

Distributed-Memory Models and Algorithms

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Collectives Protocols for Large Messages Collectives via Butterfly Networks	Collectives Protocols for Large Messages Collectives via Butterfly Networks		
Butterfly Reduce	Butterfly All-to-All		
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	Note that the size of the message stays the same at each level		
	$\mathcal{T}_{ ext{all-to-all}} = lpha \cdot \log(p) + eta \cdot \sum_{i=1}^{\log(p)} s = lpha \cdot \log(p) + eta \cdot s \cdot \log(p)$		
FTH Zirich, 9.12.2014, 262-2800.001	Its possible to do All-to-All in less bandwidth cost (as low as $\beta \cdot s$ by sending directly to targets) at the cost of more message (as high as $\alpha \cdot p$ if sending directly) ETH Zirich, 912 2014, 203290,001 Distributed.Memory Models and Algorithms 32/54		
ETT Zunch, 5.12.2014, 203-2000-00E Discributed-memory models and Argonanis - 31/-34	ETTT Zunch, 9.12.2019, 209-200-00E Distributed-memory models and Algorithms - 32/ 34		
BSP Model Introduction BSP model definition	Synchronization vs latency		
 The Bulk Synchronous Parallel (BSP) model (Valiant 1990) is a theoretical execution/cost model for parallel algorithms execution is subdivided into supersteps, each associated with a global synchronization within each superstep each processor can send and receive up to h messages (called an h-relation) the cost of sending or receiving h messages of size m is h · m · ĝ the total cost of a superstep is the max over all processors at that superstep when h = 1 the BSP model is closely related to the α-β model with β = ĝ and LogGP mode with G = ĝ we will focus on a variant of BSP with h = p and for consistency refer to ĝ as β and the cost of a synchronization as α 	 By picking h = p, we allow a global barrier to execute in the same time as the point-to-point latency this abstraction is good if the algorithm's performance is not expected to be latency-sensitive messages become non-blocking, but progress must be guaranteed by barrier collectives can be done in linear bandwidth cost with O(1) supersteps enables high-level algorithm development: how many collective protocols does the algorithm need to execute? global barrier may be a barrier of a subset of processors, if BSP is used recursively 		
ETH Zürich, 9.12.2014, 263-2800-00L Distributed-Memory Models and Algorithms 33/ 54	ETH Zürich, 9.12.2014, 263-2800-00L Distributed-Memory Models and Algorithms 34/54		
BSP Model Introduction	BSP Model Collective Communication		
Nonblocking communication	(Reduce-)Scatter and (All)Gather in BSP		
 The paradigm of sending non-blocking messages then synchronizing later is sensible MPI provides non-blocking 'l(send/recv)' primitives that may be 'Wait'ed on in bulk (these are slightly slower than blocking primitives, due to buffering) MPI and other communication frameworks also provide one-sided messaging primitives which are zero-copy (no buffering) and very efficient one-sided communication progress must be guaranteed by a barrier on all or a subset of processors (or MPI Win Flush between a pair) 	 When h = p all discussed collectives that require a single butterfly can be done in time T_{butterfly} = α + s ⋅ β i.e. they can all be done in one superstep Scatter: root sends each message to its target (root incurs s ⋅ β send bandwidth) Reduce-Scatter: each processor sends its portion to every other processor (every processor incurs s ⋅ β send bandwidth) Gather: send each message to root (root incurs s ⋅ β receive bandwidth) Allgather: each processor sends its portion to every other processor (every processor sends its portion to every other processor (every processor sends its portion to every other processor (every processor sends its portion to every other processor (every processor incurs s ⋅ β send and receive bandwidth) Allgather: each processor sends its portion to every other processor (every processor incurs s ⋅ β send and receive bandwidth) Men h < p, we could perform the above algorithms using a butterfly with 'radix'=h (number of neighbors at each butterfly level) in time T_{butterfly} = log_h(p) ⋅ α + s ⋅ β 		







Backup slides	
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