Sequential Consitency

Exercise 1

For the following executions, please indicate if they are sequentially consistent. All variables are intially set to 0.

- 1. P1: W(x,1); P2: R(x,0); R(x,1)
- 2. P1: W(x,1); P2: R(x,1); R(x,0);
- 3. P1: W(x,1); P2: W(x,2); P3: R(x,1); R(x,2);
- P1: W(x,1); P2: W(x,2); P3: R(x,2); R(x,1);
- P1: W(x,1);
 P2: W(x,2);
 P3: R(x,2); R(x,1);
 P4: R(x,1); R(x,2);
- P1: W(x,1); R(x,1); R(y,0);
 P2: W(y,1); R(y,1); R(x,1);
 P3: R(x,1); R(y,0);
 P4: R(y,0); R(x,0);
- P1: W(x,1); R(x,1); R(y,0);
 P2: W(y,1); R(y,1); R(x,1);
 P3: R(y,1); R(x,0);

Exercise 2

P1	P2	P3
x = 1;	y = 1;	z = 1;
print(y,z);	print(x,z);	print(x,y);

All variables are stored in a memory system which offers sequential consistency. All operations, even the print statements, are atomic. Atomicity means, that no operation can overlap with other operations. Are the following sequences legal outputs?

- 1. 001011
- 2. 001111
- 3. 001110

Explain your answer by showing one possible interleaving of the instructions that might lead to the legal output. In case of an illegal output, explain why no possible interleaving exists.

Design of Parallel and High Performance Computing *HS 2013 Markus Püschel, Torsten Hoefler Department of Computer Science ETH Zurich*

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Non-blocking caches

Consider a system with three processors. Each processor has a non-blocking cache (i.e., a processor does not stop upon encountering a cache miss; while the missing cache line is brought in from memory, the processor continues to execute instructions that are not data or control dependent upon a missing load).

The memory locations x and y are originally 0. The processors execute the following sequence:

P1: W(x,1); R(y,0); P2: W(y,1); R(y,1); R(x,1); P3: R(y,1); R(x,0);

Is this system sequentially consistent?

The x86 Memory Model: TLO+CC

- 1. Describe the memory model of the x86 architecture. Where does it differ from sequential consistency.
- 2. Two threads execute the following code (given in AT&T assembly syntax) on a machine using TLO+CC. Is it possible that the registers $eax = 0 \land ebx = 0$ after both threads have finished?. Would it be possible in sequential consistency?

Initial: All registers and memory locations are 0		
Thread A Thread B		
movl \$1, 0x42	movl \$1, 0x50	
movl 0x50, %eax	movl 0x42, %ebx	

In sequential consistency, it is impossible that both threads observe eax=0 \land ebx=0, however, in TLO+CC this is possible.

First, we will prove that it is impossible in sequential consistency. For this we first translate the above fragments into read and write statements:

Initial: All registers and memory locations are 0		
Thread A	Thread B	
W(a, 1)	W(b,1)	
R(b, x)	R(a,x)	
W(eax, x)	W(ebx, x)	

Now we assume that it **is** possible for both threads to finish and have eax=ebx=0 and show that this leads to a contradiction. Without loss of generality, we also assume Thread B is the last one to finish.

The first assumption tells us that the processes must execute the following read/write sequences:

$$\begin{split} W_A(a,1) &\to R_A(b,0) \to W_A(eax,0) \\ W_B(b,1) \to R_B(a,0) \to W_B(ebx,0) \end{split}$$

the second assumption translates to

 $W_A(eax, 0) \rightarrow W_B(ebx, 0)$

if we combine the three equations, we see that it is neccessary to have $W_A(a, 1) \rightarrow R_B(a, 0)$ at the same time $W_B(b, 1) \rightarrow R_A(b, 0)$ which means that our initial assumption was false, and it is eax=ebx=0 is impossible in sequential consistency.

In the x86 memory model however, it is legal to reorder the given sequences into

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Thread A	Thread B
R(b, x)	R(a,x)
W(a, 1)	W(b,1)
W(eax, x)	W(ebx, x)

which allows the following interleaving:

 $R_A(b,0) \to R_B(a,0) \to W_A(a,1) \to W_B(b,1) \to W_A(eax,0) \to W_B(ebx,0).$