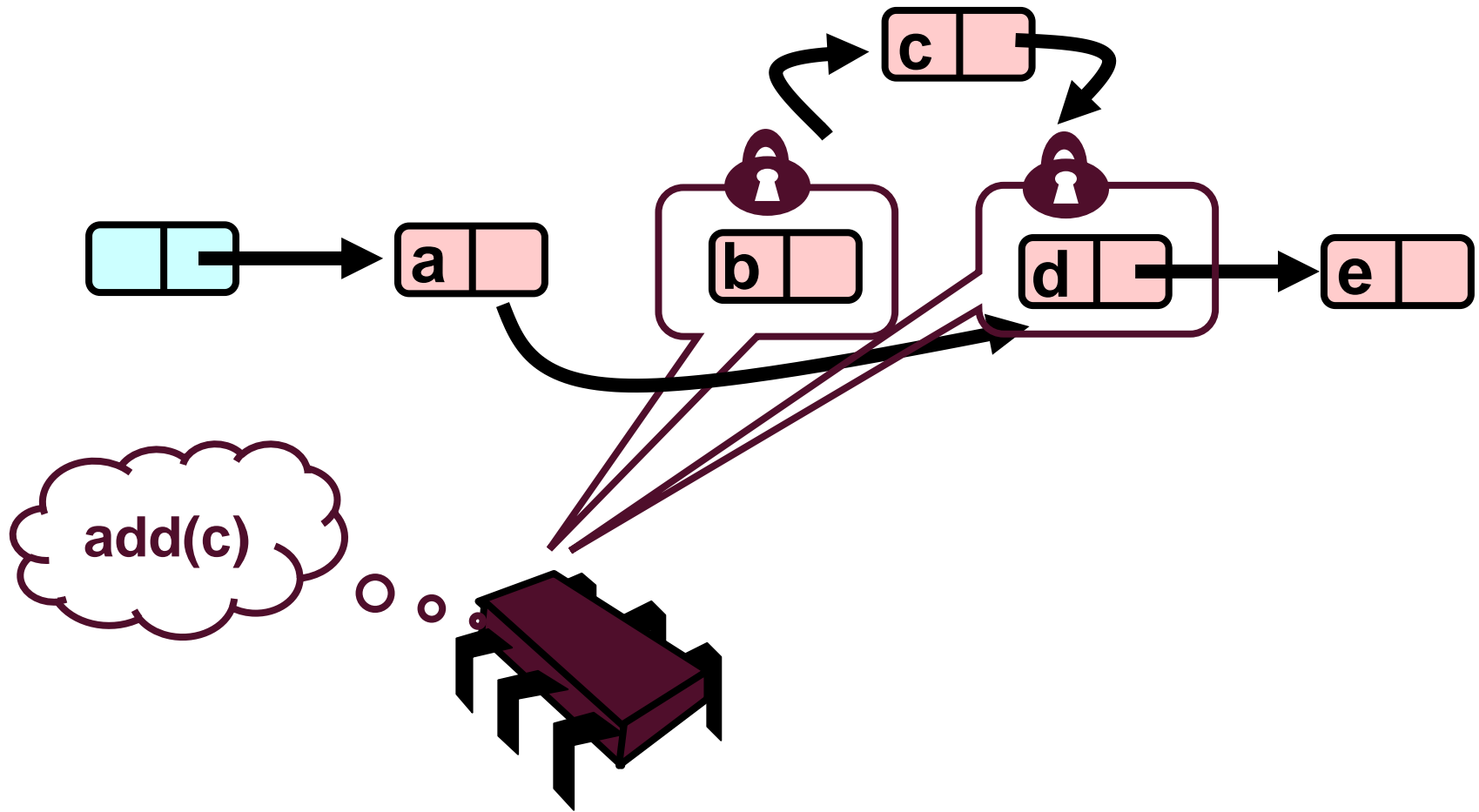
# What could go wrong?



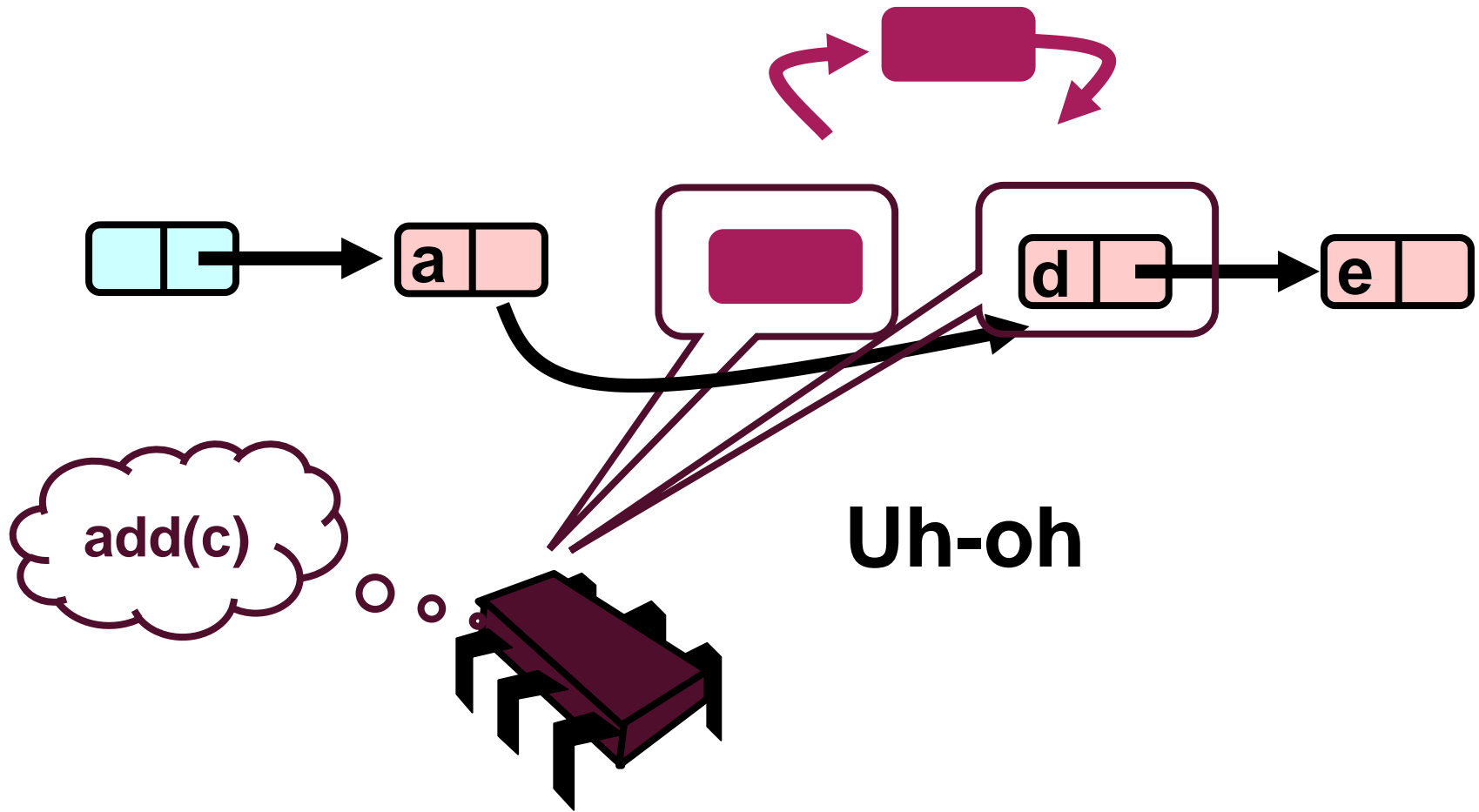
# What could go wrong?



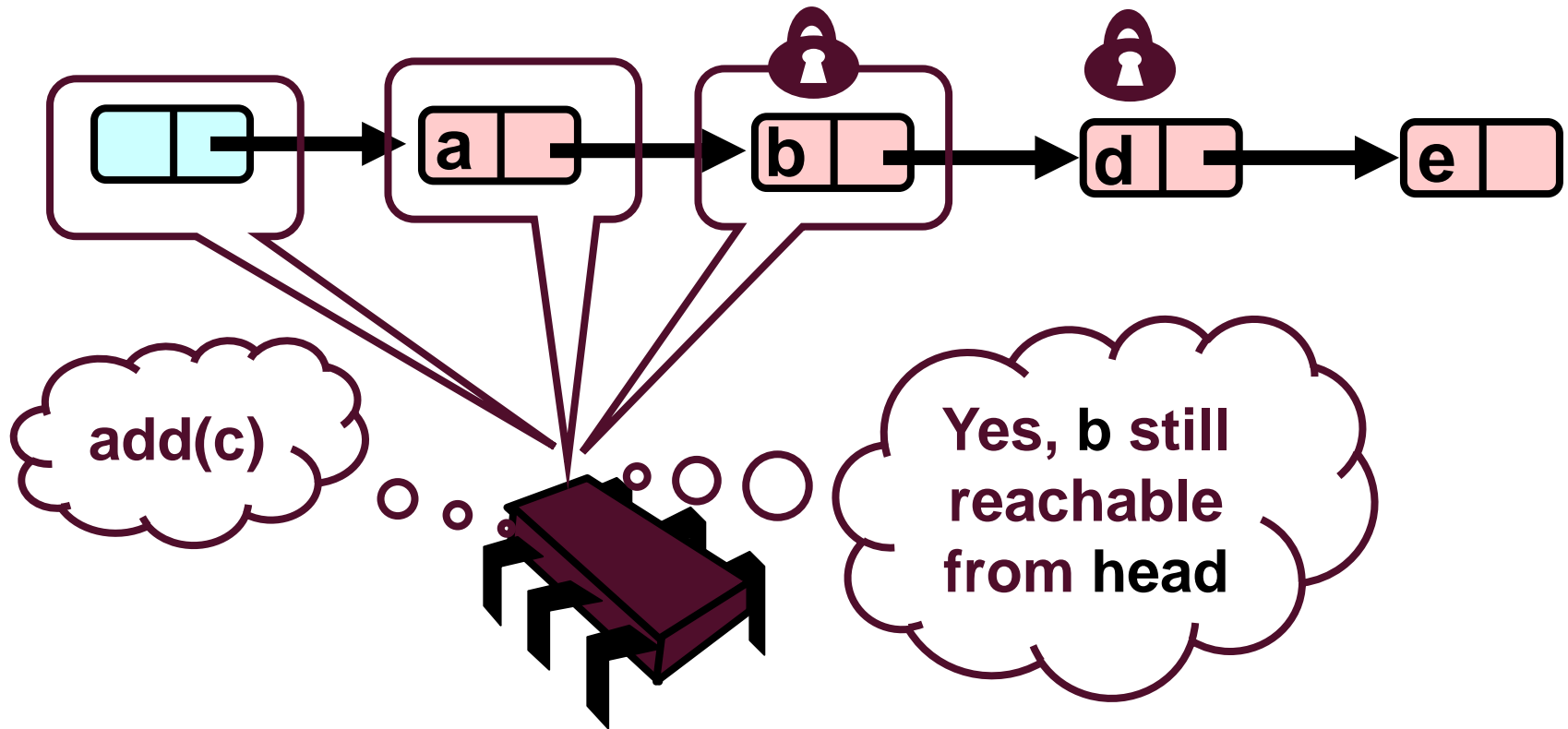
# What could go wrong?



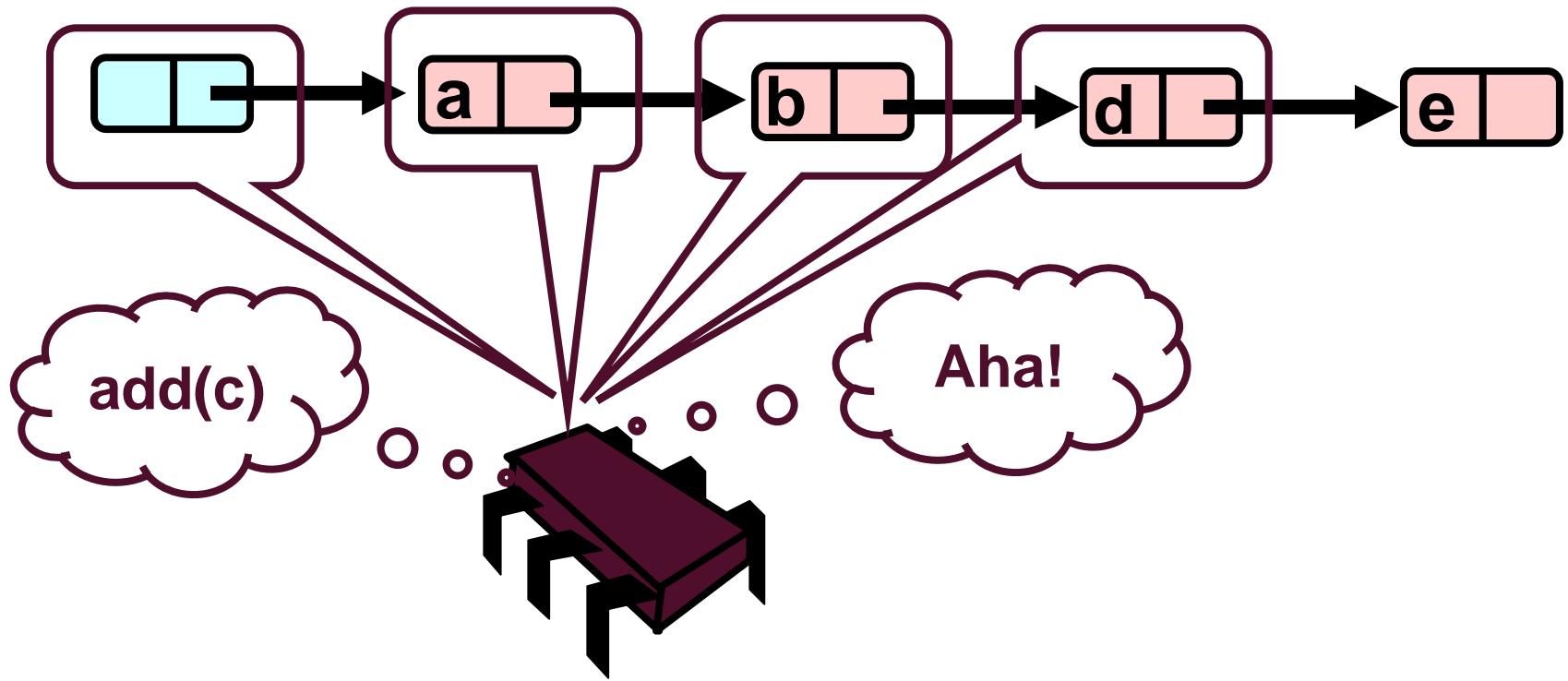
# What could go wrong?



# Validate – Part 1

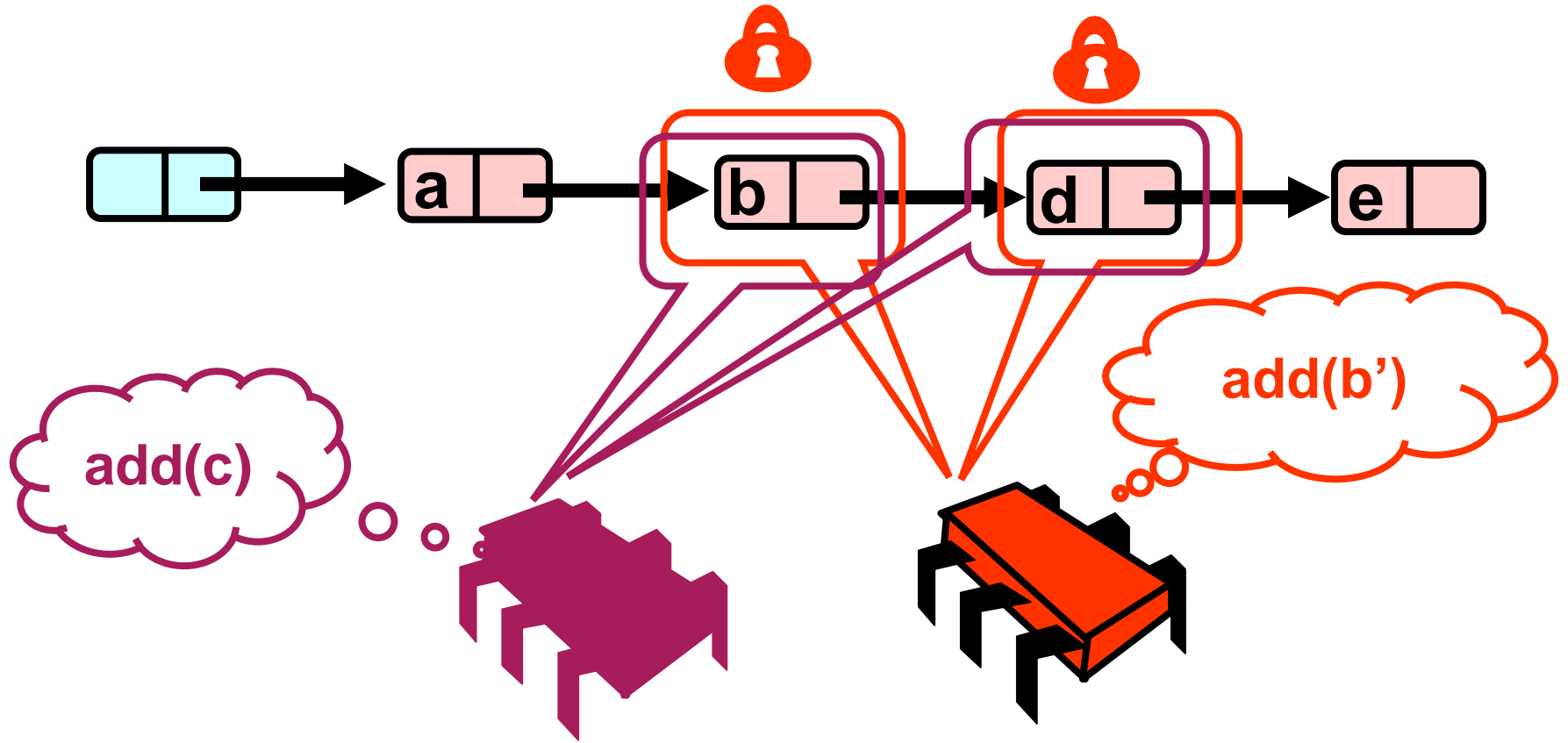


# What Else Could Go Wrong?

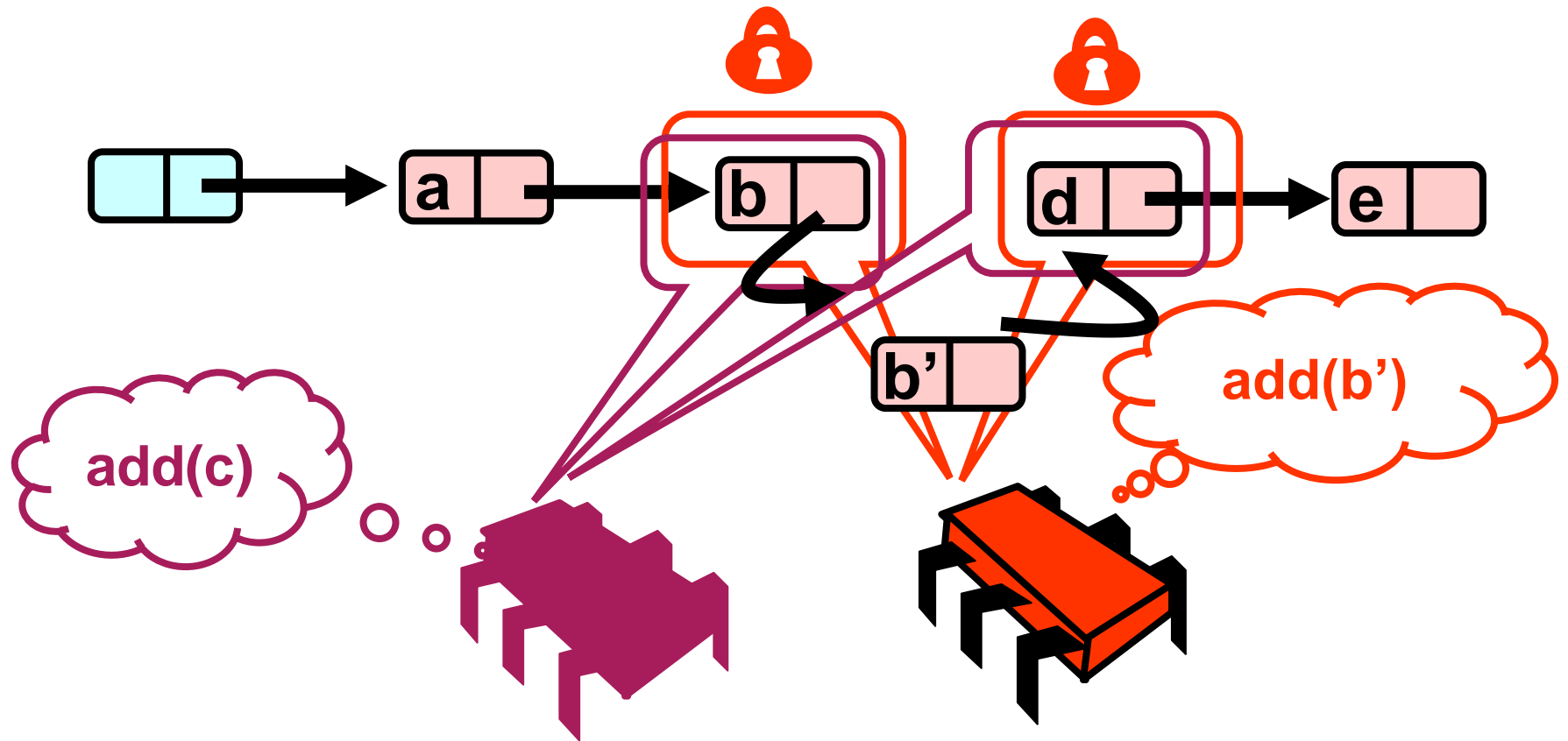




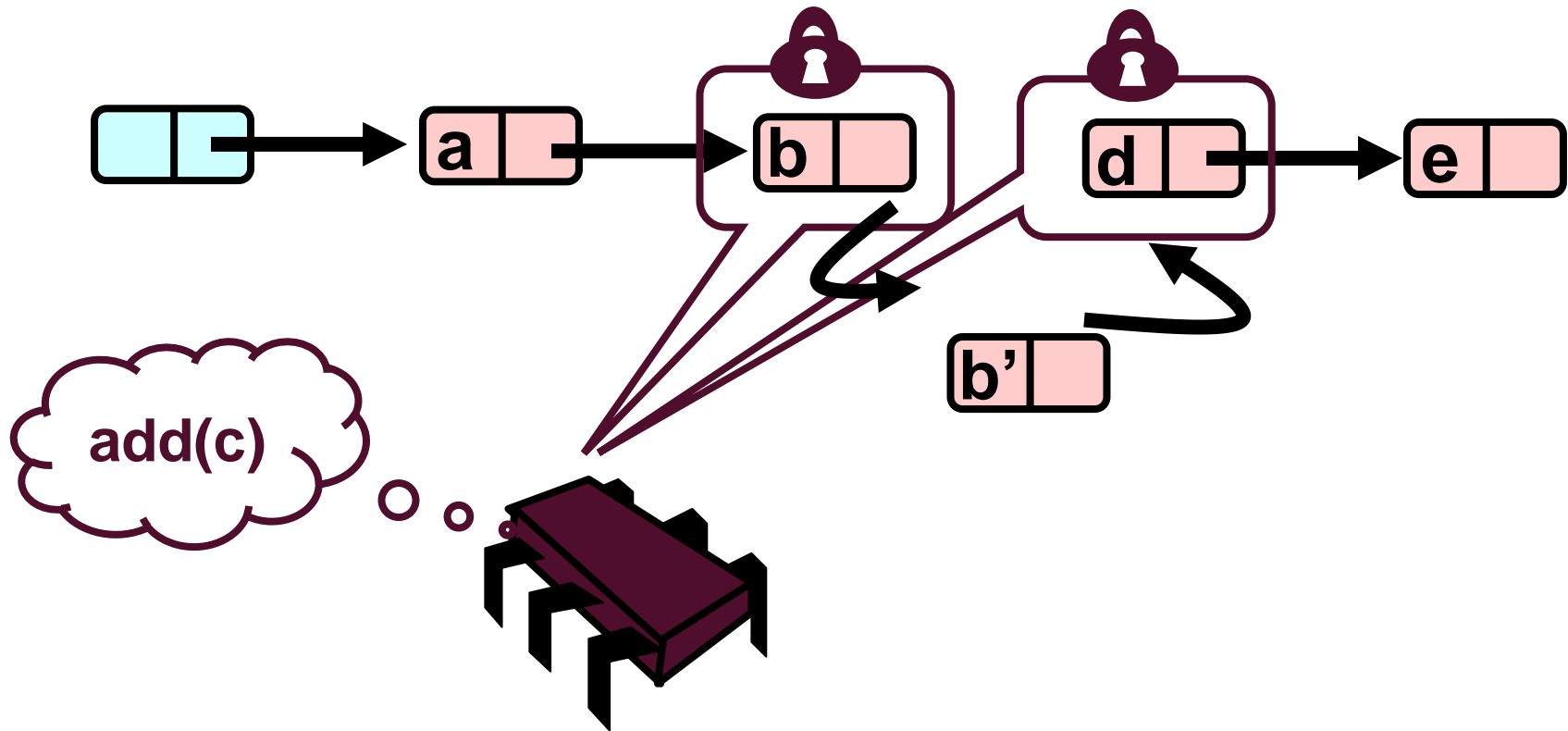
# What Else Could Go Wrong?



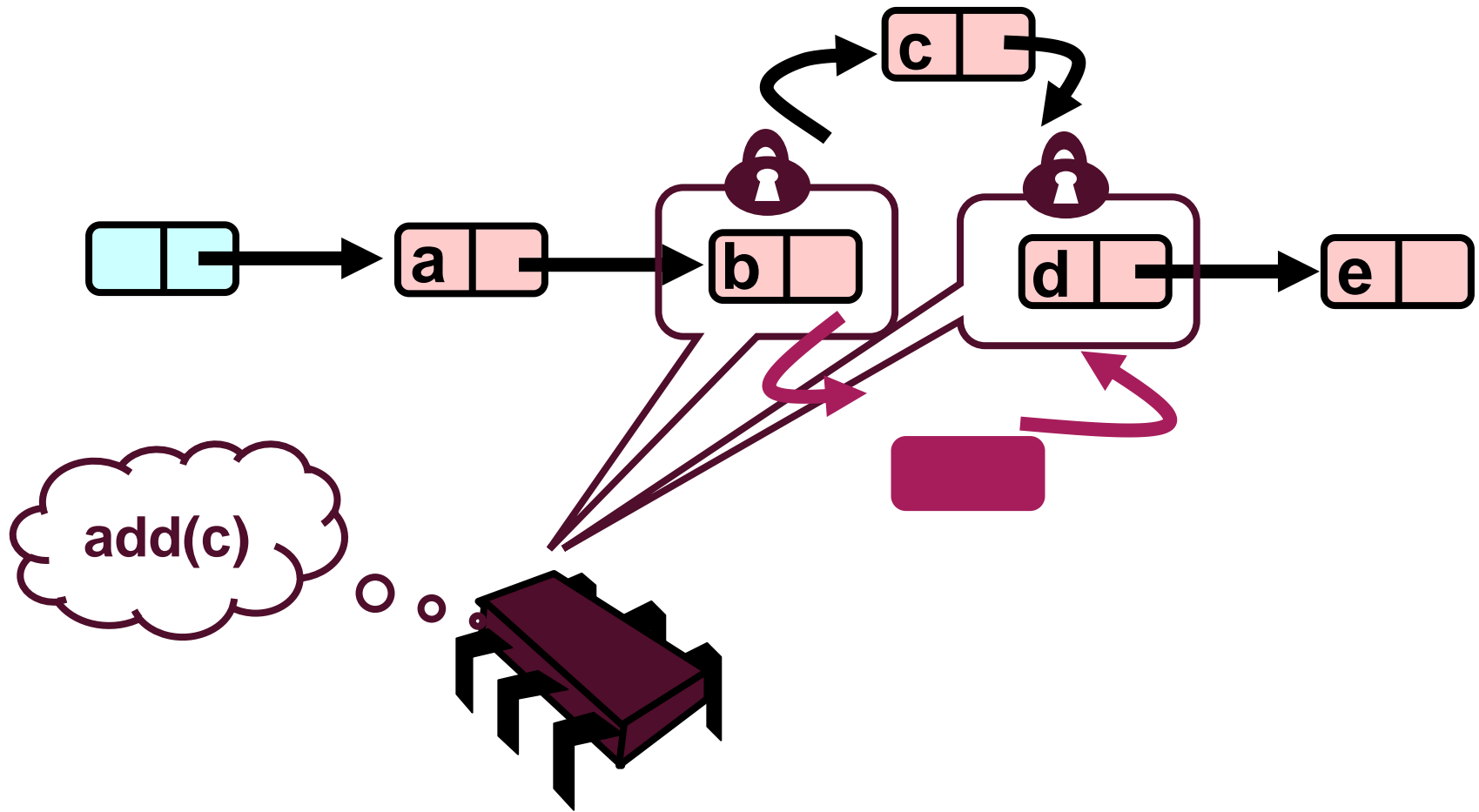
# What Else Could Go Wrong?



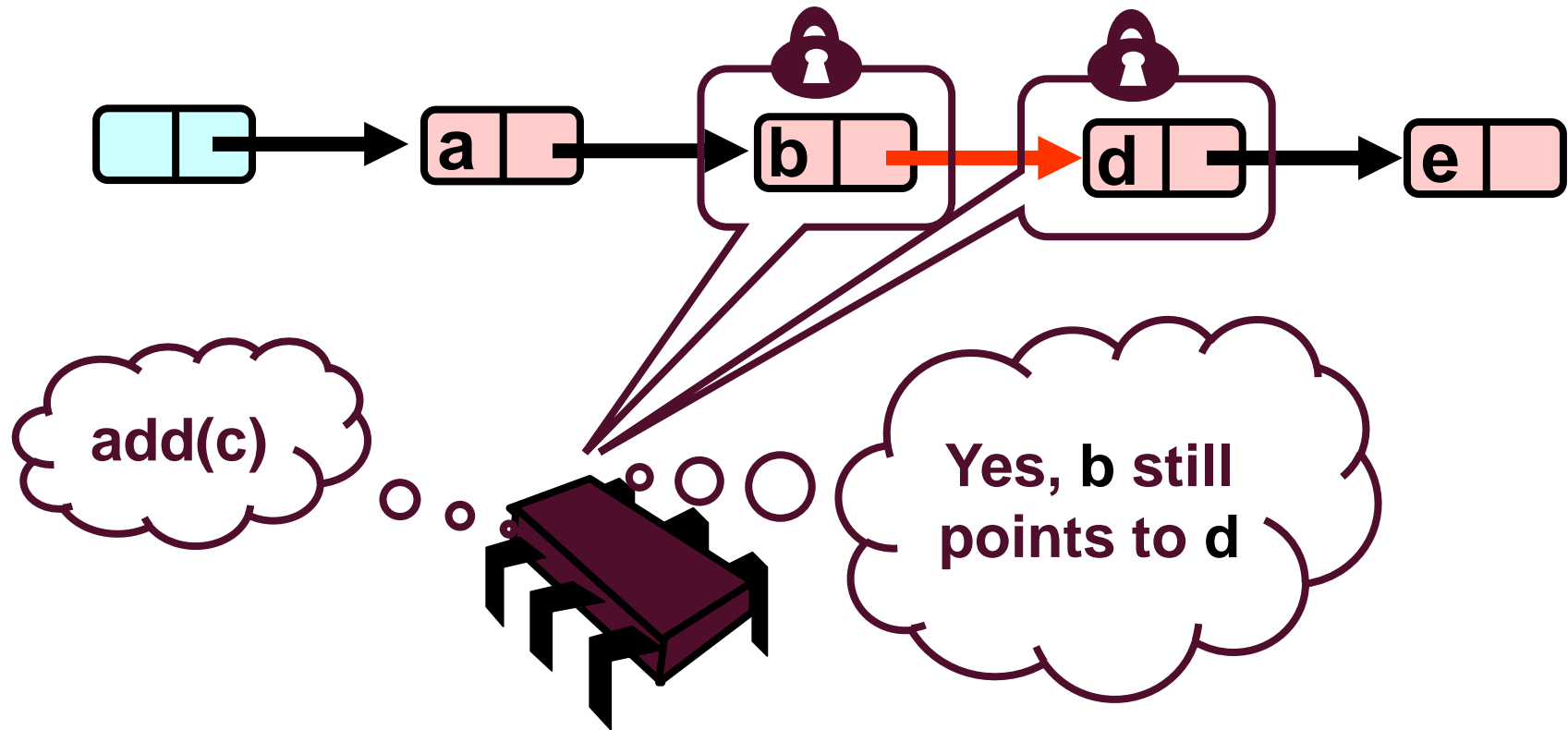
# What Else Could Go Wrong?



# What Else Could Go Wrong?



# Validate Part 2 (while holding locks)



# Optimistic synchronization

- **One MUST validate AFTER locking**

1. Check if the path how we got there is still valid!
2. Check if locked nodes are still connected
  - If any of those checks fail?

*Start over from the beginning (hopefully rare)*

- **Not starvation-free**

- A thread may need to abort forever if nodes are added/removed
- Should be rare in practice!

- **Other disadvantages?**

- All operations requires two traversals of the list!
- Even contains() needs to check if node is still in the list!

# Trick 4: Lazy synchronization

- **We really want one list traversal**
- **Also, contains() should be wait-free**
  - Is probably the most-used operation
- **Lazy locking is similar to optimistic**
  - Key insight: removing is problematic
  - Perform it “lazily”
- **Add a new “valid” field**
  - Indicates if node is still in the set
  - Can remove it without changing list structure!
  - Scan once, contains() never locks!

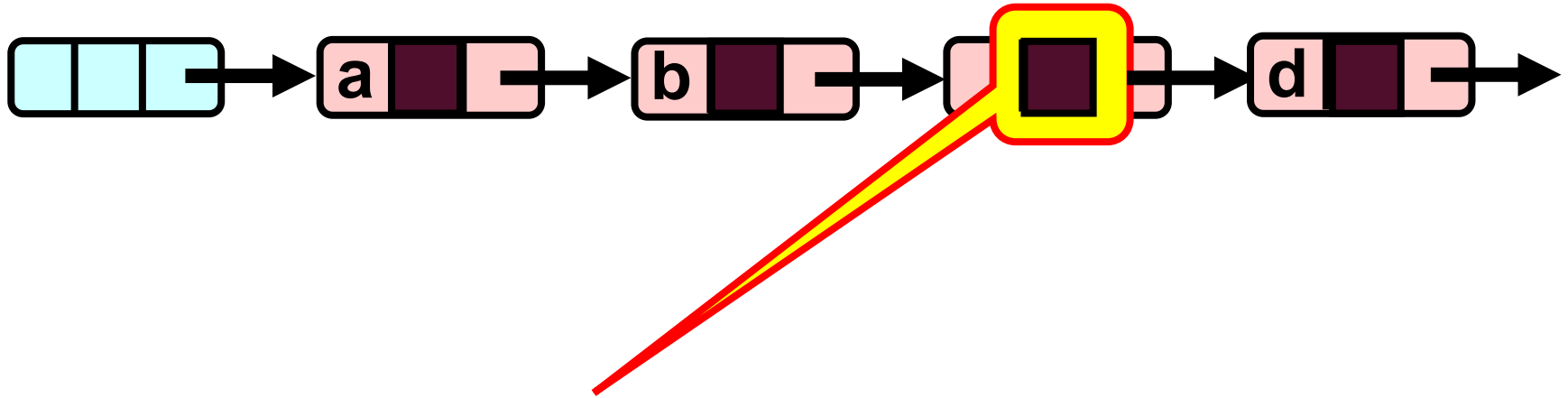
```
typedef struct {  
    int key;  
    node *next;  
    lock_t lock;  
    boolean valid;  
} node;
```

# Lazy Removal



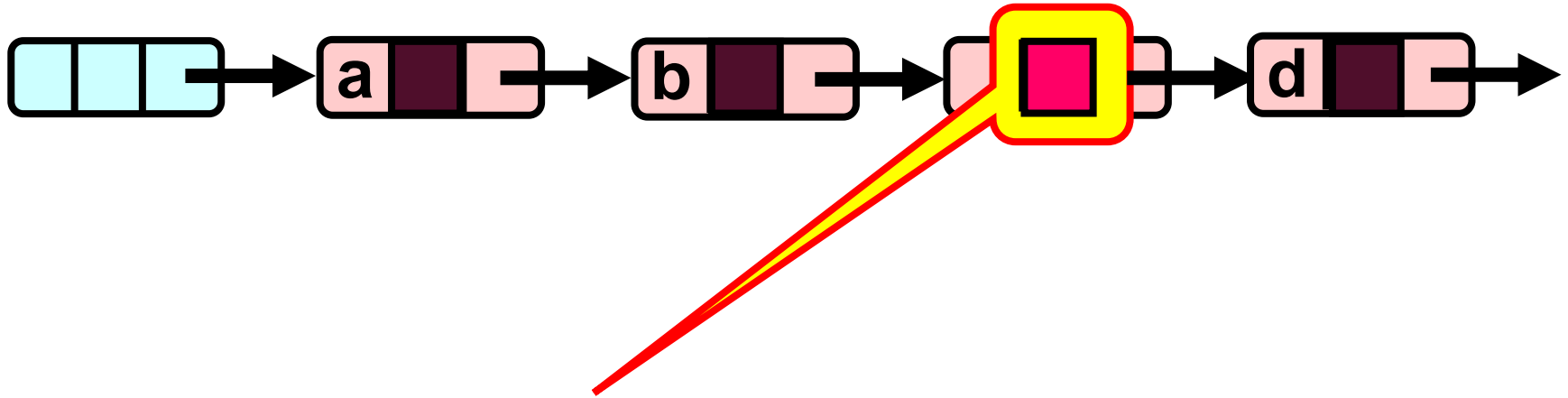


# Lazy Removal



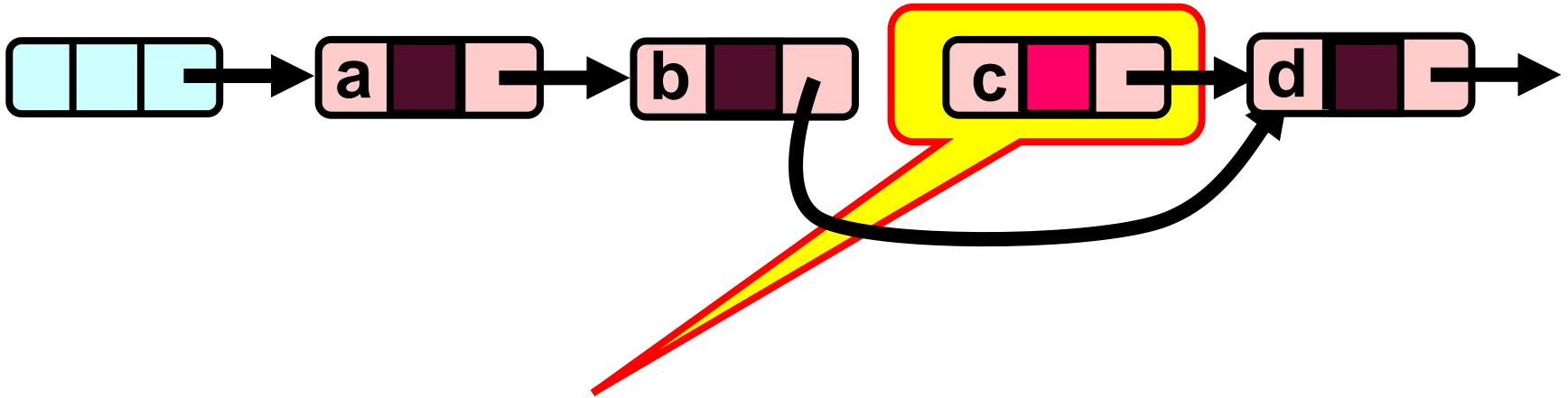
**Present in list**

# Lazy Removal



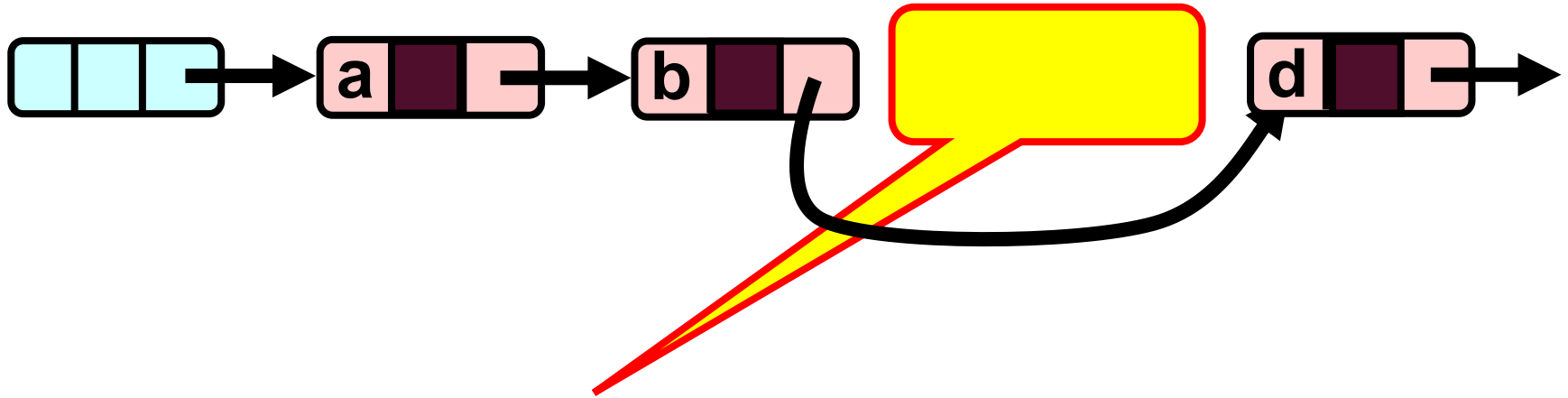
**Logically deleted**

# Lazy Removal



Physically deleted

# Lazy Removal

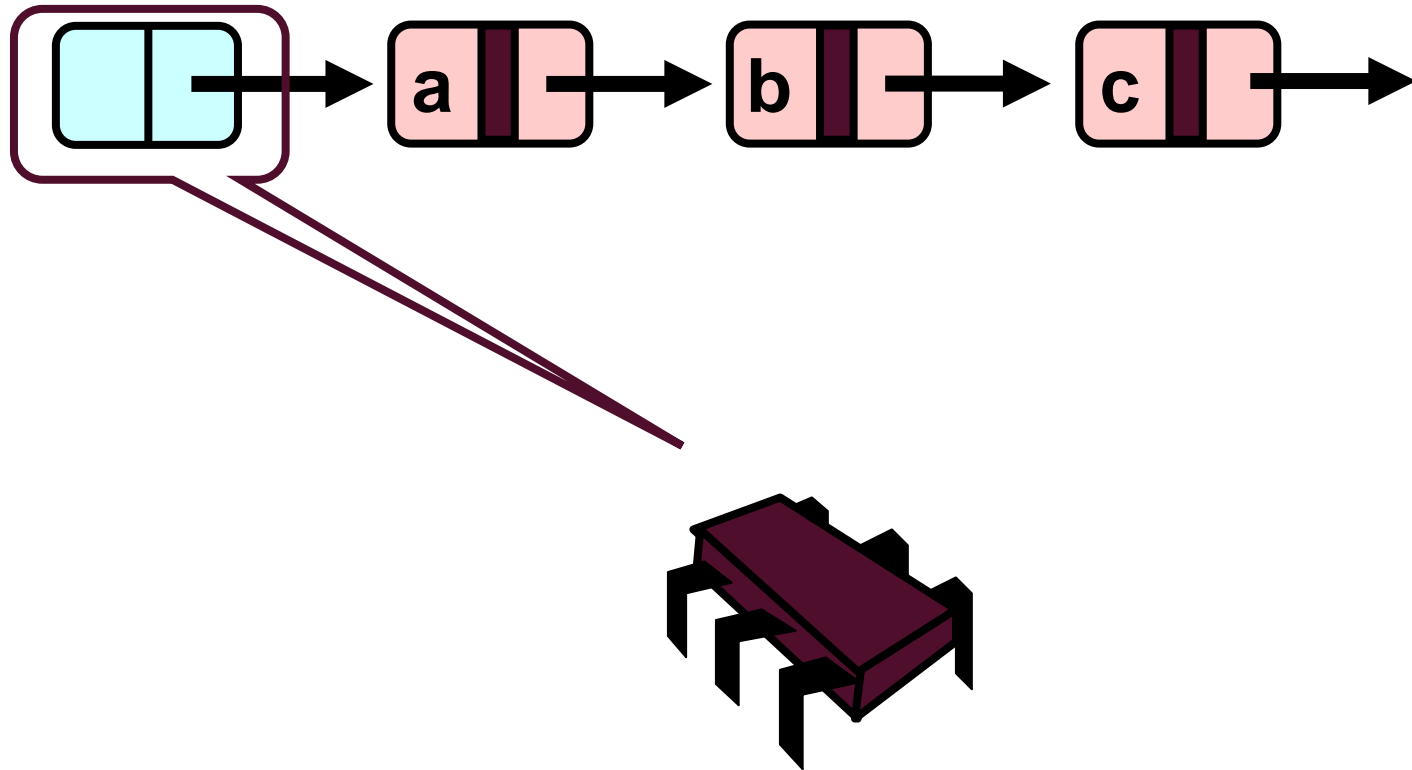


**Physically deleted**

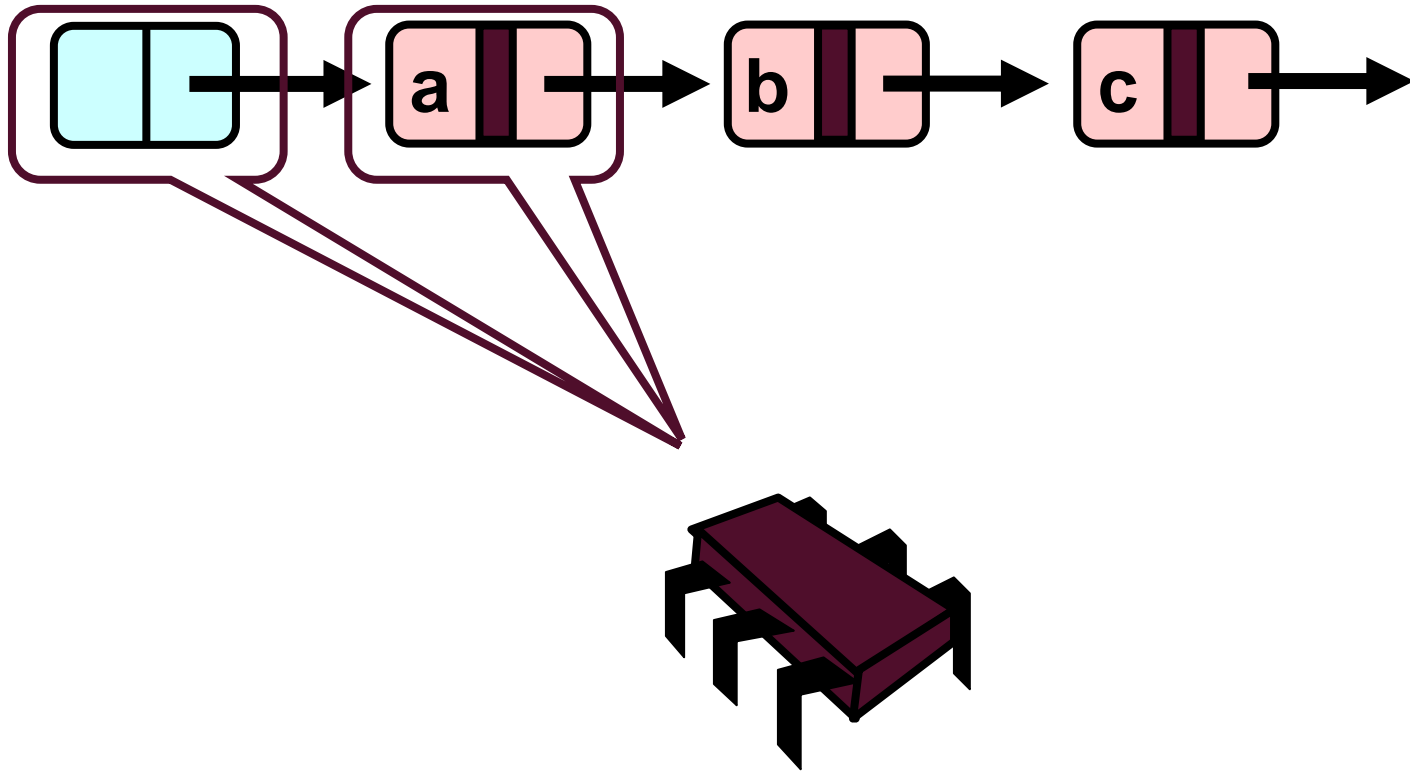
# How does it work?

- **Eliminates need to re-scan list for reachability**
  - Maintains invariant that every **unmarked** node is reachable!
- **Contains can now simply traverse the list**
  - Just check marks, not reachability, no locks
- **Remove/Add**
  - Scan through locked and marked nodes
  - Removing does not delay others
  - Must only lock when list structure is updated
    - Check if neither pred nor curr are marked, pred.next == curr*

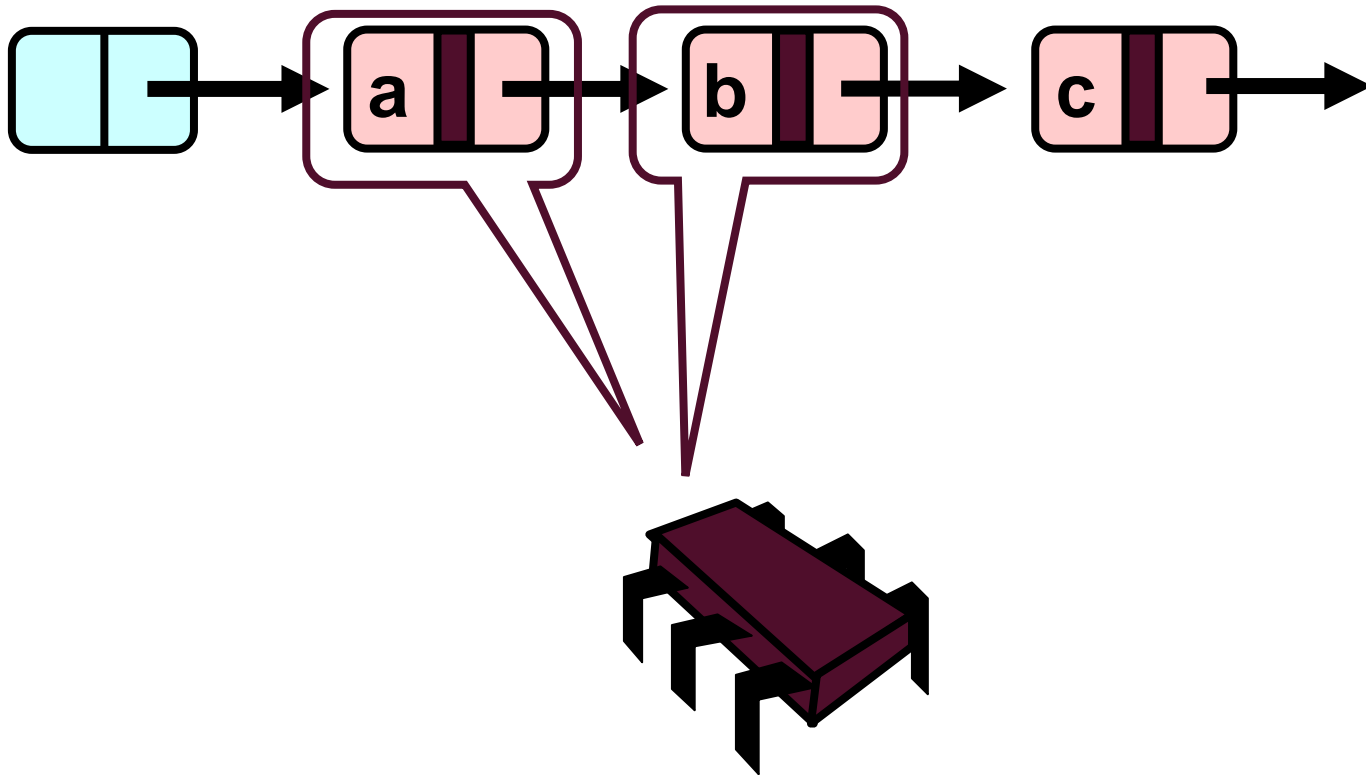
# Business as Usual



# Business as Usual

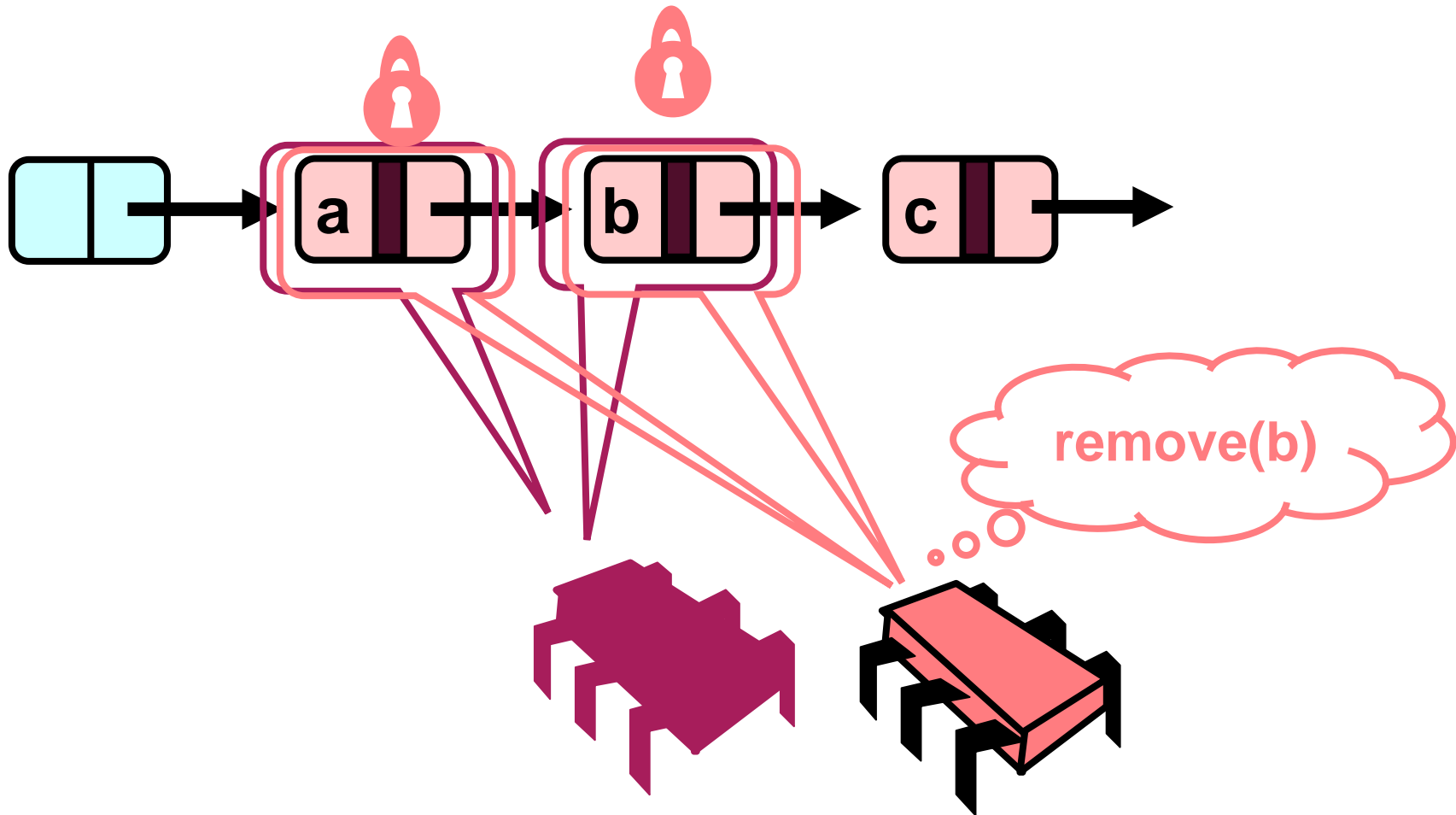


# Business as Usual

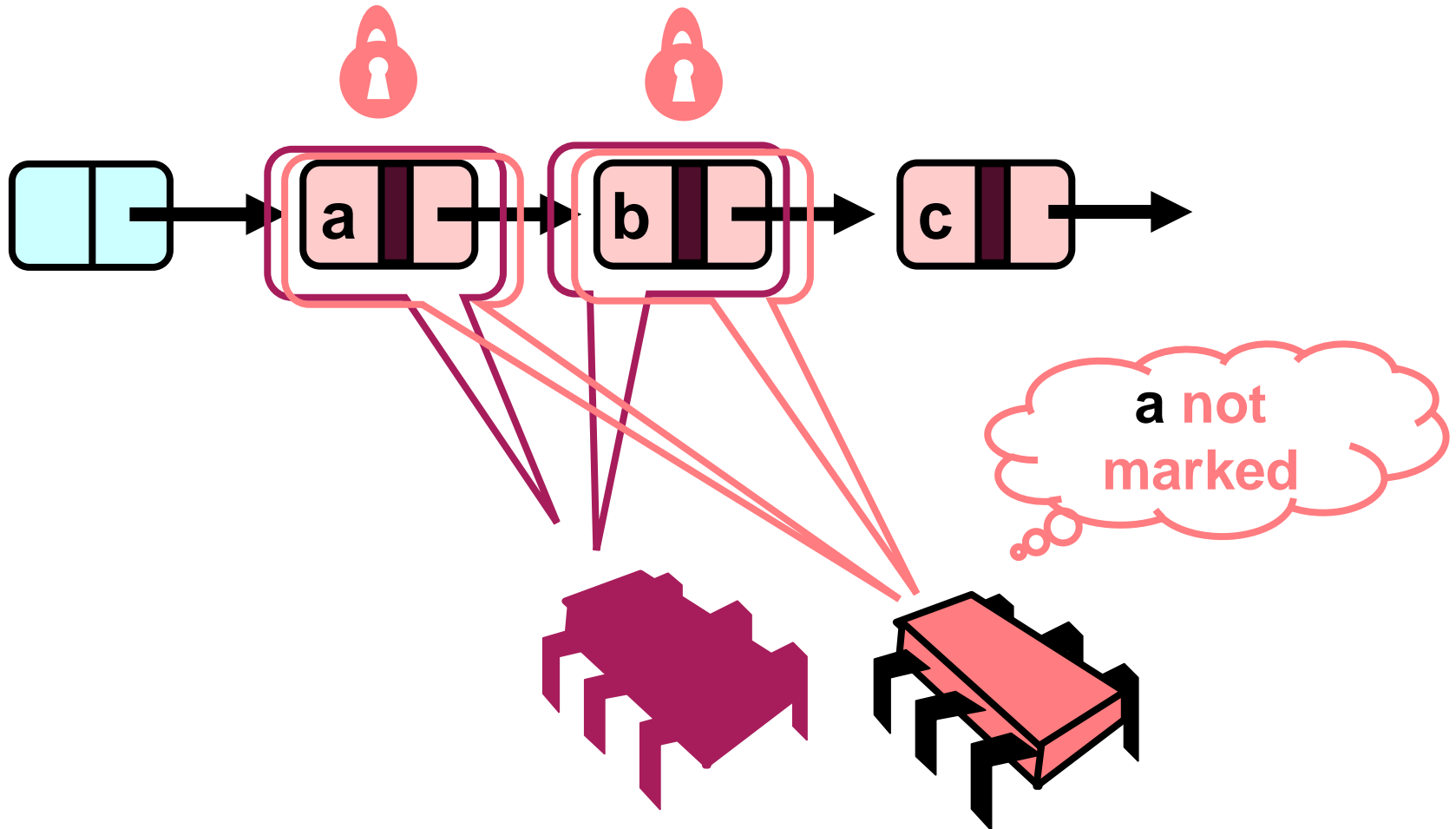




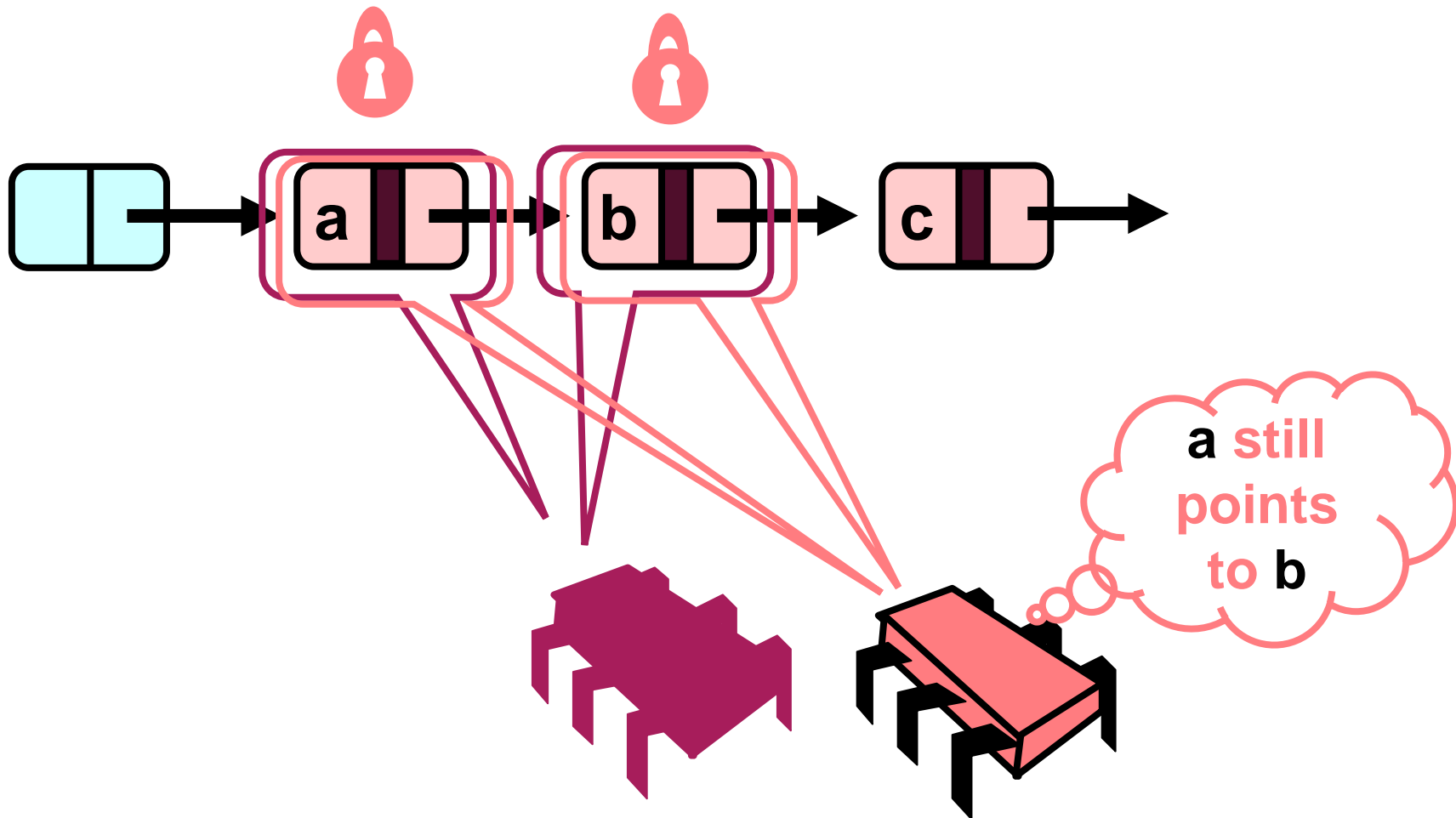
# Business as Usual



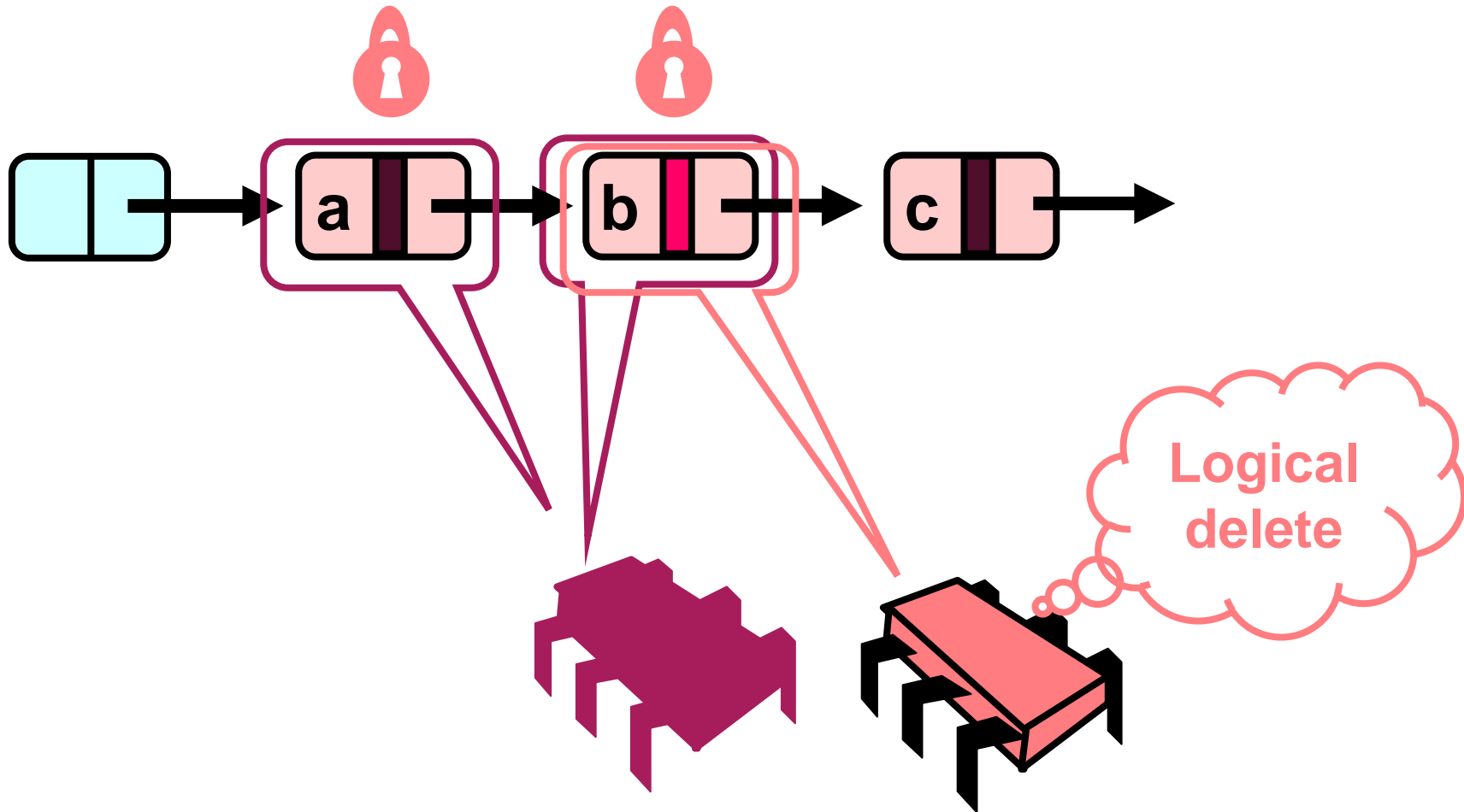
# Business as Usual



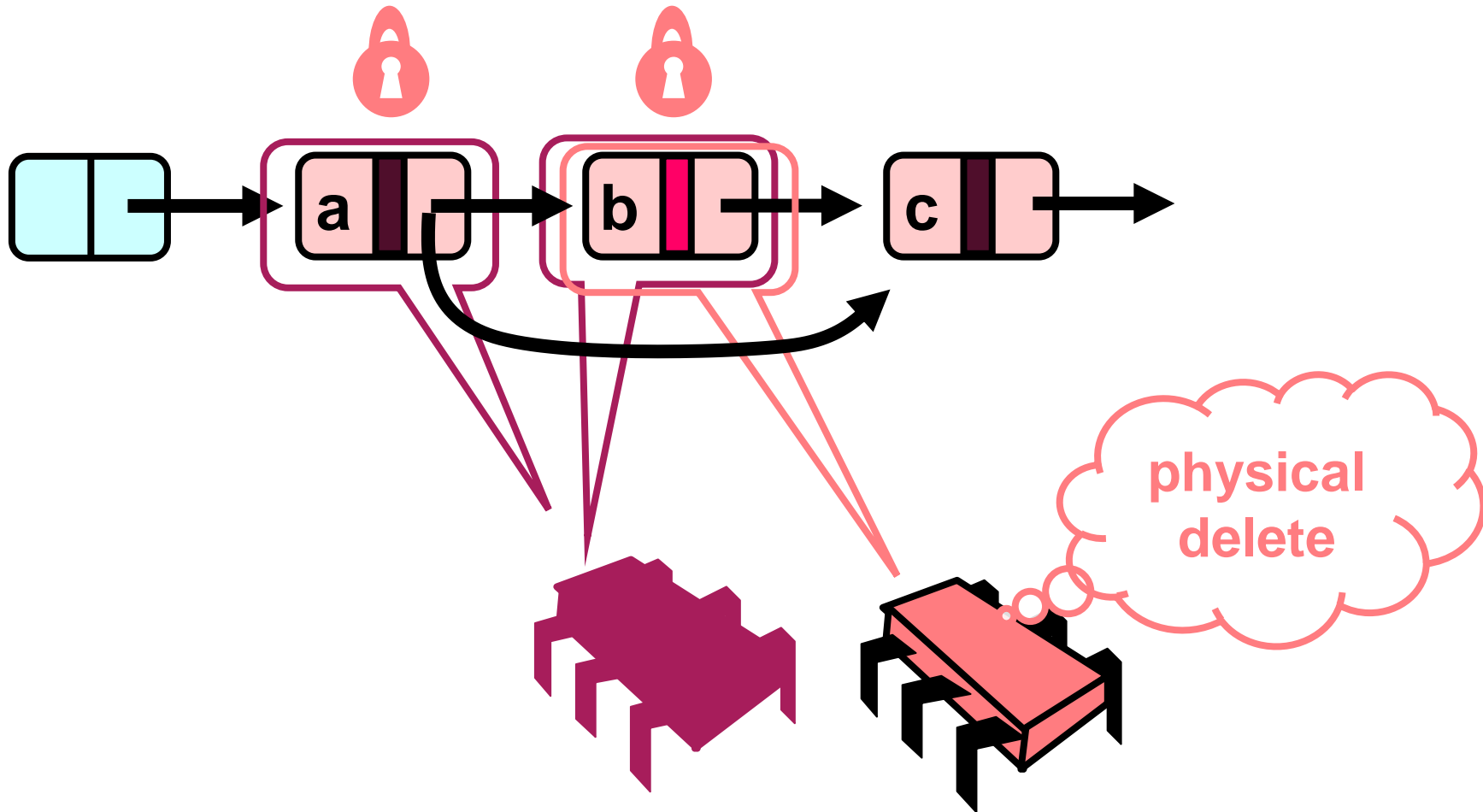
# Business as Usual



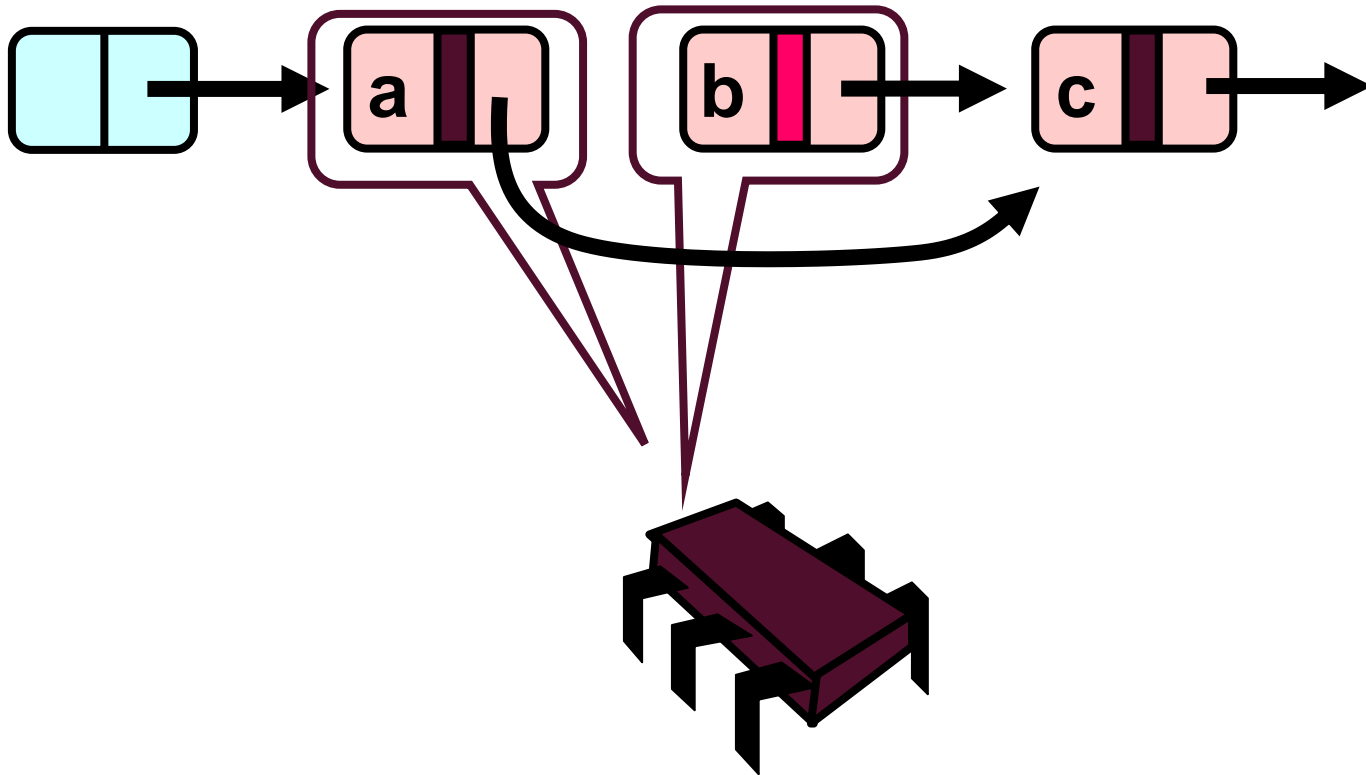
# Business as Usual



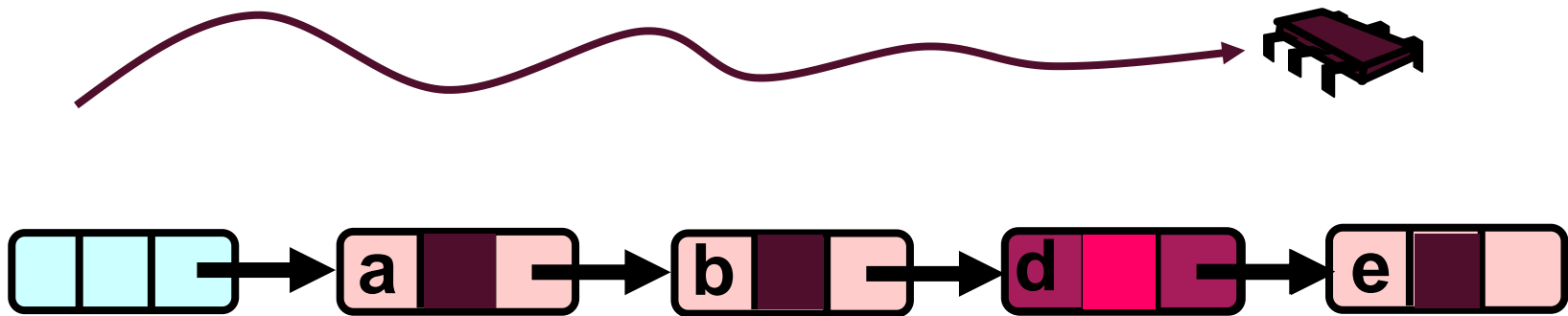
# Business as Usual



# Business as Usual



# Summary: Wait-free Contains



Use Mark bit + list ordering

1. Not marked  $\rightarrow$  in the set
2. Marked or missing  $\rightarrow$  not in the set

Lazy add() and remove() + Wait-free contains()

# Problems with Locks

- **What are the fundamental problems with locks?**
- **Blocking**
  - Threads wait, fault tolerance
  - Especially when things like page faults occur in CR
- **Overheads**
  - Even when not contended
  - Also memory/state overhead
- **Synchronization is tricky**
  - Deadlock, other effects are hard to debug
- **Not easily composable**



# Lock-free Methods

- **No matter what:**

- Guarantee minimal progress

*I.e., some thread will advance*

- Threads may halt at bad times (no CRs! No exclusion!)

*I.e., cannot use locks!*

- Needs other forms of synchronization

*E.g., atomics (discussed before for the implementation of locks)*

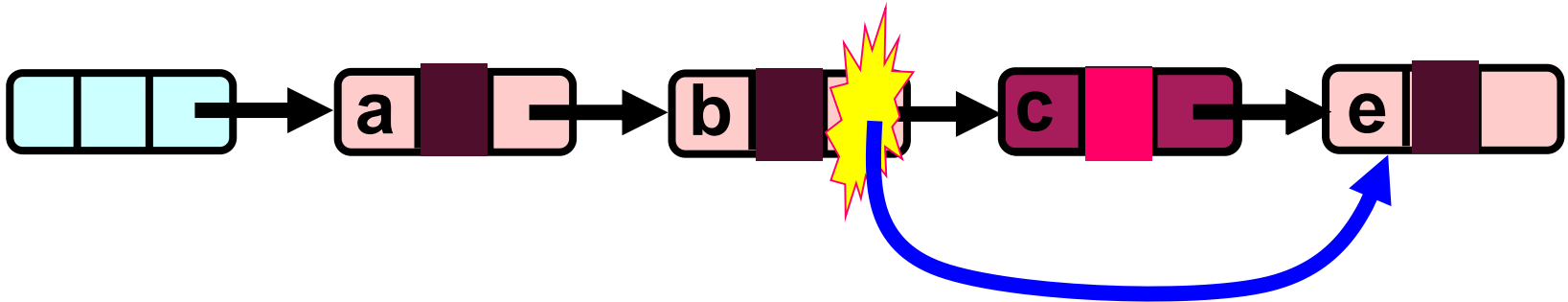
*Techniques are astonishingly similar to guaranteeing mutual exclusion*

# Trick 5: No Locking

- **Make list lock-free**
- **Logical succession**
  - We have wait-free contains
  - Make add() and remove() lock-free!  
*Keep logical vs. physical removal*
- **Simple idea:**
  - Use CAS to verify that pointer is correct before moving it

# Lock-free Lists

(1) Logical Removal



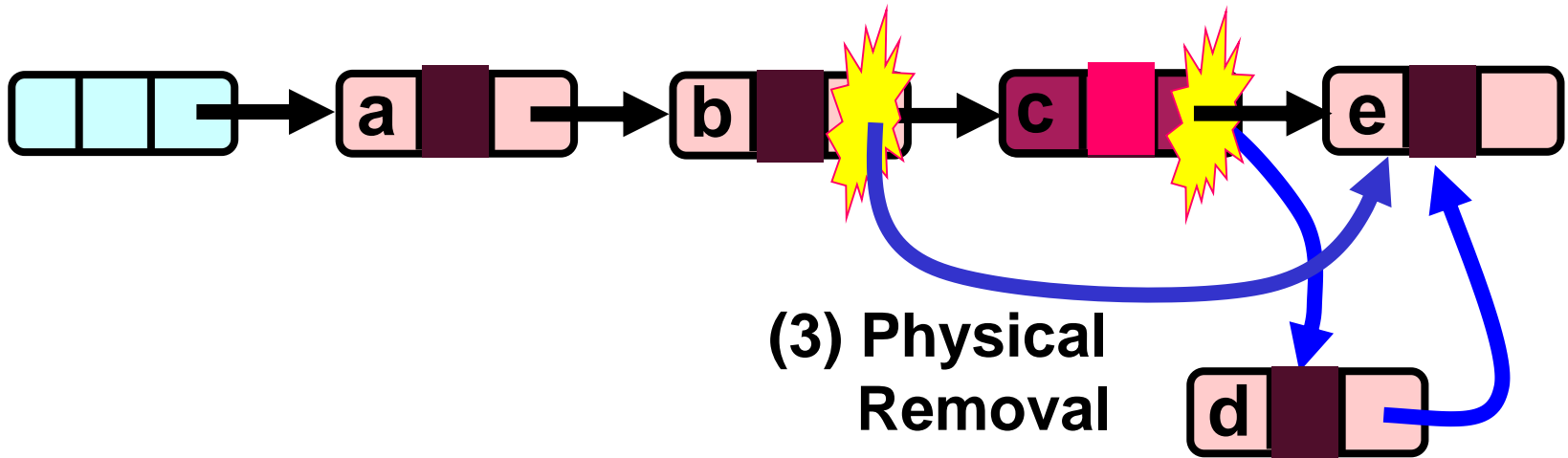
Use CAS to verify pointer is correct

(2) Physical Removal

**Not enough! Why?**

# Problem...

(1) Logical Removal



(3) Physical Removal

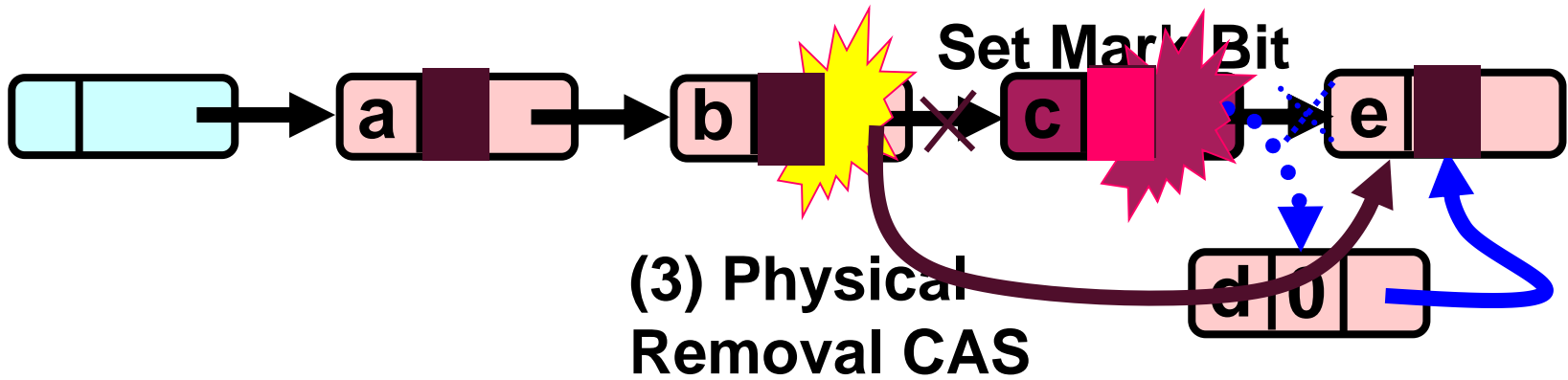
(2) Node added

# The Solution: Combine Mark and Pointer

(1) Logical Removal

=

Set Mark Bit



(2) Fail CAS: Node not added after logical Removal

Mark-Bit and Pointer are CASed together!

# Practical Solution(s)

## ■ Option 1:

- Introduce “atomic markable reference” type
- “Steal” a bit from a pointer
- Rather complex and OS specific ☹️

## ■ Option 2:

- Use Double CAS (or CAS2) 😊  
*CAS of two noncontiguous locations*
- Well, not many machines support it ☹️  
*Any still alive?*

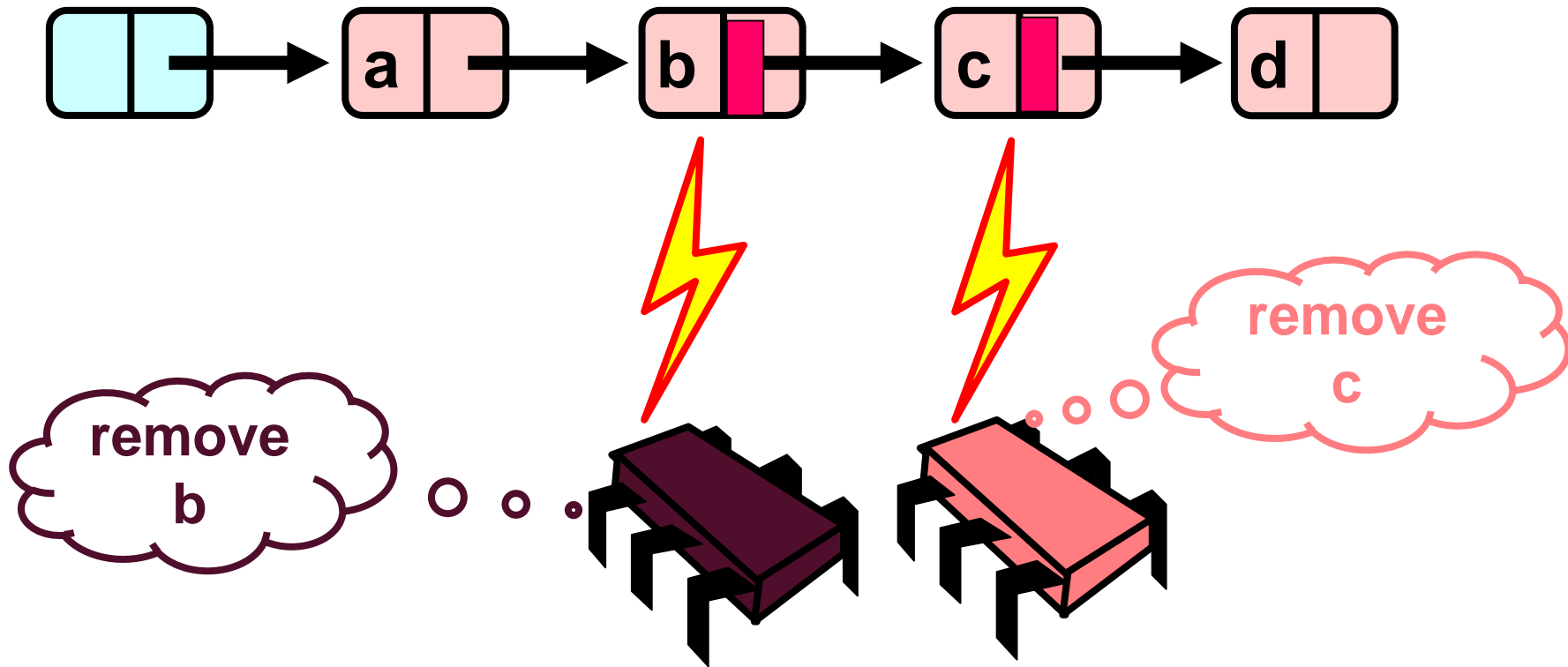
## ■ Option 3:

- Our favorite ISA (x86) offers double-width CAS  
*Contiguous, e.g., lock cmpxchg16b (on 64 bit systems)*

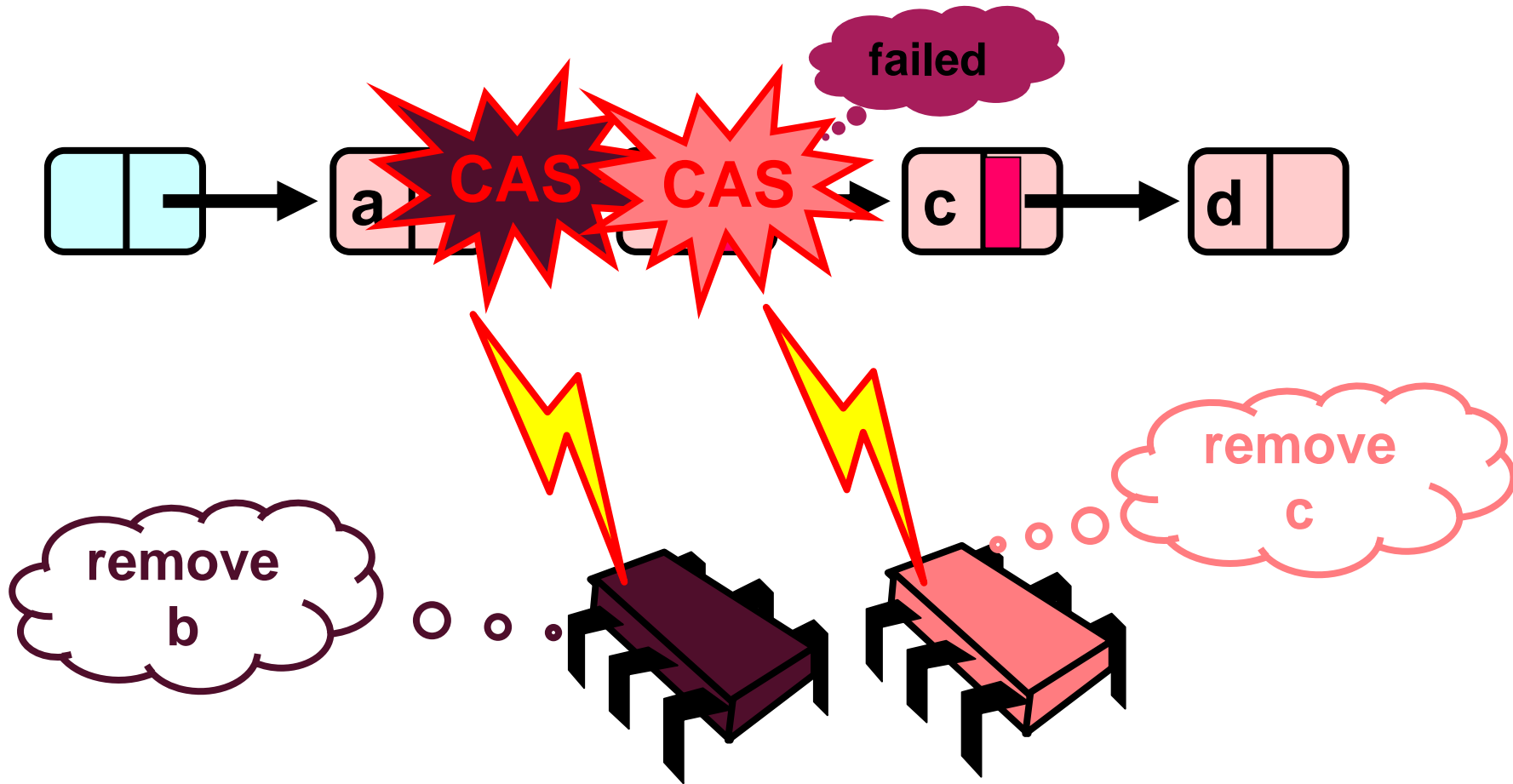
## ■ Option 4:

- TM!  
*E.g., Intel’s TSX (essentially a cmpxchg64b (operates on a cache line))*

# Removing a Node

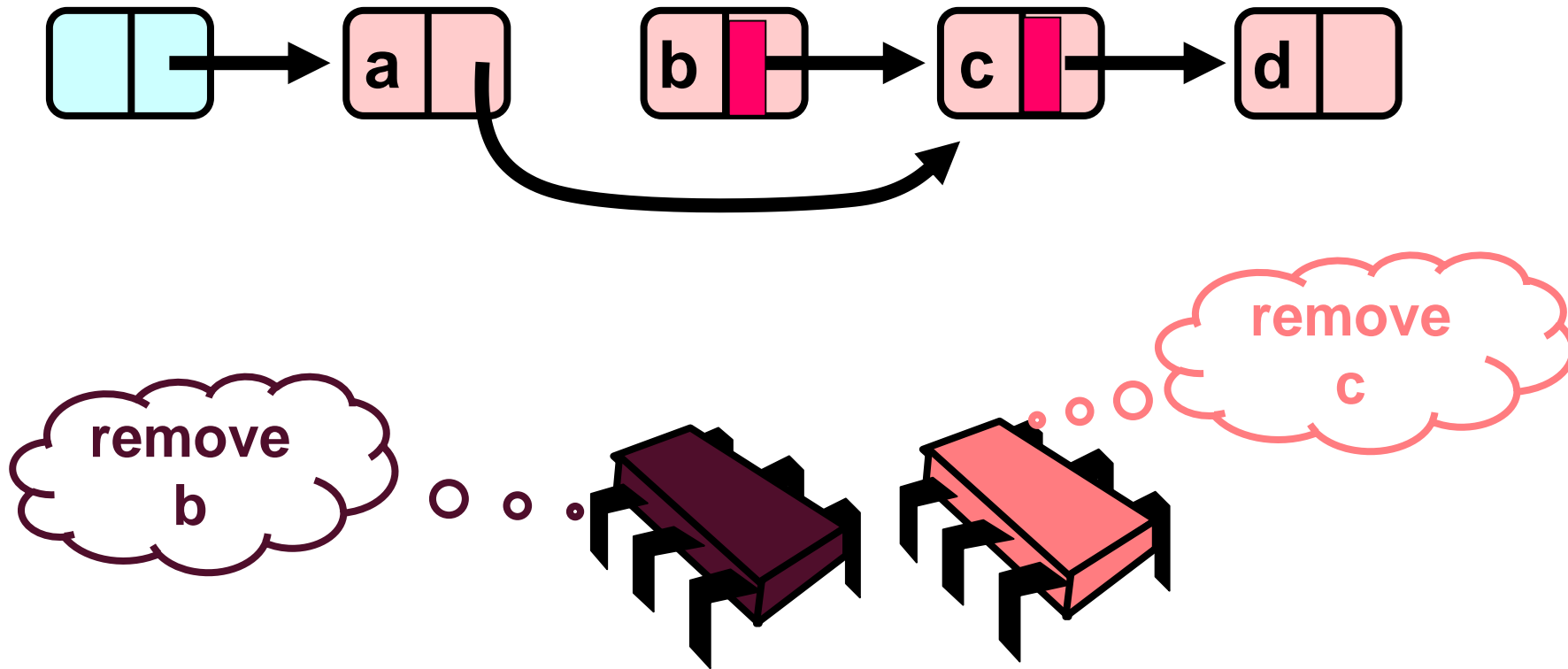


# Removing a Node

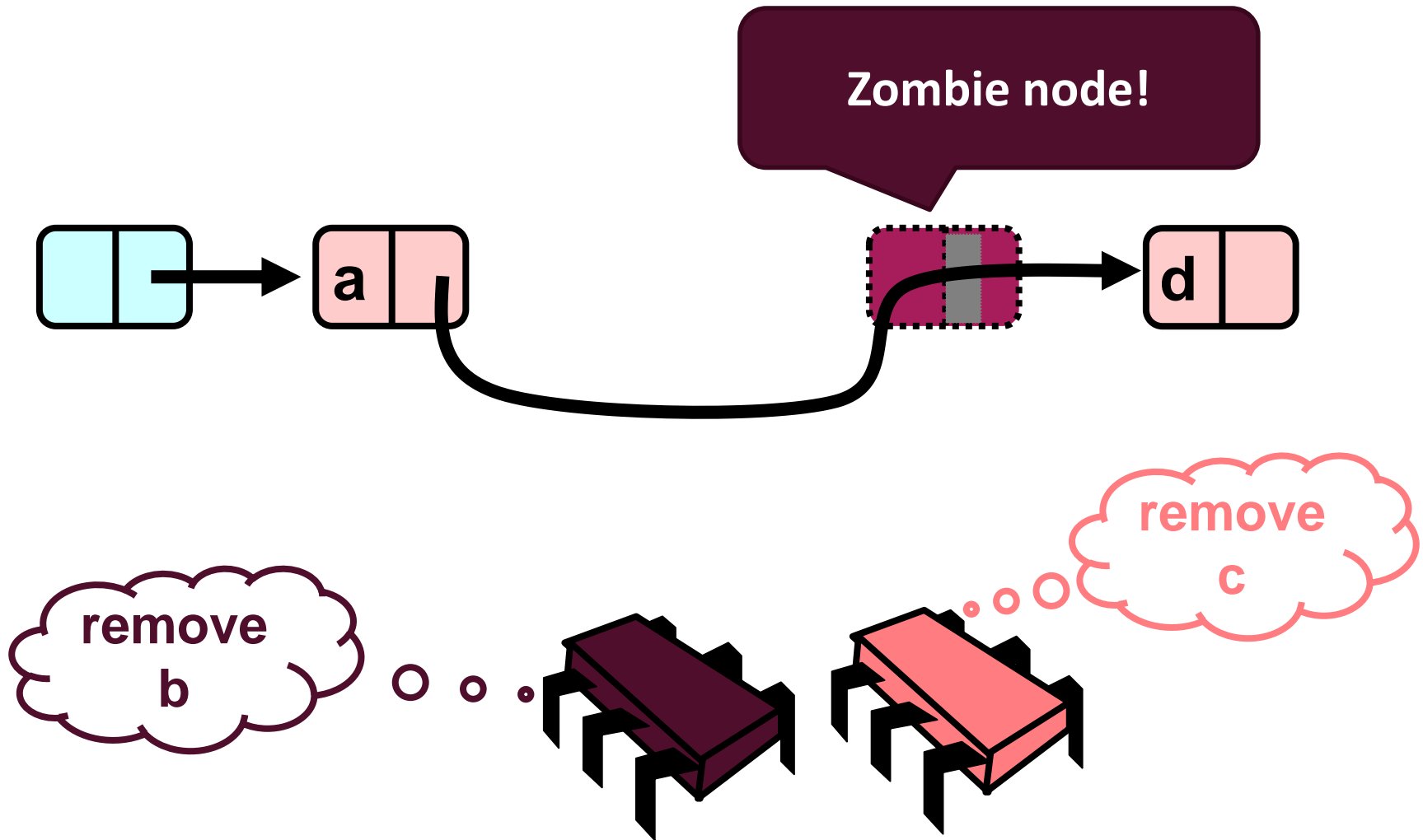




# Removing a Node



# Uh oh – node marked but not removed!



# Dealing With Zombie Nodes

- **Add() and remove() “help to clean up”**
  - Physically remove any marked nodes on their path
  - I.e., if curr is marked: CAS (pred.next, mark) to (curr.next, false) and remove curr
    - If CAS fails, restart from beginning!*
- **“Helping” is often needed in wait-free algs**
- **This fixes all the issues and makes the algorithm correct!**

# Comments

- **Atomically updating two variables (CAS2 etc.) has a non-trivial cost**
- **If CAS fails, routine needs to re-traverse list**
  - Necessary cleanup may lead to unnecessary contention at marked nodes
- **More complex data structures and correctness proofs than for locked versions**
  - But guarantees progress, fault-tolerant and maybe even faster (that really depends)

# More Comments

## ■ Correctness proof techniques

- Establish invariants for initial state and transformations

*E.g., head and tail are never removed, every node in the set has to be reachable from head, ...*

- Proofs are similar to those we discussed for locks

*Very much the same techniques (just trickier)*

*Using sequential consistency (or consistency model of your choice 😊)*

*Lock-free gets somewhat tricky*

## ■ Source-codes can be found in Chapter 9 of “The Art of Multiprocessor Programming”

# Lock-free and wait-free

## ■ A lock-free method

- guarantees that infinitely often **some** method call finishes in a finite number of steps

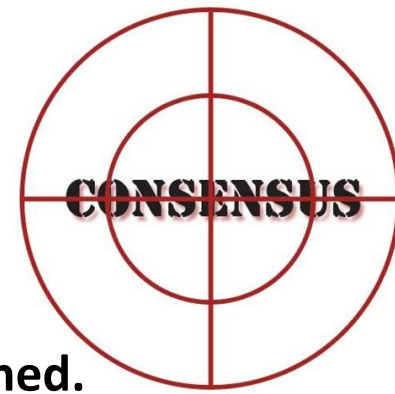
## ■ A wait-free method

- guarantees that **each** method call finishes in a finite number of steps (implies lock-free)
- Was our lock-free list also wait-free?

## ■ Synchronization instructions are not equally powerful!

- Indeed, they form an infinite hierarchy; no instruction (primitive) in level  $x$  can be used for lock-/wait-free implementations of primitives in level  $z > x$ .

# Concept: Consensus Number



- **Each level of the hierarchy has a “consensus number” assigned.**
  - Is the maximum number of threads for which primitives in level  $x$  can solve the consensus problem
- **The consensus problem:**
  - Has single function:  $\text{decide}(v)$
  - Each thread calls it at most once, the function returns a value that meets two conditions:
    - consistency: all threads get the same value*
    - valid: the value is some thread's input*
  - Simplification: binary consensus (inputs in  $\{0,1\}$ )

# Understanding Consensus

- **Can a particular class solve n-thread consensus wait-free?**
  - A class C solves n-thread consensus if there exists a consensus protocol using **any number** of objects of class C and **any number** of atomic registers
  - The protocol has to be wait-free (bounded number of steps per thread)
  - The consensus number of a class C is the largest n for which that class solves n-thread consensus (may be infinite)
  - Assume we have a class D whose objects can be constructed from objects out of class C. If class C has consensus number n, what does class D have?



# Starting simple ...

- **Binary consensus with two threads (A, B)!**
  - Each thread moves until it decides on a value
  - May update shared objects
  - Protocol state = state of threads + state of shared objects
  - Initial state = state before any thread moved
  - Final state = state after all threads finished
  - States form a tree, wait-free property guarantees a finite tree
    - Example with two threads and two moves each!*

# Atomic Registers

- **Theorem [Herlihy'91]: Atomic registers have consensus number one**
  - Really?
- **Proof outline:**
  - Assume arbitrary consensus protocol, thread A, B
  - Run until it reaches critical state where next action determines outcome (show that it must have a critical state first)
  - Show all options using atomic registers and show that they cannot be used to determine one outcome for all possible executions!
    - 1) *Any thread reads (other thread runs solo until end)*
    - 2) *Threads write to different registers (order doesn't matter)*
    - 3) *Threads write to same register (solo thread can start after each write)*

# Atomic Registers

- **Theorem [Herlihy'91]: Atomic registers have consensus number one**
- **Corollary: It is impossible to construct a wait-free implementation of any object with consensus number of  $>1$  using atomic registers**
  - “perhaps one of the most striking impossibility results in Computer Science” (Herlihy, Shavit)
  - → We need hardware atomics or TM!

- **Proof technique borrowed from:**

[Impossibility of distributed consensus with one faulty process](#)

MJ Fischer, NA Lynch, [MS Paterson](#) - Journal of the ACM (JACM), 1985 - dl.acm.org

Abstract The **consensus** problem involves an asynchronous system of processes, some of which may be unreliable. The problem is for the reliable processes to agree on a binary value. In this paper, it is shown that every protocol for this problem has the possibility of ...

[Cited by 3180](#) [Related articles](#) [All 164 versions](#)

- **Very influential paper, always worth a read!**
  - Nicely shows proof techniques that are central to parallel and distributed computing!

# Other Atomic Operations

- **Simple RMW operations (Test&Set, Fetch&Op, Swap, basically all functions where the op commutes or overwrites) have consensus number 2!**
  - Similar proof technique (bivalence argument)
- **CAS and TM have consensus number  $\infty$** 
  - Constructive proof!

# Compare and Set/Swap Consensus

```
const int first = -1
volatile int thread = -1;
int proposed[n];

int decide(v) {
    proposed[tid] = v;
    if(CAS(thread, first, tid))
        return v; // I won!
    else
        return proposed[thread]; // thread won
}
```



- **CAS provides an infinite consensus number**
  - Machines providing CAS are **asynchronous** computation equivalents of the Turing Machine
  - I.e., any concurrent object can be implemented in a wait-free manner (not necessarily fast!)

# Now you know everything 😊

- **Not really ... ;-)**

- We'll argue about **performance** now!

- **But you have all the tools for:**

- Efficient locks
- Efficient lock-based algorithms
- Efficient lock-free algorithms (or even wait-free)
- Reasoning about parallelism!

- **What now?**

- A different class of problems

*Impact on wait-free/lock-free on actual performance is not well understood*

- Relevant to HPC, applies to shared and distributed memory

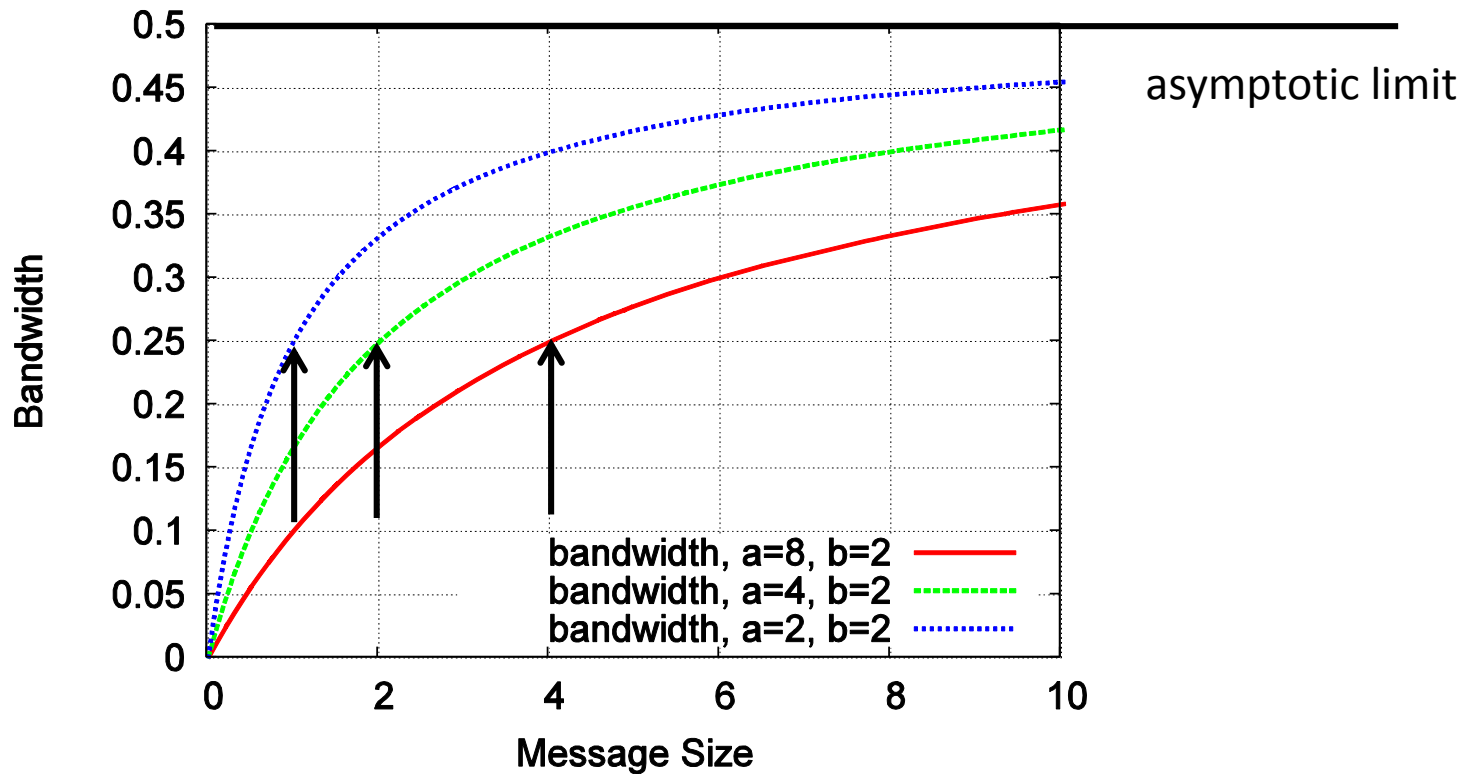
→ *Group communications*

# Remember: A Simple Model for Communication

- **Transfer time  $T(s) = \alpha + \beta s$** 
  - $\alpha$  = startup time (latency)
  - $\beta$  = cost per byte (bandwidth =  $1/\beta$ )
- **As  $s$  increases, bandwidth approaches  $1/\beta$  asymptotically**
  - Convergence rate depends on  $\alpha$
  - $s_{1/2} = \alpha/\beta$
- **Assuming no pipelining (new messages can only be issued from a process after all arrived)**

# Bandwidth vs. Latency

- $s_{1/2} = \alpha/\beta$  often used to distinguish bandwidth- and latency-bound messages
  - $s_{1/2}$  is in the order of kilobytes on real systems





# Quick Example

- **Simplest linear broadcast**
  - One process has a data item to be distributed to all processes
- **Broadcasting  $s$  bytes among  $P$  processes:**
  - $T(s) = (P-1) * (\alpha + \beta s) = \mathcal{O}(P)$
- **Class question: Do you know a faster method to accomplish the same?**

# k-ary Tree Broadcast

- Origin process is the root of the tree, passes messages to k neighbors which pass them on

- k=2 -> binary tree

- **Class Question: What is the broadcast time in the simple latency/bandwidth model?**

- $T(s) \approx \lceil \log_k(P) \rceil \cdot k \cdot (\alpha + \beta \cdot s) = \mathcal{O}(\log(P))$  (for fixed k)

- **Class Question: What is the optimal k?**

- $0 = \frac{\ln(P) \cdot k}{\ln(k)} \frac{d}{dk} = \frac{\ln(P) \ln(k) - \ln(P)}{\ln^2(k)} \rightarrow k = e = 2.71\dots$

- Independent of P,  $\alpha$ ,  $\beta$ s? Really?

# Faster Trees?

- **Class Question: Can we broadcast faster than in a ternary tree?**

- Yes because each respective root is idle after sending three messages!
- Those roots could keep sending!
- Result is a k-nomial tree

*For  $k=2$ , it's a binomial tree*

- **Class Question: What about the runtime?**

- $$T(s) = \lceil \log_k(P) \rceil \cdot (k - 1) \cdot (\alpha + \beta \cdot s) = \mathcal{O}(\log(P))$$

- **Class Question: What is the optimal k here?**

- $T(s) \frac{d}{dk}$  is monotonically increasing for  $k>1$ , thus  $k_{\text{opt}}=2$

- **Class Question: Can we broadcast faster than in a k-nomial tree?**

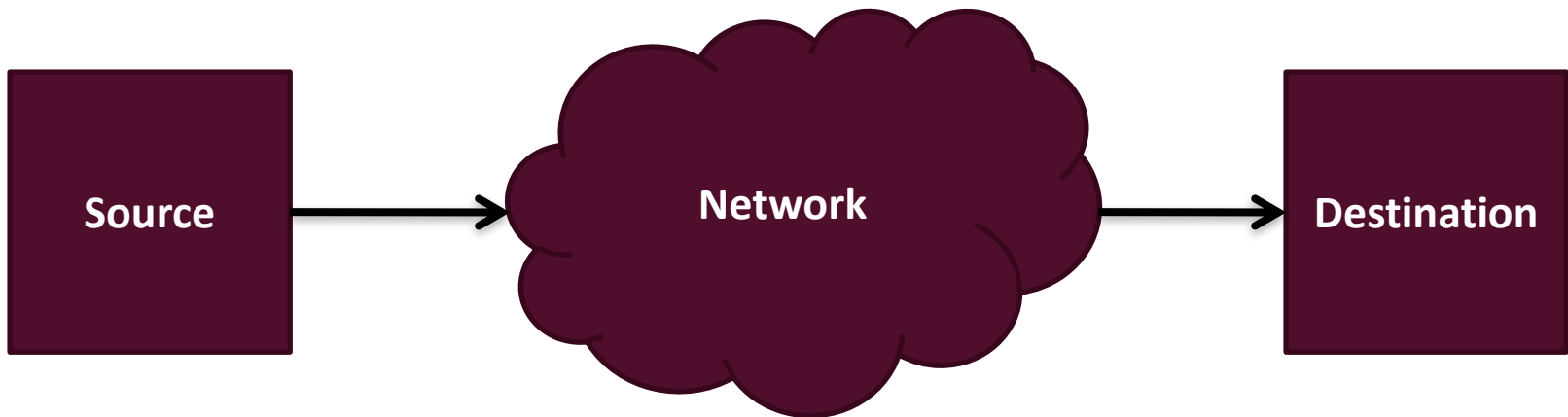
- $\mathcal{O}(\log(P))$  is asymptotically optimal for  $s=1$ !
- But what about large  $s$ ?

# Open Problems

- **Look for optimal parallel algorithms (even in simple models!)**
  - And then check the more realistic models
  - Useful optimization targets are MPI collective operations  
*Broadcast/Reduce, Scatter/Gather, Alltoall, Allreduce, Allgather, Scan/Exscan, ...*
  - Implementations of those (check current MPI libraries 😊)
  - Useful also in scientific computations  
*Barnes Hut, linear algebra, FFT, ...*
- **Lots of work to do!**
  - Contact me for thesis ideas (or check SPCL) if you like this topic
  - Usually involve optimization (ILP/LP) and clever algorithms (algebra) combined with practical experiments on large-scale machines (10,000+ processors)

# HPC Networking Basics

- **Familiar (non-HPC) network: Internet TCP/IP**
  - Common model:



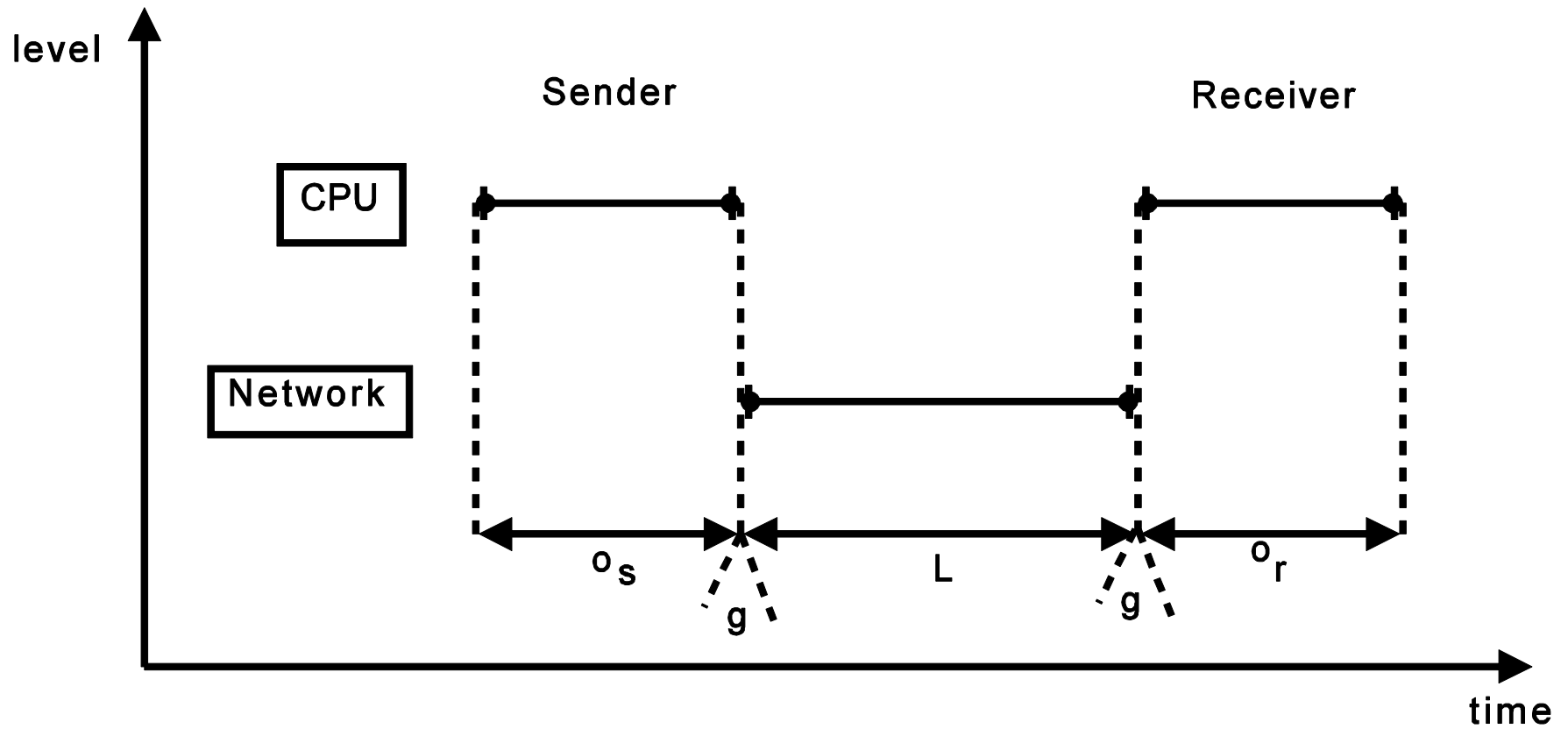
- **Class Question: What parameters are needed to model the performance (including pipelining)?**
  - Latency, Bandwidth, Injection Rate, Host Overhead

# The LogP Model

- **Defined by four parameters:**

- L: an upper bound on the latency, or delay, incurred in communicating a message containing a word (or small number of words) from its source module to its target module.
- o: the overhead, defined as the length of time that a processor is engaged in the transmission or reception of each message; during this time, the processor cannot perform other operations.
- g: the gap, defined as the minimum time interval between consecutive message transmissions or consecutive message receptions at a processor. The reciprocal of g corresponds to the available per-processor communication bandwidth.
- P: the number of processor/memory modules. We assume unit time for local operations and call it a cycle.

# The LogP Model



# Simple Examples

- **Sending a single message**

- $T = 2o + L$

- **Ping-Pong Round-Trip**

- $T_{RTT} = 4o + 2L$

- **Transmitting  $n$  messages**

- $T(n) = L + (n-1) * \max(g, o) + 2o$



# Simplifications

- **o is bigger than g on some machines**
  - g can be ignored (eliminates max() terms)
  - be careful with multicore!
- **Offloading networks might have very low o**
  - Can be ignored (not yet but hopefully soon)
- **L might be ignored for long message streams**
  - If they are pipelined
- **Account g also for the first message**
  - Eliminates “-1”

# Benefits over Latency/Bandwidth Model

- **Models pipelining**
  - L/g messages can be “in flight”
  - Captures state of the art (cf. TCP windows)
- **Models computation/communication overlap**
  - Asynchronous algorithms
- **Models endpoint congestion/overload**
  - Benefits balanced algorithms

# Example: Broadcasts

- **Class Question: What is the LogP running time for a linear broadcast of a single packet?**
  - $T_{lin} = L + (P-2) * \max(o,g) + 2o$
- **Class Question: Approximate the LogP runtime for a binary-tree broadcast of a single packet?**
  - $T_{bin} \leq \log_2 P * (L + \max(o,g) + 2o)$
- **Class Question: Approximate the LogP runtime for an k-ary-tree broadcast of a single packet?**
  - $T_{k-n} \leq \log_k P * (L + (k-1)\max(o,g) + 2o)$

# Example: Broadcasts

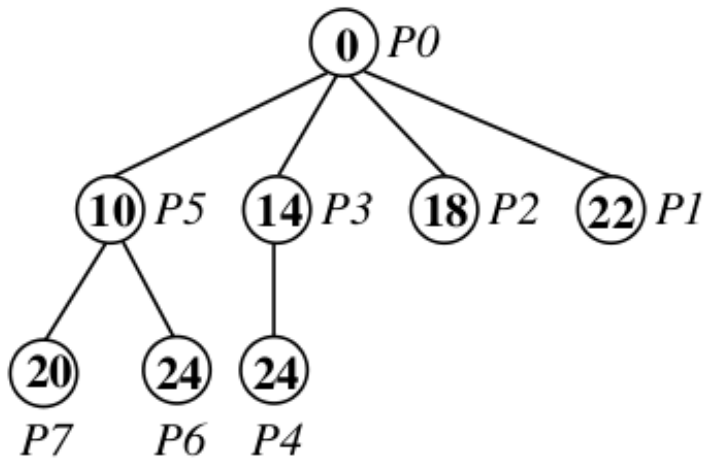
- **Class Question: Approximate the LogP runtime for a binomial tree broadcast of a single packet (assume  $L > g!$ )?**
  - $T_{\text{bin}} \leq \log_2 P * (L + 2o)$
- **Class Question: Approximate the LogP runtime for a k-nomial tree broadcast of a single packet?**
  - $T_{k-n} \leq \log_k P * (L + (k-2)\max(o,g) + 2o)$
- **Class Question: What is the optimal k (assume  $o > g$ )?**
  - Derive by k:  $0 = o * \ln(k_{\text{opt}}) - L/k_{\text{opt}} + o$  (solve numerically)  
*For larger L, k grows and for larger o, k shrinks*
  - Models pipelining capability better than simple model!

# Example: Broadcasts

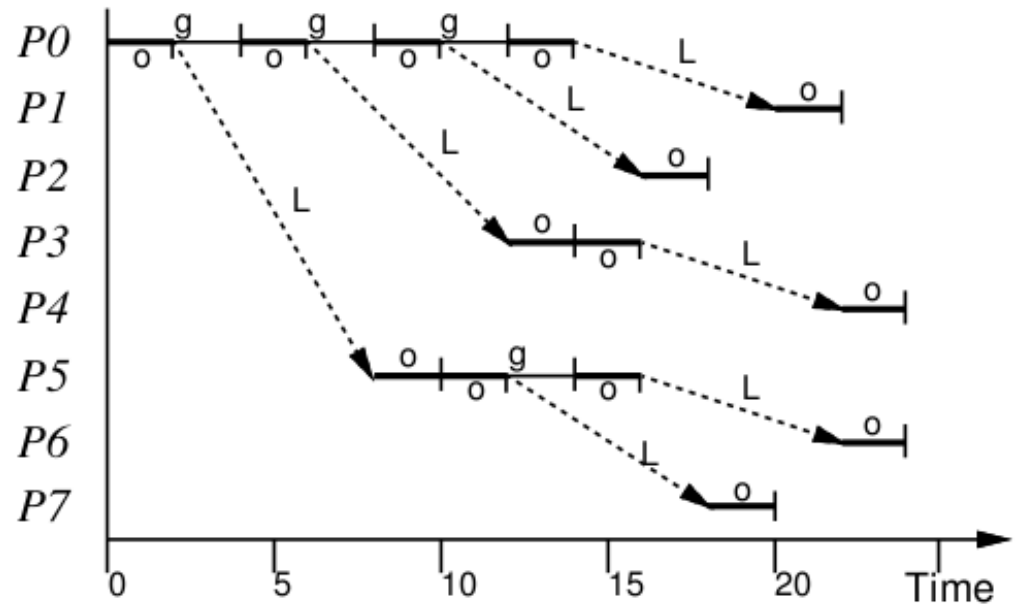
- **Class Question: Can we do better than  $k_{\text{opt}}$ -ary binomial broadcast?**
  - Problem: fixed  $k$  in all stages might not be optimal
  - We can construct a schedule for the optimal broadcast in practical settings
  - First proposed by Karp et al. in “Optimal Broadcast and Summation in the LogP Model”

# Example: Optimal Broadcast

- **Broadcast to P-1 processes**
  - Each process who received the value sends it on; each process receives exactly once



$P=8, L=6, g=4, o=2$



# Optimal Broadcast Runtime

- This determines the maximum number of PEs ( $P(t)$ ) that can be reached in time  $t$
- $P(t)$  can be computed with a generalized Fibonacci recurrence (assuming  $o > g$ ):

$$P(t) = \begin{cases} 1 & : t < 2o + L \\ P(t - o) + P(t - L - 2o) & : \text{otherwise.} \end{cases} \quad (1)$$

- Which can be bounded by (see [1]):  $2^{\lfloor \frac{t}{L+2o} \rfloor} \leq P(t) \leq 2^{\lfloor \frac{t}{o} \rfloor}$ 
  - A closed solution is an interesting open problem!

# The Bigger Picture

- **We learned how to program shared memory systems**
  - Coherency & memory models & linearizability
  - Locks as examples for reasoning about correctness and performance
  - List-based sets as examples for lock-free and wait-free algorithms
  - Consensus number
- **We learned about general performance properties and parallelism**
  - Amdahl's and Gustafson's laws
  - Little's law, Work-span, ...
  - Balance principles & scheduling
- **We learned how to perform model-based optimizations**
  - Distributed memory broadcast example with two models
- **What next? MPI? OpenMP? UPC?**
  - Next-generation machines “merge” shared and distributed memory concepts → Partitioned Global Address Space (PGAS)