Operating Systems and Networks

Network Lecture 3: Link Layer (1)

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Pending Issues

- Dis-connect of homework from lecture
- Earlier posting of lecture slides

Where we are in the Course

Moving on to the Link Layer!

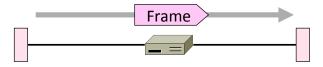


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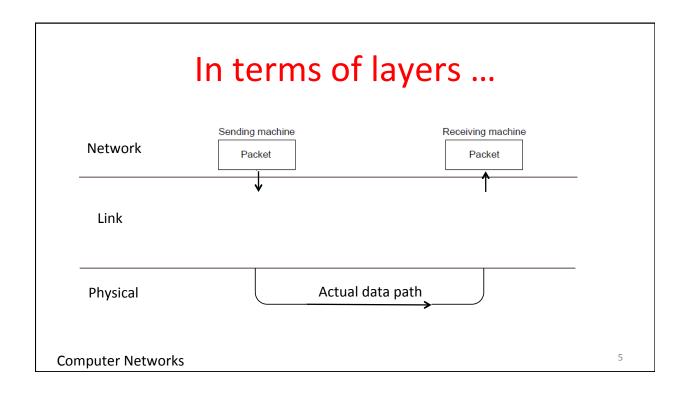
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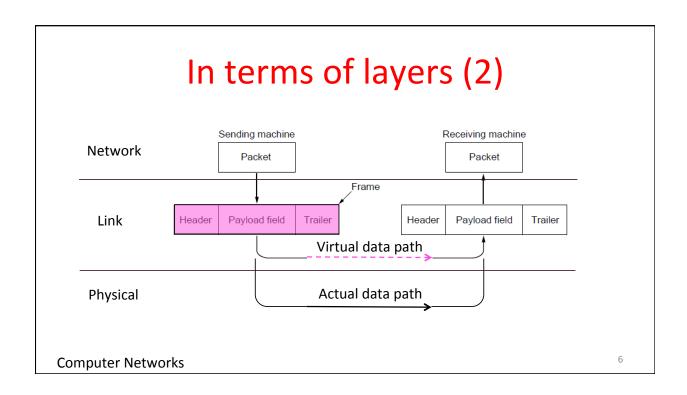
Scope of the Link Layer

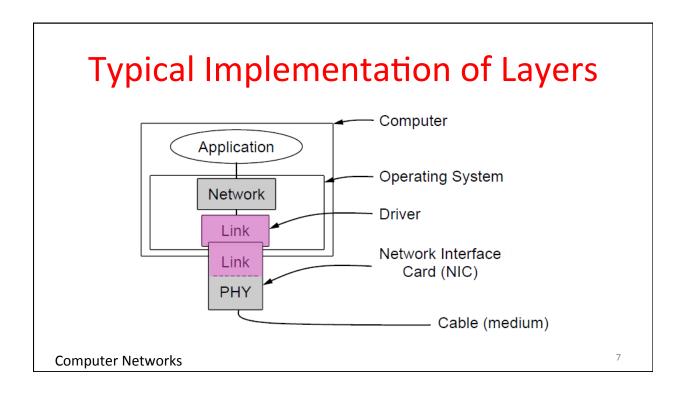
- Concerns how to transfer messages over one or more connected links
 - Messages are frames, of limited size
 - Builds on the physical layer

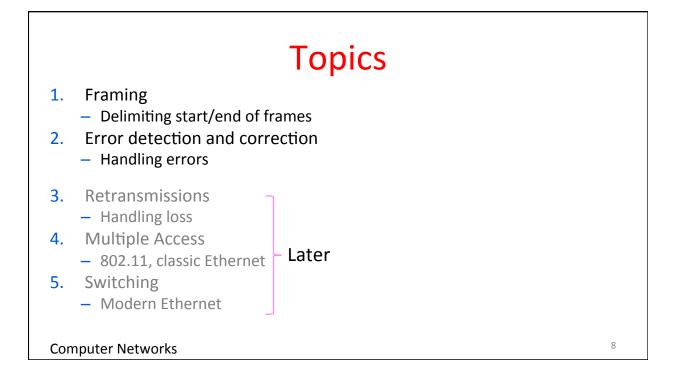


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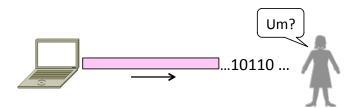






Framing (§3.1.2)

• The Physical layer gives us a stream of bits. How do we interpret it as a sequence of frames?



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Framing Methods

- We'll look at:
 - Byte count (motivation)
 - Byte stuffing
 - Bit stuffing
- In practice, the physical layer often helps to identify frame boundaries
 - E.g., Ethernet, 802.11

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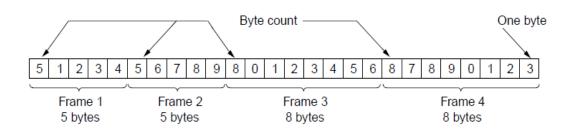
Byte Count

- First try:
 - Let's start each frame with a length field!
 - It's simple, and hopefully good enough ...

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11

Byte Count (2)

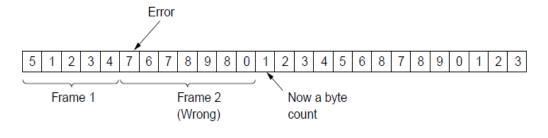


How well do you think it works?

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Byte Count (3)

- Difficult to re-synchronize after framing error
 - Want a way to scan for a start of frame



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13

Byte Stuffing

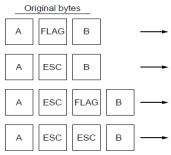
- Better idea:
 - Have a special flag byte value that means start/end of frame
 - Replace ("stuff") the flag inside the frame with an escape code
 - Complication: have to escape the escape code too!



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Byte Stuffing (2)

- Rules:
 - Replace each FLAG in data with ESC FLAG
 - Replace each ESC in data with ESC ESC

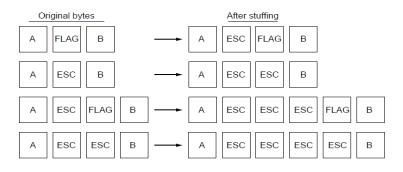


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15

Byte Stuffing (3)

Now any unescaped FLAG is the start/end of a frame



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Bit Stuffing

- Can stuff at the bit level too
 - Call a flag six consecutive 1s
 - On transmit, after five 1s in the data, insert a 0
 - On receive, a 0 after five 1s is deleted

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17

Bit Stuffing (2)

Example:

Transmitted bits with stuffing

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Bit Stuffing (3)

So how does it compare with byte stuffing?

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10

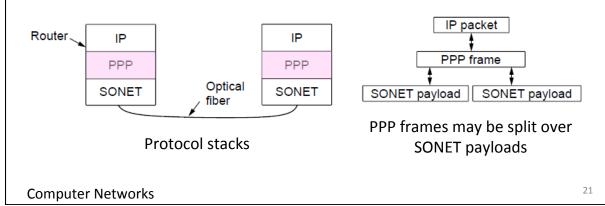
Link Example: PPP over SONET

- PPP is Point-to-Point Protocol
- Widely used for link framing
 - E.g., it is used to frame IP packets that are sent over SONET optical links

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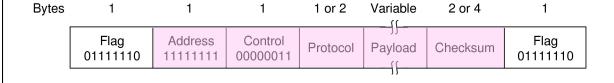
Link Example: PPP over SONET (2)

 Think of SONET as a bit stream, and PPP as the framing that carries an IP packet over the link



Link Example: PPP over SONET (3)

- Framing uses byte stuffing
 - FLAG is 0x7E and ESC is 0x7D



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Link Example: PPP over SONET (4)

- Byte stuffing method:
 - To stuff (unstuff) a byte, add (remove) ESC (0x7D), and XOR byte with 0x20
 - Removes FLAG from the contents of the frame

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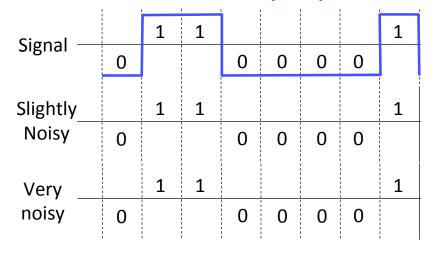
2.

Error Coding Overview (§3.2)

- Some bits will be received in error due to noise. What can we do?
 - Detect errors with codes
 - Correct errors with codes
 - Retransmit lost frames Later
- Reliability is a concern that cuts across the layers we'll see it again

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Problem – Noise may flip received bits



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Approach – Add Redundancy

- Error detection codes
 - Add <u>check bits</u> to the message bits to let some errors be detected
- Error correction codes
 - Add more check bits to let some errors be corrected
- Key issue is now to structure the code to detect many errors with few check bits and modest computation

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Motivating Example

- A simple code to handle errors:
 - Send two copies! Error if different.
- How good is this code?
 - How many errors can it detect/correct?
 - How many errors will make it fail?

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Motivating Example (2)

- We want to handle more errors with less overhead
 - Will look at better codes; they are applied mathematics
 - But, they can't handle all errors
 - And they focus on accidental errors (will look at secure hashes later)

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Using Error Codes

 Codeword consists of D data plus R check bits (=systematic block code)

Data bits Check bits

D R=fn(D) →

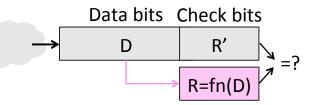
- Sender:
 - Compute R check bits based on the D data bits; send the codeword of D+R bits

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29

Using Error Codes (2)

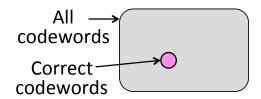
- Receiver:
 - Receive D+R bits with unknown errors
 - Recompute R check bits based on the D data bits; error if R doesn't match R'



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Intuition for Error Codes

For D data bits, R check bits:



 Randomly chosen codeword is unlikely to be correct; overhead is low

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3:

R.W. Hamming (1915-1998)

- Much early work on codes:
 - "Error Detecting and Error Correcting Codes", BSTJ, 1950
- See also:
 - "You and Your Research", 1986



Source: IEEE GHN, © 2009 IEEE

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Hamming Distance

- Distance is the number of bit flips needed to change D+R₁ to D+R₂
- Hamming distance of a code is the minimum distance between any pair of codewords

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33

Hamming Distance (2)

- Error detection:
 - For a code of distance d+1, up to d errors will always be detected

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Hamming Distance (3)

- Error correction:
 - For a code of distance 2d+1, up to d errors can always be corrected by mapping to the closest codeword

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Error Detection (§3.2.2)

- Some bits may be received in error due to noise. How do we detect this?
 - Parity
 - Checksums
 - CRCs
- Detection will let us fix the error, for example, by retransmission (later).

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Simple Error Detection – Parity Bit

- Take D data bits, add 1 check bit that is the sum of the D bits
 - Sum is modulo 2 or XOR

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Parity Bit (2)

- How well does parity work?
 - What is the distance of the code?
 - How many errors will it detect/correct?
- What about larger errors?

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Checksums

- Idea: sum up data in N-bit words
 - Widely used in, e.g., TCP/IP/UDP

1500 bytes 16 bits

Stronger protection than parity

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39

Internet Checksum

- Sum is defined in 1s complement arithmetic (must add back carries)
 - And it's the negative sum
- "The checksum field is the 16 bit one's complement of the one's complement sum of all 16 bit words ..." – RFC 791

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Internet Checksum (2)

Sending:

1. Arrange data in 16-bit words

- 2. Put zero in checksum position, add
- 3. Add any carryover back to get 16 bit
- 4. Negate (complement) to get sum

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41

Internet Checksum (3)

Sending:

1. Arrange data in 16-bit words

2. Put zero in checksum position, add

+(0000)

3. Add any carryover back to get 16 bits

2ddf0 ddf0

ddf2

4. Negate (complement) to get sum

220d

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Internet Checksum (4)

Receiving:

1. Arrange data in 16-bit words

2. Checksum will be non-zero, add

0001
f203
f4f5
f6f7

- 3. Add any carryover back to get 16 bits
- 4. Negate the result and check it is 0

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Internet Checksum (5)

Receiving:

1. Arrange data in 16-bit words

2. Checksum will be non-zero, add

3. Add any carryover back to get 16 bits

4. Negate the result and check it is 0

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Internet Checksum (6)

- How well does the checksum work?
 - What is the distance of the code?
 - How many errors will it detect/correct?
- What about larger errors?

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45

Cyclic Redundancy Check (CRC)

- Even stronger protection
 - Given n data bits, generate k check bits such that the n+k bits are evenly divisible by a generator C
- Example with numbers:
 - n = 302, k = one digit, C = 3

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CRCs (3)

- Send Procedure:
- 1. Extend the n data bits with k zeros
- 2. Divide by the generator value C
- 3. Keep remainder, ignore quotient
- 4. Adjust k check bits by remainder
- Receive Procedure:
- 1. Divide and check for zero remainder

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47

CRCs (4)

Data bits: 10011 1 1 0 1 0 1 1 1 1 1

1101011111

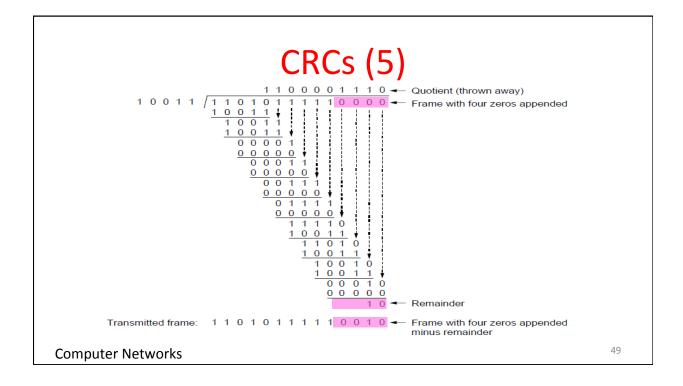
Check bits:

$$C(x)=x^4+x^1+1$$

$$C = 10011$$

$$k = 4$$

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CRCs (6)

- Protection depend on generator
 - Standard CRC-32 is 1 0000 0100 1100 0001 0001 1101 1011 0111
- Properties:
 - HD=4, detects up to triple bit errors
 - Also odd number of errors
 - And bursts of up to k bits in error
 - Not vulnerable to systematic errors like checksums

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Error Detection in Practice

- CRCs are widely used on links
 - Ethernet, 802.11, ADSL, Cable ...
- Checksum used in Internet
 - IP, TCP, UDP ... but it is weak
- Parity
 - Is little used

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51

Error Correction (§3.2.1)

- Some bits may be received in error due to noise.
 How do we fix them?
 - Hamming code
 - Other codes
- And why should we use detection when we can use correction?

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Why Error Correction is Hard

- If we had reliable check bits we could use them to narrow down the position of the error
 - Then correction would be easy
- But error could be in the check bits as well as the data bits!
 - Data might even be correct

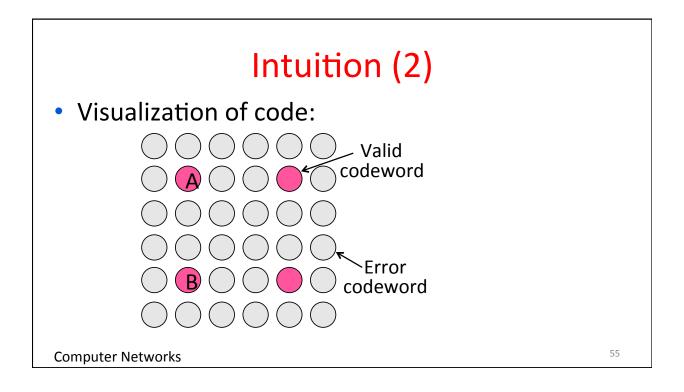
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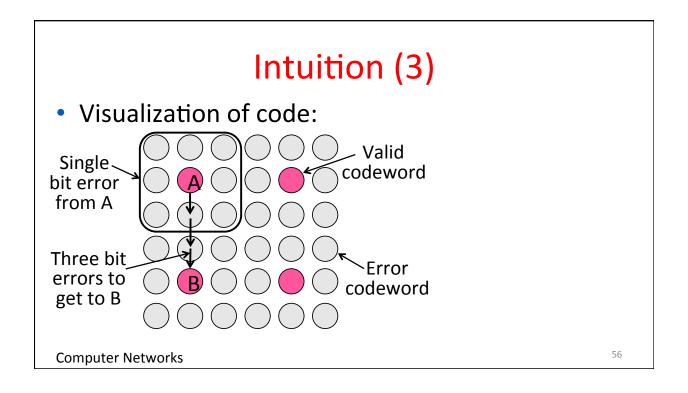
53

Intuition for Error Correcting Code

- Suppose we construct a code with a Hamming distance of at least 3
 - Need ≥3 bit errors to change one valid codeword into another
 - Single bit errors will be closest to a unique valid codeword
- If we assume errors are only 1 bit, we can correct them by mapping an error to the closest valid codeword
 - Works for d errors if HD ≥ 2d + 1

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Hamming Code

- Gives a method for constructing a code with a distance of 3
 - Uses $n = 2^k k 1$, e.g., n=4, k=3
 - Put check bits in positions p that are powers of 2, starting with position 1
 - Check bit in position p is parity of positions with a p term in their values
- Plus an easy way to correct [soon]

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5

Hamming Code (2)

- Example: data=0101, 3 check bits
 - 7 bit code, check bit positions 1, 2, 4
 - Check 1 covers positions 1, 3, 5, 7
 - Check 2 covers positions 2, 3, 6, 7
 - Check 4 covers positions 4, 5, 6, 7

1 2 3 4 5 6 7

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Hamming Code (3)

- Example: data=0101, 3 check bits
 - 7 bit code, check bit positions 1, 2, 4
 - Check 1 covers positions 1, 3, 5, 7
 - Check 2 covers positions 2, 3, 6, 7
 - Check 4 covers positions 4, 5, 6, 7

$$\underbrace{0}_{1} \underbrace{1}_{2} \underbrace{0}_{3} \underbrace{0}_{4} \underbrace{1}_{5} \underbrace{0}_{6} \underbrace{1}_{7}$$

$$p_1 = 0+1+1 = 0$$
, $p_2 = 0+0+1 = 1$, $p_4 = 1+0+1 = 0$

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50

Hamming Code (4)

- To decode:
 - Recompute check bits (with parity sum including the check bit)
 - Arrange as a binary number
 - Value (syndrome) tells error position
 - Value of zero means no error
 - Otherwise, flip bit to correct

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Hamming Code (5)

• Example, continued

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61

Hamming Code (6)

• Example, continued

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Hamming Code (7)

Example, continued

```
ightharpoonup \frac{0}{1} \frac{1}{2} \frac{0}{3} \frac{0}{4} \frac{1}{5} \frac{1}{6} \frac{1}{7}
p_1 = p_2 = p_4 = p_4 = p_2 = p_4 = p_4
```

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63

Hamming Code (8)

Example, continued

```
ightharpoonup \frac{0}{1} \frac{1}{2} \frac{0}{3} \frac{0}{4} \frac{1}{5} \frac{1}{6} \frac{1}{7}
p_1 = 0 + 0 + 1 + 1 = 0, \quad p_2 = 1 + 0 + 1 + 1 = 1, \quad p_4 = 0 + 1 + 1 + 1 = 1

Syndrome = 1 1 0, flip position 6
Data = 0 1 0 1 (correct after flip!)
```

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Other Error Correction Codes

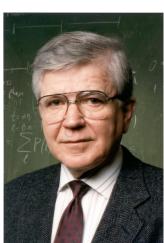
- Codes used in practice are much more involved than Hamming
- Convolutional codes (§3.2.3)
 - Take a stream of data and output a mix of the recent input bits
 - Makes each output bit less fragile
 - Decode using Viterbi algorithm (which can use bit confidence values)

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65

Other Codes (2) – LDPC

- Low Density Parity Check (§3.2.3)
 - LDPC based on sparse matrices
 - Decoded iteratively using a belief propagation algorithm
 - State of the art today
- Invented by Robert Gallager in 1963 as part of his PhD thesis
 - Promptly forgotten until 1996 ...



Source: IEEE GHN, © 2009 IEEE

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Detection vs. Correction

- Which is better will depend on the pattern of errors. For example:
 - 1000 bit messages with a bit error rate (BER) of 1 in 10000
- Which has less overhead?

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67

Detection vs. Correction

- Which is better will depend on the pattern of errors. For example:
 - 1000 bit messages with a bit error rate (BER) of 1 in 10000
- Which has less overhead?
 - It still depends! We need to know more about the errors

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Detection vs. Correction (2)

- Assume bit errors are random
 - Messages have 0 or maybe 1 error
- Error correction:
 - Need ~10 check bits per message
 - Overhead:
- Error detection:
 - Need ~1 check bits per message plus 1000 bit retransmission 1/10 of the time
 - Overhead:

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69

Detection vs. Correction (3)

- 2. Assume errors come in bursts of 100
 - Only 1 or 2 messages in 1000 have errors
- Error correction:
 - Need >>100 check bits per message
 - Overhead:
- Error detection:
 - Need 32? check bits per message plus 1000 bit resend 2/1000 of the time
 - Overhead:

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Detection vs. Correction (4)

- Error correction:
 - Needed when errors are expected
 - Or when no time for retransmission
- Error detection:
 - More efficient when errors are not expected
 - And when errors are large when they do occur

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71

Error Correction in Practice

- Heavily used in physical layer
 - LDPC is the future, used for demanding links like 802.11, DVB, WiMAX, LTE, power-line, ...
 - Convolutional codes widely used in practice
- Error detection (w/ retransmission) is used in the link layer and above for residual errors
- Correction also used in the application layer
 - Called Forward Error Correction (FEC)
 - Normally with an erasure error model
 - E.g., Reed-Solomon (CDs, DVDs, etc.)

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